



# The Neutron Structure Functions from BoNuS using CLAS

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Elba XII Workshop

Electron-Nucleus Scattering XII

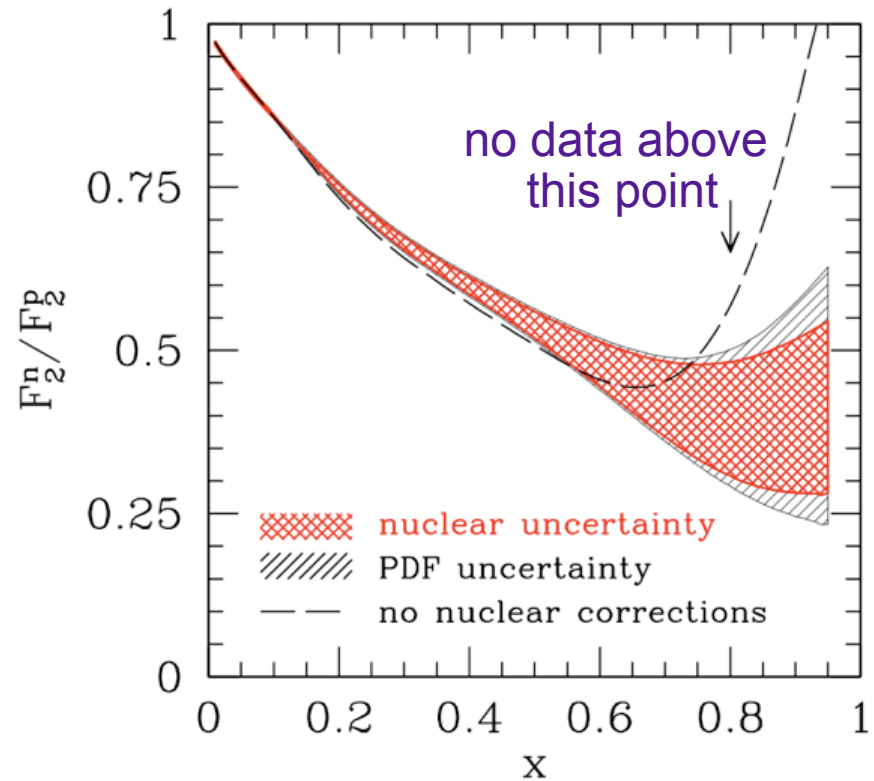
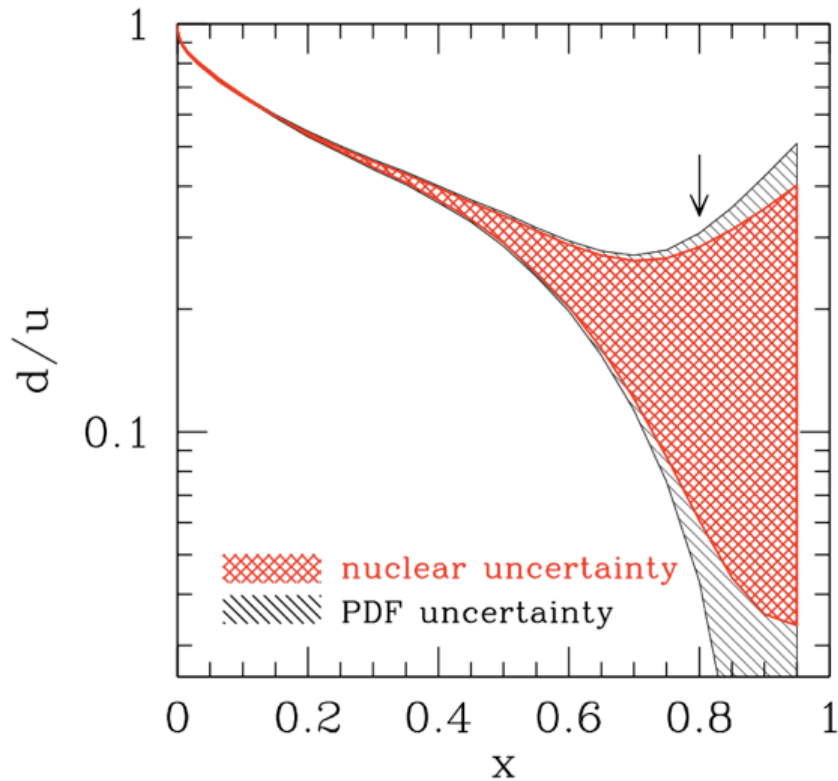
Marciana Marina, Isola d'Elba, Italy

25-29 June 2012



# The Problem

- There is no free ~~lunch~~ neutron target
- Nuclear uncertainties inhibit extracting  $F_2^n$  from  $d(e,e')X$  at large  $x$
- We need to measure the neutron free of nuclear effects



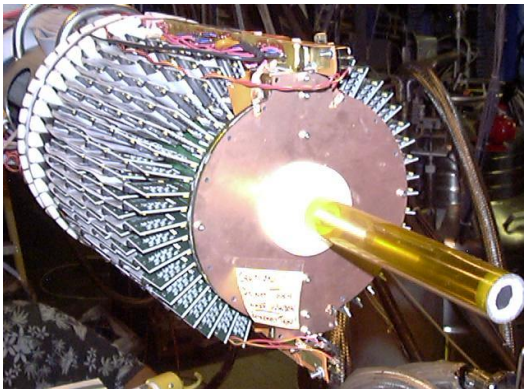
Accardi, AIP Conf. Proc. **1374**(11)383



