Electroweak Processes in Few-Nucleon Systems

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Electroweak Processes

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Outline







Weak interactions



Collaborators

- F. Spadoni Graduate student, Pisa
- R. Schiavilla Jefferson Lab. & ODU, Norfolk (VA, USA)
- S. Pastore ANL (USA)
- L. Girlanda University of Salento & INFN-Lecce, Lecce (Italy)
- A. Kievsky & L.E. Marcucci INFN-Pisa & Pisa University, Pisa (Italy)

Chiral symmetry - QCD with *u* and *d* quarks only

$$q = \begin{pmatrix} u \\ d \end{pmatrix} \qquad q_{R/L} = \frac{(1 \pm \gamma^5)}{2} q = \begin{pmatrix} u_{R/L} \\ d_{R/L} \end{pmatrix} \qquad q_R' = Rq_R = \exp\left(-i\vec{\theta}_R \cdot \vec{\tau}/2\right) q_R$$
$$q_L' = Lq_L = \exp\left(-i\vec{\theta}_L \cdot \vec{\tau}/2\right) q_L$$

 $\vec{\theta}_R = \vec{\theta}_L = \vec{\theta}_V$: isospin transformation $\vec{\theta}_R = -\vec{\theta}_L = \vec{\theta}_A$: axial transformation

• \mathcal{L}_{QCD} (almost) invariant under the *L*, *R* transformations since m_u , m_d "small"

also for locals transformations introducing external currents

$$\mathcal{L} = \mathcal{L}_{\text{QCD}}^{0} + \overline{q}_{L}\gamma^{\mu} \left(l_{\mu}(x) + \frac{1}{3} v^{(s)}{}_{\mu}(x) \right) q_{L} + \overline{q}_{R}\gamma^{\mu} \left(r_{\mu}(x) + \frac{1}{3} v^{(s)}{}_{\mu}(x) \right) q_{R}$$
$$- \overline{q}_{R}(x) \left(s(x) + ip(x) \right) q_{L}(x) - \overline{q}_{L}(x) \left(s(x) - ip(x) \right) q_{R}(x)$$

•
$$r_{\mu}(x)
ightarrow r'_{\mu}(x) = R(x)r_{\mu}(x)R^{\dagger}(x) + iR(x)\partial_{\mu}R^{\dagger}(x)$$
, etc

• The external current are related to $A_{\mu}(x)$ and $W^{\pm}_{\mu}(x)$ to reproduce the EM and weak interactions of the quarks

Example

$$egin{array}{rll} r_{\mu}(x) &=& l_{\mu}(x) = -erac{ au_{z}}{2}\mathcal{A}_{\mu}(x) \qquad v_{\mu}^{(s)}(x) = -rac{e}{2}\mathcal{A}_{\mu}(x) \ \mathcal{L}_{em} &=& -e\mathcal{A}_{\mu}\left(rac{2}{3}\overline{u}\gamma^{\mu}u - rac{1}{3}\overline{d}\gamma^{\mu}d
ight) \end{array}$$

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Non-linear realization of the chiral symmetry for hadrons

[Weinberg, 1968, 1990],[CCWZ, 1969],[Gasser & Leutwyler, 1984], ...

"Compensator field" h

Nucleons

• $u = \exp(i\vec{\pi} \cdot \vec{\tau}/2f_{\pi})$

•
$$u' = Luh^{\dagger} = huR^{\dagger}$$

• $h \equiv h(L, R, \pi)$

• N' = hN

 However (∂_μN) does not transform "covariantly"

 $u_{\mu} = i[u^{\dagger}(\partial_{\mu} - ir_{\mu})u - u(\partial_{\mu} - il_{\mu})u^{\dagger}] \qquad D_{\mu} = \partial_{\mu} + \frac{1}{2}[u^{\dagger}(\partial_{\mu} - ir_{\mu})u + u(\partial_{\mu} - il_{\mu})u^{\dagger}] - iv_{\mu}^{(s)}$

- Transformations: $u'_{\mu} = h u_{\mu} h^{\dagger}$ $(D_{\mu} N)' = h D_{\mu} N$
- Lagrangian $\mathcal{L}_{\pi N} = \overline{N} \left(i \gamma^{\mu} D_{\mu} m_{N} + \frac{g_{A}}{2} \gamma^{\mu} \gamma^{5} u_{\mu} \right) N + \dots + \frac{C_{S} \overline{N} N \overline{N} N + \dots$
- it contains an infinite number of LECs
- Contributions organized as an expansion over $(Q/\Lambda_{\chi})^{\nu}$ [$\Lambda_{\chi} \approx 1 \text{ GeV}$]