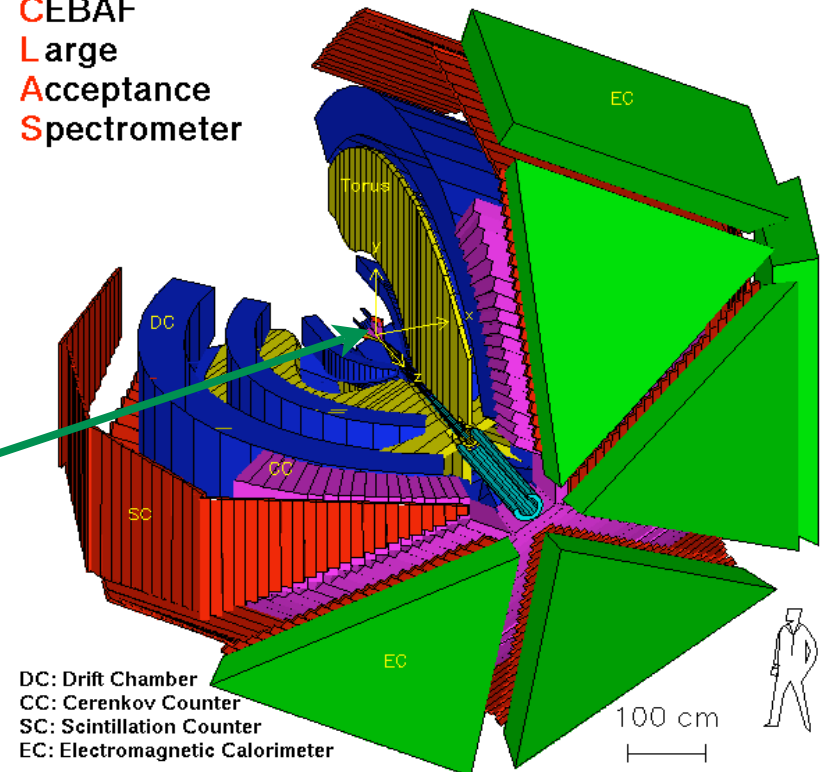
# A Solution: CLAS with RTPC

- Bound Nucleon Structure Experiment
- $d(e, e'p_s)X$  [(deep) inelastic]
- Deuterium target, spectator proton
- $70 < p_s < 150$  MeV/c
- JLab Hall B CLAS with an RTPC
- Measure  $F_2^n$  at high  $x$

N. Baillie, S. Tkachenko,  
W. Melnitchouk, K. Griffioen,  
S. Kuhn, C. Keppel, M.E. Christy,  
H. Fenker, J. Zhang, S. Bültmann

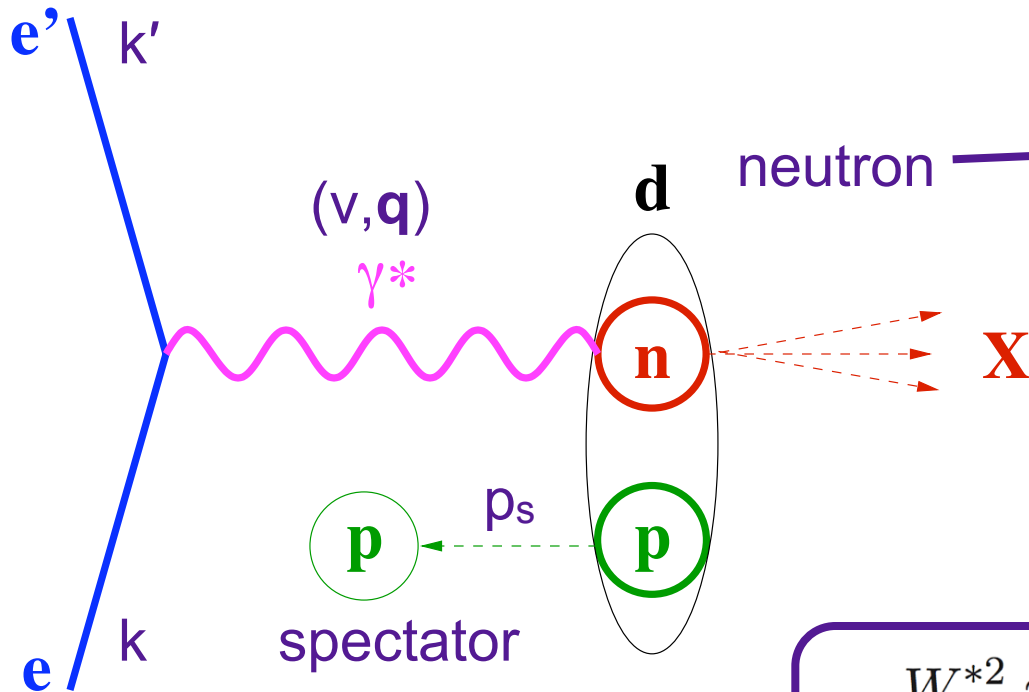


CEBAF  
Large  
Acceptance  
Spectrometer





# $d(e, e' p_s) X$



before

$$\begin{aligned}
 p_n &= (M_d - E_s, -\vec{p}_s) \\
 M_d &= E_n + E_s \\
 E_n &= M_d - \sqrt{M_s^2 + p_s^2} \\
 M^{*2} &= (M_d - E_s)^2 - \vec{p}_s^2
 \end{aligned}$$

after

$$\begin{aligned}
 W^{*2} &\approx M^{*2} - Q^2 + 2M_s\nu(2 - \alpha_s) \\
 \alpha_s &= \frac{E_s - p_{s\parallel}}{M_s} \\
 x^* &= \frac{Q^2}{2p_n \cdot q} \approx \frac{Q^2}{2M_s\nu(2 - \alpha_s)} = \frac{x}{2 - \alpha_s}
 \end{aligned}$$

- Plane-wave impulse approximation
- Backward-emitted p is a spectator
- Struck neutron is off-shell
- $p_s$  and  $p_n$  are equal and opposite
- Lorentz invariants are corrected for initial neutron 4-momentum



# PWIA Spectator Formalism

$$\frac{d\sigma}{dx^* dQ^2} = \frac{4\pi\alpha_{EM}^2}{x^* Q^4} \left[ \frac{y^2}{2(1+R)} + (1-y) + \frac{M^{*2} x^{*2} y^2}{Q^2} \frac{1-R}{1+R} \right] F_2(x^*, \alpha_s, p_T, Q^2) \times S(\alpha_s, p_T) \frac{d\alpha_s}{\alpha_s} d^2 p_T,$$

Cross Section

Off-Shell  $F_2$

$$R = \sigma_L / \sigma_T$$

Light Cone

Spectral Function

Nonrelativistic w.f.

$$P(\vec{p}_s) = J |\psi_{NR}(p_s)|^2$$

$$J = 1 + \frac{p_{s||}}{E_n} = \frac{(2 - \alpha_s) M_d}{2(M_d - E_s)}$$

$$S(\alpha_s, p_T) \frac{d\alpha_s}{\alpha_s} d^2 p_T = P(\vec{p}_s) d^3 p_s$$

$$S^{LC}(\alpha_s, p_T) \frac{d\alpha_s}{\alpha_s} d^2 p_T = |\psi_{NR}(|\vec{k}|^2)|^2 d^3 k$$

$$|\vec{k}| = \sqrt{\frac{M^2 + p_T^2}{\alpha_s(2 - \alpha_s)} - M^2} \quad \alpha_s = 1 - \frac{k_{||}}{\sqrt{M^2 + \vec{k}^2}}$$

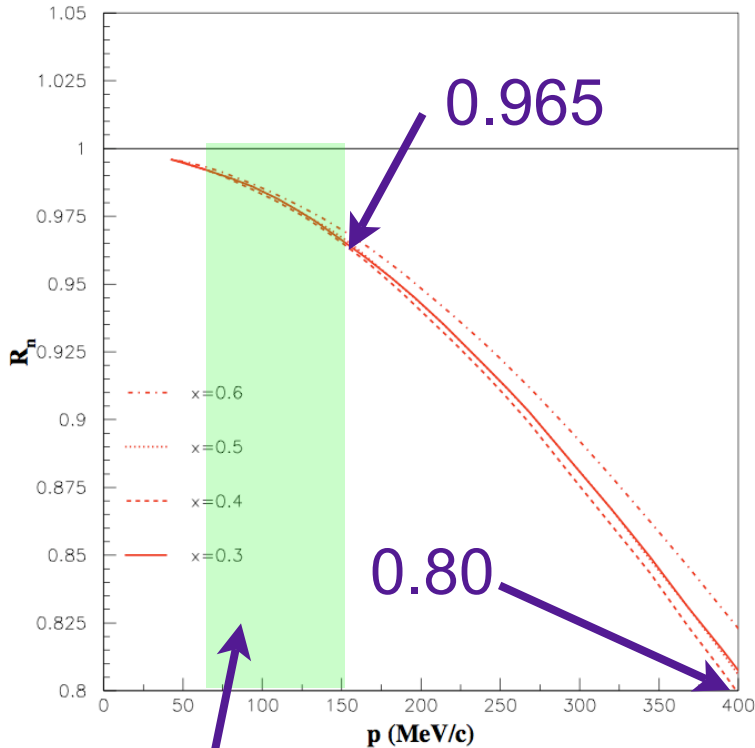
$$k_0 = \sqrt{M^2 + \vec{k}^2} \quad \vec{p}_T = \vec{k}_T$$