NN, 3N, ..., potentials from the EFT

NN Potential V

- Two methods:
 - S-matrix: for a given process $NN \rightarrow NN$ define V so that (on-shell) $\langle NN | T_{EFT} | NN \rangle \equiv \langle NN | T_V | NN \rangle$
 - Unitary transformation: find *U* in order to decouple $|NN\rangle$ Hilbert space from $|NN\pi\rangle$, etc.
- Realization thanks to the chiral counting: all terms can be organized as powers of Q/Λ_{χ} , $Q \sim$ small momenta or the pion mass
- Alternatively: Lattice χEFT [Lee et al., 2010]

Example

- $T_{\text{EFT}} = T_V \equiv V + VG_0V + \cdots$ $G_0 = (E H_0 + i\epsilon)^{-1}$
- $T_{\rm EFT} \equiv T_{\rm EFT}^{(0)} + T_{\rm EFT}^{(1)} + T_{\rm EFT}^{(2)} \dots$ $V \equiv V^{(0)} + V^{(1)} + V^{(2)} \dots$ $T_{\rm EFT}^{(n)}, V^{(n)} \sim Q^n$

$$\langle \boldsymbol{p}_{1}^{\prime} \boldsymbol{p}_{2}^{\prime} | V^{(n^{\prime})} G_{0} V^{(n)} | \boldsymbol{p}_{1} \boldsymbol{p}_{2} \rangle = \sum_{\boldsymbol{p}_{1}^{\prime \prime} \boldsymbol{p}_{2}^{\prime \prime}} \frac{ \langle \boldsymbol{p}_{1}^{\prime} \boldsymbol{p}_{2}^{\prime} | V^{(n^{\prime})} | \boldsymbol{p}_{1}^{\prime \prime} \boldsymbol{p}_{2}^{\prime \prime} \rangle \langle \boldsymbol{p}_{1}^{\prime \prime} \boldsymbol{p}_{2}^{\prime \prime} | V^{(n)} | \boldsymbol{p}_{1} \boldsymbol{p}_{2} \rangle}{E_{\boldsymbol{p}_{1}} + E_{\boldsymbol{p}_{2}} - E_{\boldsymbol{p}_{1}}^{\prime \prime} - E_{\boldsymbol{p}_{2}}^{\prime \prime} + i\epsilon} \sim Q^{n+n^{\prime}+1}$$

• Then $V^{(0)} = T^{(0)}_{\text{EFT}}$ $V^{(1)} = T^{(1)}_{\text{EFT}} - V^{(0)}G_0V^{(0)}$, etc

NN, 3N, ..., potentials from the EFT

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$$\left< \boldsymbol{p}_{1}^{\prime} \boldsymbol{p}_{2}^{\prime} \right| V^{(n^{\prime})} G_{0} V^{(n)} \left| \boldsymbol{p}_{1} \boldsymbol{p}_{2} \right> = \sum_{\boldsymbol{p}_{1}^{\prime \prime} \boldsymbol{p}_{2}^{\prime \prime}} \frac{ \left< \boldsymbol{p}_{1}^{\prime} \boldsymbol{p}_{2}^{\prime} \right| V^{(n^{\prime})} \left| \boldsymbol{p}_{1}^{\prime \prime} \boldsymbol{p}_{2}^{\prime \prime} \right> \left< \boldsymbol{p}_{1}^{\prime \prime} \boldsymbol{p}_{2}^{\prime \prime} \right| V^{(n^{\prime})} \left| \boldsymbol{p}_{1} \boldsymbol{p}_{2} \right>}{E_{\boldsymbol{p}_{1}} + E_{\boldsymbol{p}_{2}} - E_{\boldsymbol{p}_{1}}^{\prime \prime} - E_{\boldsymbol{p}_{2}}^{\prime \prime} + i\epsilon} \sim Q^{n+n^{\prime}+1}$$

• Then
$$V^{(0)} = T^{(0)}_{\text{EFT}}$$
 $V^{(1)} = T^{(1)}_{\text{EFT}} - V^{(0)}G_0V^{(0)}$, etc