$$\int \int \int S^{LC}(\alpha_s, p_T) \frac{d\alpha_s}{\alpha_s} d^2 p_T = 1$$



# Off-Shell Structure Functions

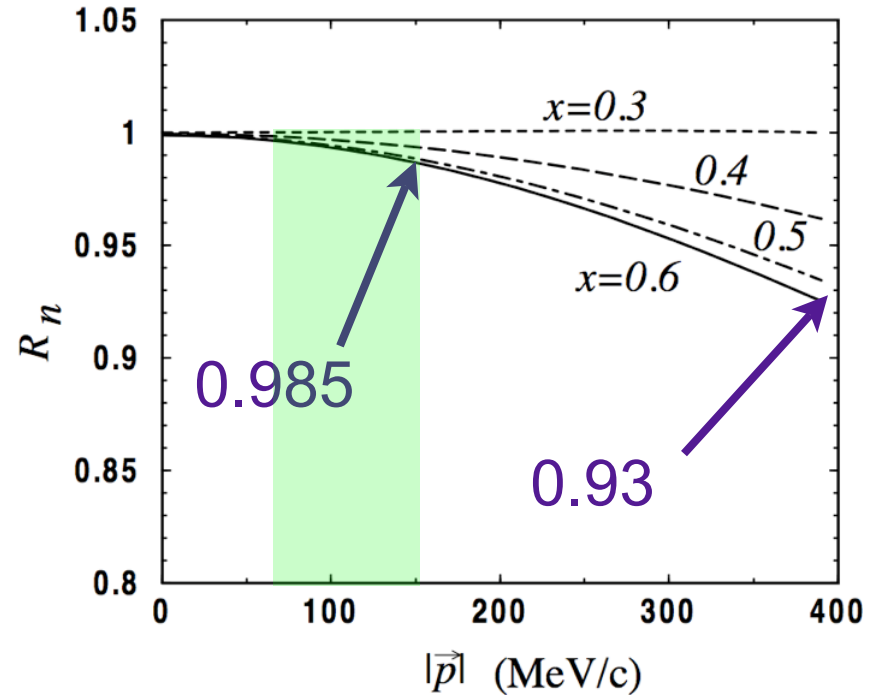
Liuti & Gross PLB356(95)157



$$R_n \equiv (F_2^n)^{\text{eff}} / (F_2^n)^{\text{free}}$$

BoNuS  $p_s$   
detection range

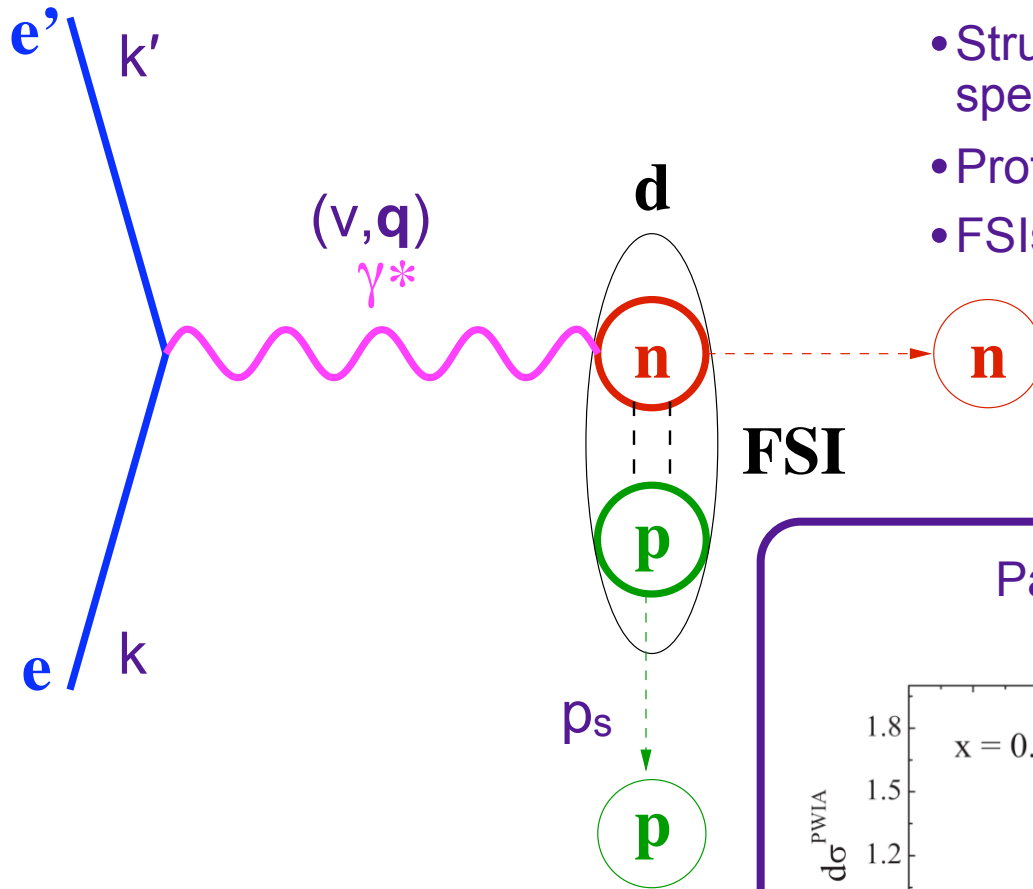
Melnitchouk *et al.*, PLB335(94)11



- $R_n$  decreases with  $p_s$  or  $\alpha_s$
- At  $x^*=0.5$  and  $p_s=400$  MeV/c,  $R_n$  deviates from unity by 7-20% in these models



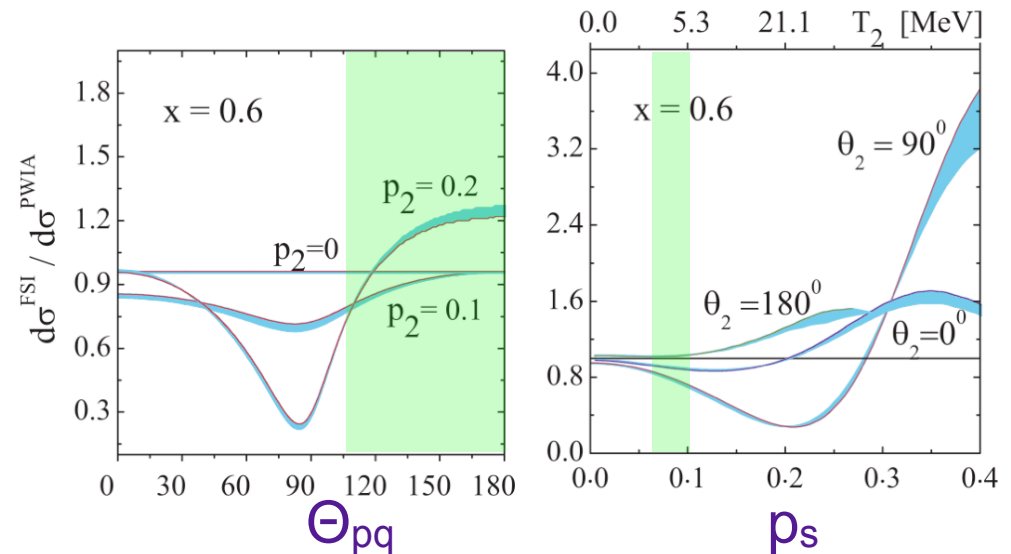
# Final State Interactions



- Struck neutron can interact with the spectator proton
- Proton momentum is enhanced
- FSIs are small at low  $p_s$  and large  $\Theta_{pq}$

- Several groups have calculated FSIs
- $\Theta_{pq} > 110^\circ$  and  $p_s < 100$  MeV/c greatly reduces FSIs

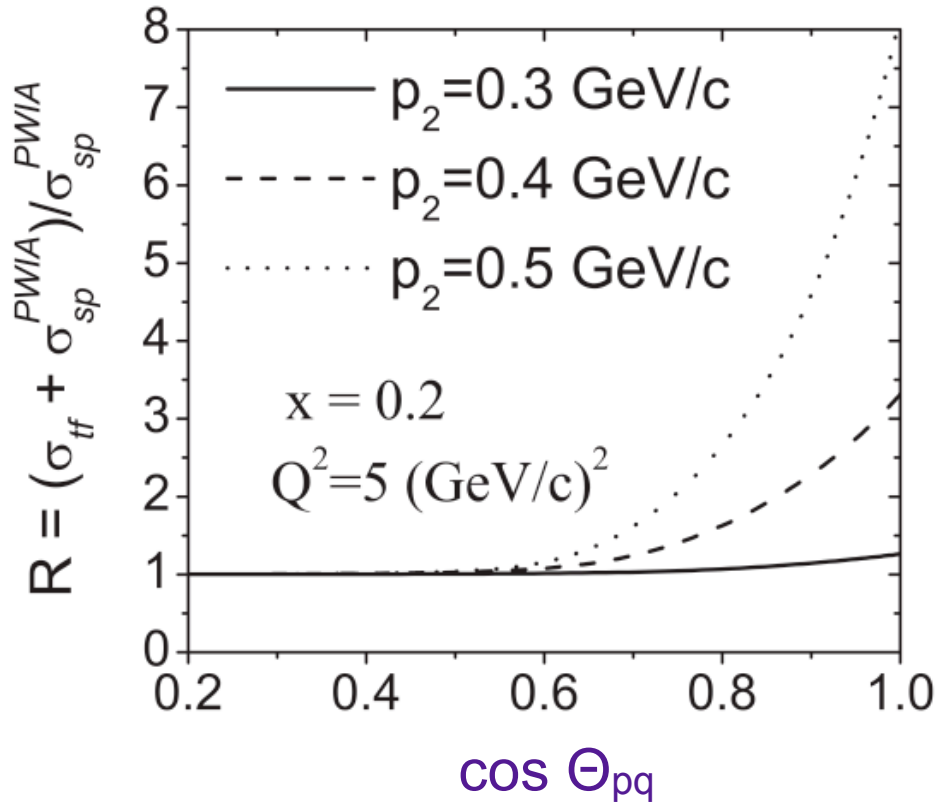
Palli *et al.*, PRC80(09)054610





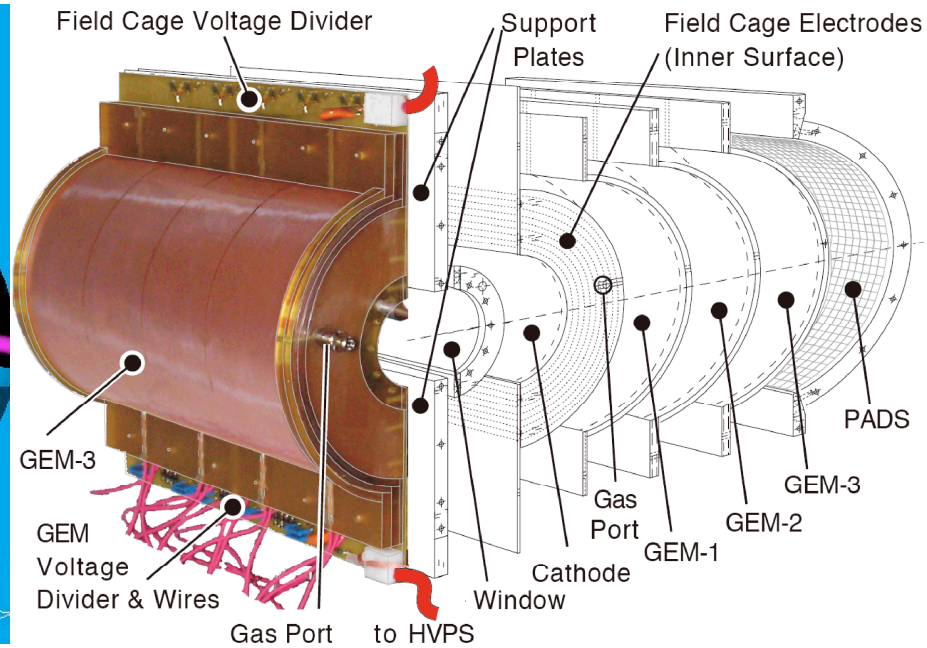
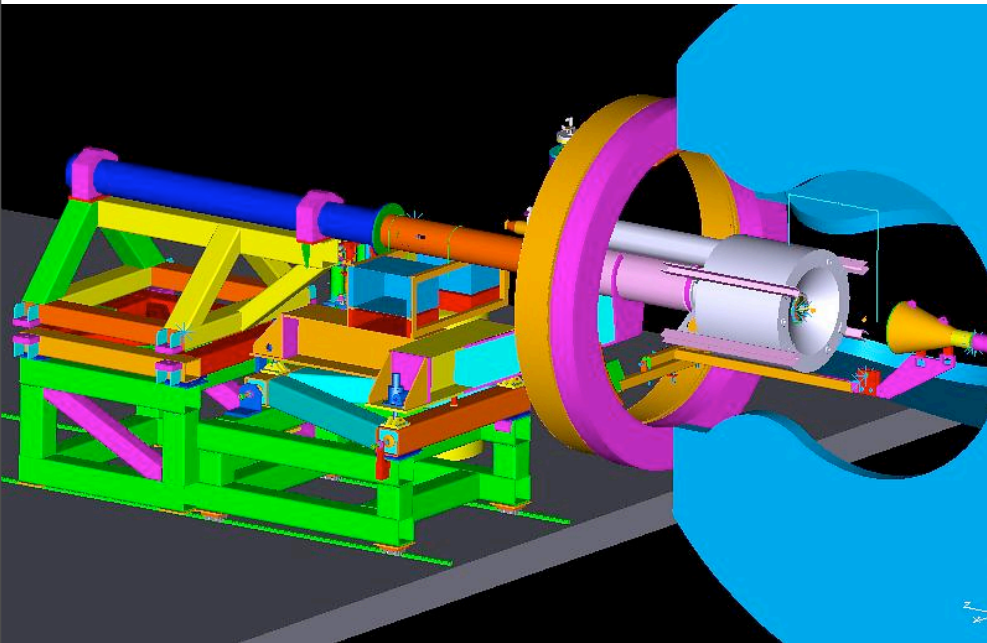
# Target Fragmentation