For more information see for example [Epelbaum *et al.*, NPA **714**, 535 (2003)]

| | 2N force | 3N force | 4N force |
|-------------------|-----------------|----------|----------|
| LO | XH | — | _ |
| NLO | ХЫАМЦ | — | _ |
| N²LO | 허석 | HH HX X | — |
| N ³ LO | X0444- 4908- | 构州网- | 174 I #1 |

NN interaction

- J-N3LO [Epelbaum and Coll, 1998-2006]
- I-N3LO [Entem & Machleidt, 2003]

Part of the LEC's fitted to the NN database or πN database

3N interaction

- J-N2LO [Epelbaum et al, 2002]
- N-N2LO [Navratil, 2007]
- 3N force at N3LO [see Kreb's talk]
- . At N2LO there are two LECS c_D and c_E : fitted to some 3N data (see later)
 - At N3LO no new parameters
 - At N4LO 10 new LECs [Girlanda *et al.,* 2011]

Basic problem: transition $|\alpha\rangle + \gamma \rightarrow |\beta\rangle$

$$\langle \beta | \mathcal{H}_{e.m.} | lpha; \boldsymbol{q} \lambda
angle = \langle \Psi_{\beta} | \mathcal{K}_{1} | \Psi_{lpha}
angle \qquad \mathcal{K}_{1} = rac{-e}{\sqrt{2\omega\Omega}} \int d\boldsymbol{x} \; e^{i \boldsymbol{q} \cdot \boldsymbol{x}} \; \hat{\epsilon}_{\boldsymbol{q}\lambda} \cdot \hat{\boldsymbol{J}}(\boldsymbol{x})$$

- \mathcal{K}_1 acts only on the nucleons' d.o.f.
- $|\alpha\rangle$, $|\beta\rangle$ initial & final nuclear states, Ψ_{α} , Ψ_{β} corresponding w.f.
- $\boldsymbol{q}, \omega, \hat{\epsilon}_{\boldsymbol{q}\lambda} = \text{momentum, energy, polarization of the emitted photon}$
- for virtual photons, one needs also the m.e. of $\hat{q} \cdot \hat{J}$ and ρ

$$J^{\mu}(\boldsymbol{q}) = \int d\boldsymbol{x} \; e^{i \boldsymbol{q} \cdot \boldsymbol{x}} \; \widehat{J}^{\mu}(\boldsymbol{x}) \qquad \mu = 0, 1, 2, 3$$

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Meson exchange currents



$$\widehat{\boldsymbol{J}}(\boldsymbol{x}) = \sum_{i} \widehat{\boldsymbol{j}}_{i}(\boldsymbol{x}) + 2B + 3B + \dots$$

Current conservation $\nabla \cdot \widehat{\boldsymbol{J}}(\boldsymbol{x}) = -i[H, \rho(\boldsymbol{x})]$

• Strict interplay between H, \hat{J} and $\hat{\rho}$

$$\widehat{\rho}(\boldsymbol{x}) = \sum_{i=1}^{A} \frac{1 + \tau_{\boldsymbol{z}}(i)}{2} \delta(\boldsymbol{r}_{i} - \boldsymbol{x})$$

• [Buchmann *et al*, 1985]

- [Riska, 1989], [Schiavilla et al, 1990]
- EFT approach: *H* and J^{μ} derived from the same Lagrangian.

Current at N3LO

[Park et al, 1993], [Kolling et al, 2009], [Pastore et al, 2009]



black square= $(Q/M_N)^2$ relativistic correction to the $NN\gamma$ vertex

Note: $NN\gamma$ vertex = $(e_N/2M_N)(\mathbf{p}+\mathbf{p}')+i(e_N+\kappa_N)\mu_N(\boldsymbol{\sigma}\times\mathbf{q})$ it takes into account the Pauli term + pion loop corrections



N3LO (Q¹) terms



black dot= three $(Q/\Lambda_{\chi})^2$ vertices

Most of the LECs enter also the NN potential. There are 5 uncostrained LECs $(\rightarrow \mu_d, \mu_{3H}, \mu_{3He}, \text{etc.})$

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HH variational method: A. Kievsky, S. Rosati, MV, L.E. Marcucci, and L. Girlanda J. Phys. G, **35**, 063101 (2008)

A benchmark for A = 4

- AGS: Deltuva & Fonseca, PRL 98 162502 (2007)
- FY: Lazauskas & Carbonell, PRC 70, 044002 (2004)
- $n {}^{3}\text{H}$ & $p {}^{3}\text{He}$ elastic scattering $0 \le E_{c.m.} \le B_{3} B_{2} \approx 5.5$ MeV

NN interaction models:

- AV18 [Wiringa, Stoks & Schiavilla (1995)]
- I-N3LO [Entem & Machleidt (2003)]
- V_{low-q} [Bogner, Kuo & Schwenk, (2003)] (derived from the CD-Bonn potential [Machleidt (2001)])
- Results reported in [MV et al., 2011]

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$n - {}^{3}\text{H}$ scattering (I-N3LO pot.)