Palli *et al.*, PRC80(09)054610

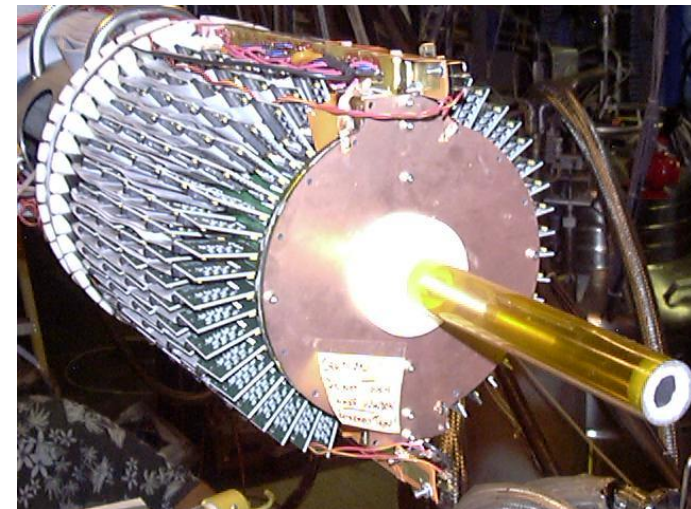


- Target fragmentation enhances the proton yield only at forward angles ( $\cos \Theta_{pq} > 0.6$ )
- This can be ignored

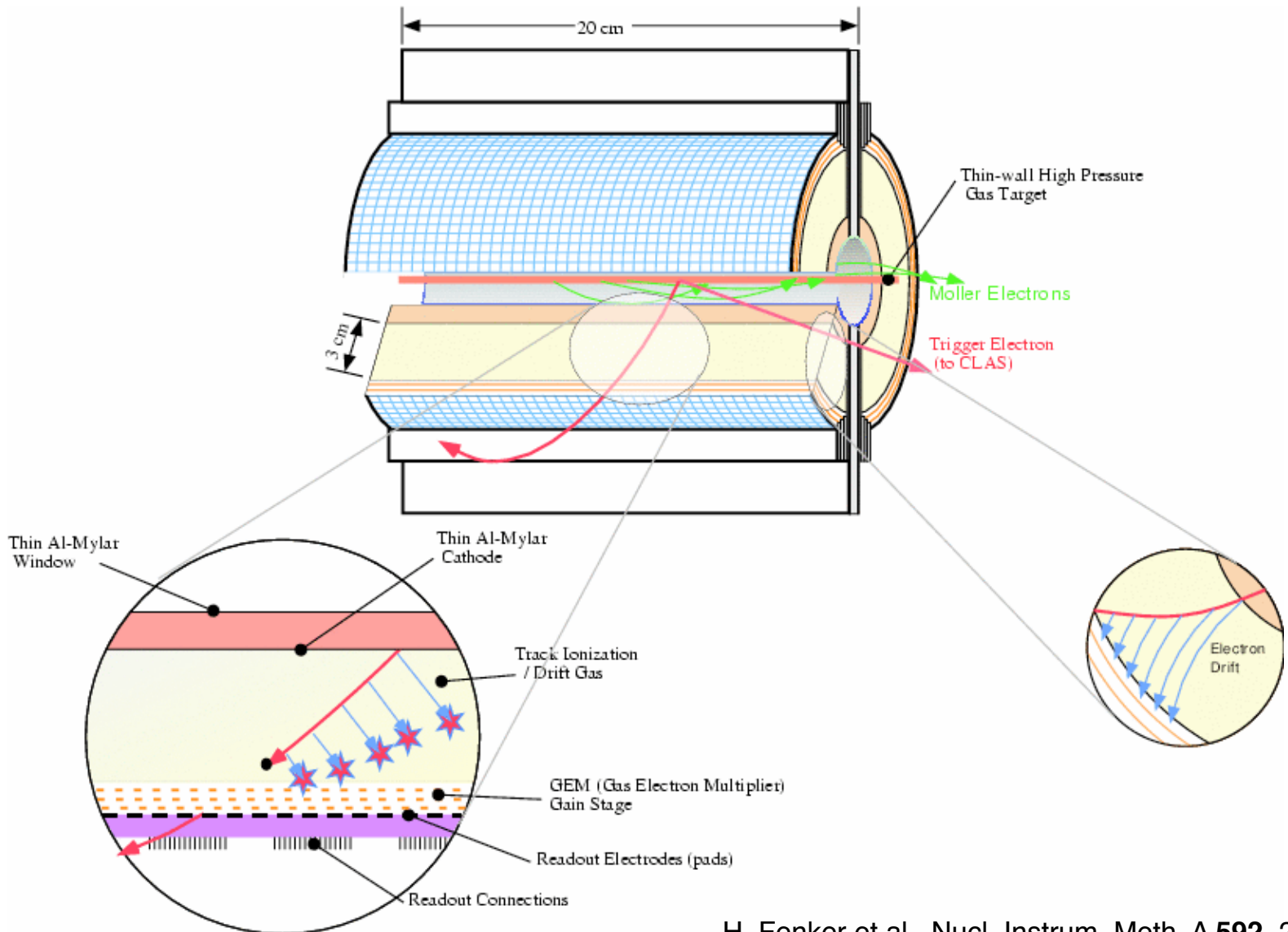




- Bound Nucleon Structure Experiment
- Hall B, JLab, CLAS
- $d(e, e'p_s)X$  with  $70 < p_s < 150$  MeV/c
- $E_{\text{beam}} = 1.1, 2.1, 4.2, 5.3$  GeV
- Radial time projection chamber for  $p_s$
- Data taking in 2005



# BoNuS Detector

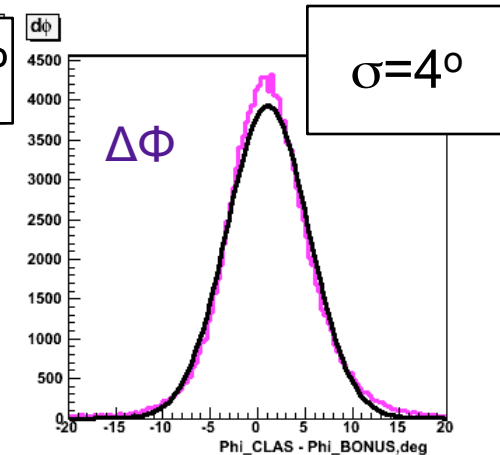
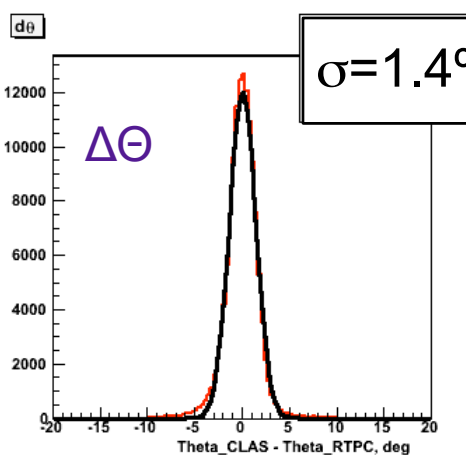
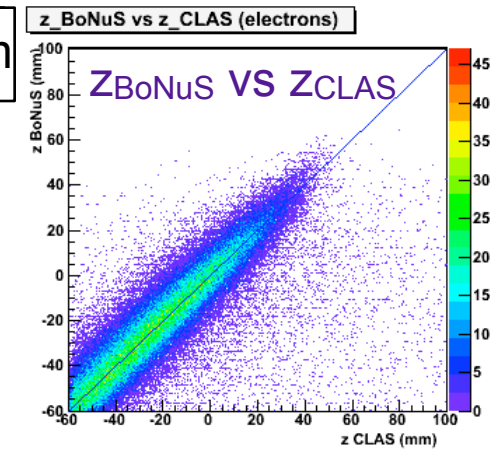
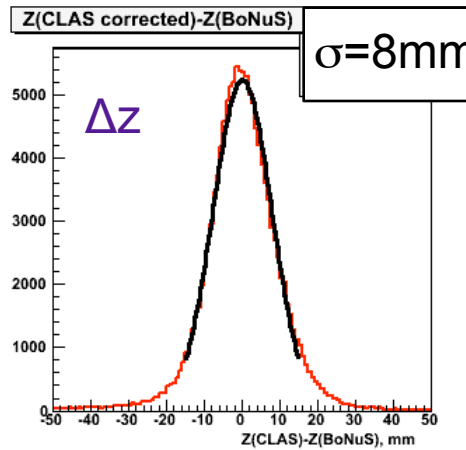
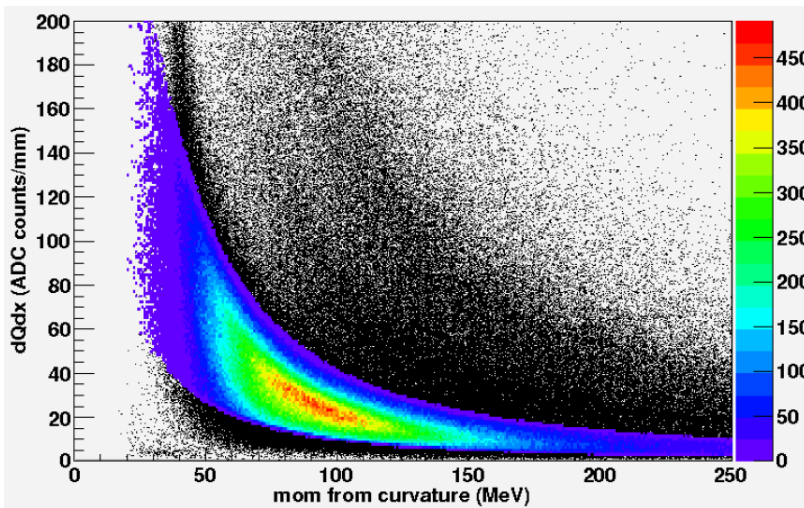
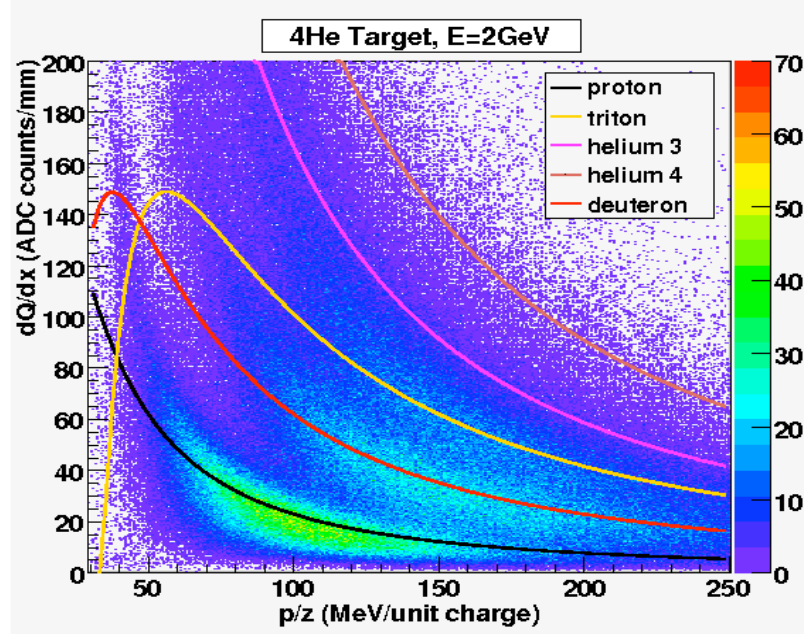