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$n - {}^{3}\text{H}$ scattering (I-N3LO pot.)



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$n - {}^{3}\text{H}$ scattering (I-N3LO pot.)



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$p - {}^{3}\text{He}$ scattering (I-N3LO pot.)



Predictions by different potentials





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Results for $\overline{A = 3, 4}$ (1)



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Study of the 3N force in A = 4 scattering in progress

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Fit of the LECS

Current at N3LO ($\mathcal{O}(Q)$) \leftrightarrow NN potential at NLO ($\mathcal{O}(Q^2)$) $\boldsymbol{q} \cdot \widehat{\boldsymbol{J}}(\boldsymbol{q}) = -[H, \rho(\boldsymbol{q})]$

Fit of the LECs

- We have constructed a NN potential at NLO and fitted the corresponding LECs to the NN database: [Pastore et al., 2009]
- In *J* there are 5 additional LECs: fitted to the A = 2, 3 magnetic moments & n p capture cross section at thermal energies using the I-N3LO NN potential
- The model depends on a cutoff Λ ($\Lambda = 500 600$ MeV)
 - the dependence on Λ is used to test the convergence
 - [Girlanda et al., 2010]



Deuteron-photodisintegration

- Wave functions calculated using I-N3LO for Λ = 500 & 600 MeV
- Observable dominated by the E1 transitions



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$n - d \& n - {}^{3}\text{He}$ radiative captures at thermal energies

- n d capture from the ²S_{1/2} & ⁴S_{3/2} waves
- $n {}^{3}\text{He}$ capture from the ${}^{3}S_{1}$ wave

Scattering lenghts

| | | | _ |
|--------------------------------|---------------|-----------|---|
| Case | I-N3LO/N-N2LO | Expt. | 4 |
| a _{nd} doublet | 0.675 | 0.645(10) | |
| and quartet | 6.342 | 6.35(2) | |
| $a_{n^{3}\mathrm{He}}$ doublet | 3.37 | 3.278(53) | _ |

| n - d & n - 3 | He capture cross | sections |
|---------------|------------------|----------|
|---------------|------------------|----------|

| Order | σ_{n-d} [mb] | $\sigma_{n-^{3}\mathrm{He}}\left[\mub ight]$ |
|---------------|---------------------|--|
| LO | 0.235 | 10.6 |
| +NLO | 0.361 | 5.9 |
| +N2LO | 0.334 | 0.9 |
| +N3LO (loops) | 0.276 | 1.4 |
| +N3LO (LECs) | 0.478 | 48.4 |
| Expt | 0.508(15) | 52(4) |



Compton scattering (1)

Nucleon Polarizabilities

Induced dipoles by an EM field: $\mathbf{d} = \alpha \mathbf{E} \ \boldsymbol{\mu} = \beta \mathbf{B}$

$$H_{\rm eff} = -2\pi \left[\alpha \mathbf{E}^2 + \beta \mathbf{B}^2 + \gamma_{E1E1} \boldsymbol{\sigma} \cdot \left(\mathbf{E} \times \frac{\partial \mathbf{E}}{\partial t} \right) + \cdots \right]$$

Experimental status [Griesshammer et al., 2012]

• proton: from $\gamma p \rightarrow \gamma p$ experiments (MAMI [de Lèon *et al.*, 2001], ...)

- $\alpha_p = (10.7 \pm 0.3 \text{(stat)} \pm 0.2 \text{(Baldin)} \pm 0.8 \text{(theory)}) \ 10^{-4} \text{fm}^3$
- $\beta_p = (3.1 \pm 0.3 \text{(stat)} \pm 0.2 \text{(Baldin)} \pm 0.8 \text{(theory)}) \ 10^{-4} \text{fm}^3$

• neutron: from $\gamma d \rightarrow \gamma d$ experiments or with other methods

- Data sparse and not accurate [Illinois (1994), SAL (2000), Lund (2003)]
- $\alpha_n = (11.1 \pm 1.8(\text{stat}) \pm 0.4(\text{Baldin}) \pm 0.8(\text{theory})) \ 10^{-4} \text{fm}^3$
- $\beta_n = (4.1 \mp 1.8(\text{stat}) \pm 0.4(\text{Baldin}) \pm 0.8(\text{theory})) \ 10^{-4} \text{fm}^3$
- Theory input needed to separate: 1) structure effects 2) MEC effects

 New experiments on d, ³He, ⁶Li planned/in progress at TUNL/HγGS, MaxLab (Lund), S-DALINAC (Darmstaad)

Status of the calculations

- First applications to \(\gamma N\): [Bernard et al, 1992]
- Recent applications to γd:
 - Beane et al, 2004]: NNLO, no rescattering
 - Griesshammer & Shukla, 2009]: NLO, rescattering calculated with AV18
 - Review: [Griesshammer et al., 2012]
- Only a few applications to γ^{3} He

Aims of the new calculation

- $NN\gamma \rightarrow NN$ transition operators derived from the EFT at N3LO [Pastore et al., 2009]
- NN interaction derived from the same EFT (at present we have used the I-N3LO potential by Entem & Machleidt)
- Future: applications to ³He and ⁶Li

General framework



termini dispersivi

$$\langle d_{f}\gamma_{f}|\mathcal{T}|d_{i}\gamma_{i}\rangle = \langle \Psi_{f}^{d}|\mathcal{K}_{2} + \underbrace{\mathcal{K}_{1}^{\dagger}G\mathcal{K}_{1} + \mathcal{K}_{1}G\mathcal{K}_{1}^{\dagger}|\Psi_{i}^{d}}_{\text{Dispersive part}}\rangle$$

• The Green function $G = (E - H + i\epsilon)^{-1}$ describes the rescattering of the *NN* pair between the two EM vertices

- NN interaction from [Entem & Machleidt, 2003]
- The irriducible "kernel" \mathcal{K}_2 derived from the EFT at NLO ($\sim Q^{-2}$) (PRELIMNARY)
 - In literature K₂ is derived up to NNLO [Griesshammer et al, 2012]
 - inclusion of Δ d.o.f. \rightarrow [Hildebrandt Ph.D. Thesis, München, 2005]



 Diagrams (a): contribution to K₂ "seagull" (SG) & "spin-orbit" (SO)

$$\mathcal{K}_2^{(SG)} = \sum_j \frac{e_j}{2M} \boldsymbol{\epsilon}_i \cdot \boldsymbol{\epsilon}_f^* \boldsymbol{e}^{i(\boldsymbol{q}-\boldsymbol{q}')\cdot\boldsymbol{r}_j} , \quad \boldsymbol{e}_j = \frac{1+\tau_z^j}{2}$$

- Note: the SG can be derived from $H_{NR} = (1/2M)(\boldsymbol{p} \mathbf{e}\boldsymbol{A})^2$
- SG: order $\sim Q^{-3},$ SO=corrections to the SG $\sim Q^{-2}$
- Diagrams (b): contribution to K₂ from the "polarization" of the nucleon
 - They can be used to estimate α and β
 [Bernard *et al*, 1992]
 - We'll consider α and β as free parameters $(\alpha_j = \alpha_p (1 + \tau_z^j)/2 + \alpha_n (1 - \tau_z^j)/2)$

$$\begin{array}{lll} \mathcal{C}_{2}^{(\alpha\beta)} & = & \sum_{j} \Bigl[-2\pi\alpha_{j}\boldsymbol{\epsilon}_{i}\cdot\boldsymbol{\epsilon}_{f}^{*}\,qq' \\ & & -2\pi\beta_{j}(\boldsymbol{q}\times\boldsymbol{\epsilon}_{i})\cdot(\boldsymbol{q}'\times\boldsymbol{\epsilon}_{f}^{*}) \Bigr] \boldsymbol{e}^{j(\boldsymbol{q}-\boldsymbol{q}')\cdot\boldsymbol{r}_{j}} \end{array}$$

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Diagrams (2)



 Diagrams (c-f): Contributions taken into account by the "dispersive" part

 $\langle \Phi^{\textit{f}}_{\textit{d}} | \mathcal{K}_1^{\dagger} \textbf{G} \mathcal{K}_1 + \mathcal{K}_1 \textbf{G} \mathcal{K}_1^{\dagger} | \Phi^{\textit{i}}_{\textit{d}} \rangle$

• (c1), (f1)
$$\sim$$
 Q $^{-3}$, (e1), (f2) \sim Q $^{-4}$

Exact resummation [Ishikawa et al., 1998]

•
$$|\Psi_1\rangle = G\mathcal{K}_1 |\Phi_d^i\rangle$$

•
$$|\Psi_2\rangle = G \mathcal{K}_1^{\dagger} |\Phi_d^i\rangle$$

•
$$(E - H + i\epsilon)|\Psi_1\rangle = \mathcal{K}_1|\Phi_d^i\rangle$$
 $(E = q - B_d > 0)$

•
$$(E - H + i\epsilon)|\Psi_2\rangle = \mathcal{K}_1^{\dagger}|\Phi_d^i\rangle$$

 $(E = -q' - B_d < 0)$

• Diagrams (g): contribution taken into account by the fact that $|\Phi_d\rangle$ are solution of the Schroedinger equation

Diagrams (h): Contribution to K₂

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Photodisintegration

•
$$\Im[\langle \Phi_d^f | \mathcal{K}_1^\dagger G \mathcal{K}_1 | \Phi_d^i \rangle \sim \sigma_{\gamma+d \to n+p}$$

- In our calculation $[\langle \Phi_d^f | \mathcal{K}_1^{\dagger} G \mathcal{K}_1 | \Phi_d^i \rangle = \langle \Phi_d^f | \mathcal{K}_1^{\dagger} | \Psi_1 \rangle$
- At $E_{\gamma} = 20 \text{ MeV} \sigma_{\gamma+d \rightarrow n+p} = 540.7 \ \mu\text{b}$: we find 541.1 μb (I-N3LO + JEFT $\Lambda = 500 \text{ MeV}$)

Thomson limit

- For $E_{\gamma} \rightarrow 0$, the calculation should reproduce the Thomson limit
- Compton amplitude $\mathcal{M}^{(TL)} = e^2/M_d$ (note: $\mathcal{M}^{(SG)} = e^2/M \approx 2\mathcal{M}^{(TL)}$)
- True if V, \mathcal{K}_1 , and \mathcal{K}_2 are consistent (current conservation)



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49 MeV -- I-N3LO + JEFT (Λ=500 MeV)

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Sensitivity to $\alpha_n \& \beta_n$



49 MeV -- I-N3LO + JEFT (Λ=500 MeV)

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β -decay and the 3N force



[Gardestig & Phillips, 2006], [Gazit et al., 2009]

$$d_R = rac{M_n}{\Lambda_\chi g_A} rac{c_D}{D} + rac{1}{3} M_N (c_3 + 2c_4)$$

New fit of c_D and c_E using ³H binding energy and tritium β -decay lifetime



New versions of the 3N at N2LO: first application for μ -capture on d and ³He [Marcucci *et al.*, 2012]

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pp capture at astrophysical energies

Aim: new calculation of the astrophysical factor S_{11} of the $p + p \rightarrow {}^2H + e^- + \bar{\nu}_e$ reaction

$$S_{11}(E) = S_{11} + S'_{11}E + \frac{1}{2}S''_{11}E^2 + \cdots$$

Preliminary Results – units 10^{-25} MeV b I-N3LO NN interaction + weak transition operator derived from EFT

| | S ₁₁ | S' ₁₁ /S ₁₁ [MeV ⁻¹] | S_{11}''/S_{11} [MeV ⁻²] |
|----------------------|-----------------|--|--|
| $LO \Lambda = 500$ | 3.98 | 11.7 | 270 |
| LO $\Lambda = 600$ | 3.96 | 11.7 | 270 |
| Full $\Lambda = 500$ | 4.05 | 11.7 | 270 |
| Full $\Lambda = 600$ | 4.03 | 11.7 | 270 |

Motivations of this work

 consistent calculations for a variety of processes using potential/current/wave functions derived from the same EFT

Applications

- Main interest: test of 3N interaction in A = 3, 4 systems, study of reactions of astrophysical interest
 - p d & d d captures, form factors of light nuclei, *ldots*)
 - Compton scattering on ³He & ⁶Li (in the near future new data at HIγS & Lund)
 - weak transitions (*pp* capture, μ -capture, parity-violation in nuclei, . . .)

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