H. Fenker et al., Nucl. Instrum. Meth. A **592**, 273 (2008)



# BoNuS RTPC Performance

- Upper left:  $dE/dx$  vs.  $p/Z$  for He target
- Lower left:  $dE/dx$  vs.  $p$  for deuterium target
- Below RTPC+CLAS resolution for common  $e^-$  events



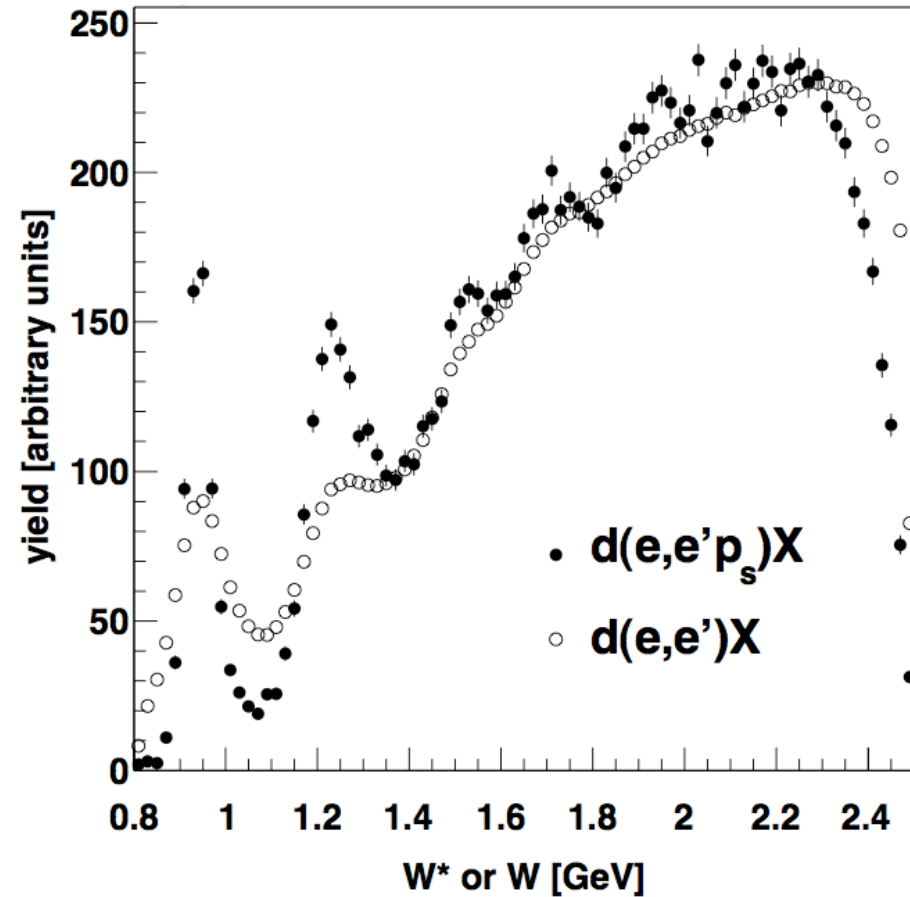
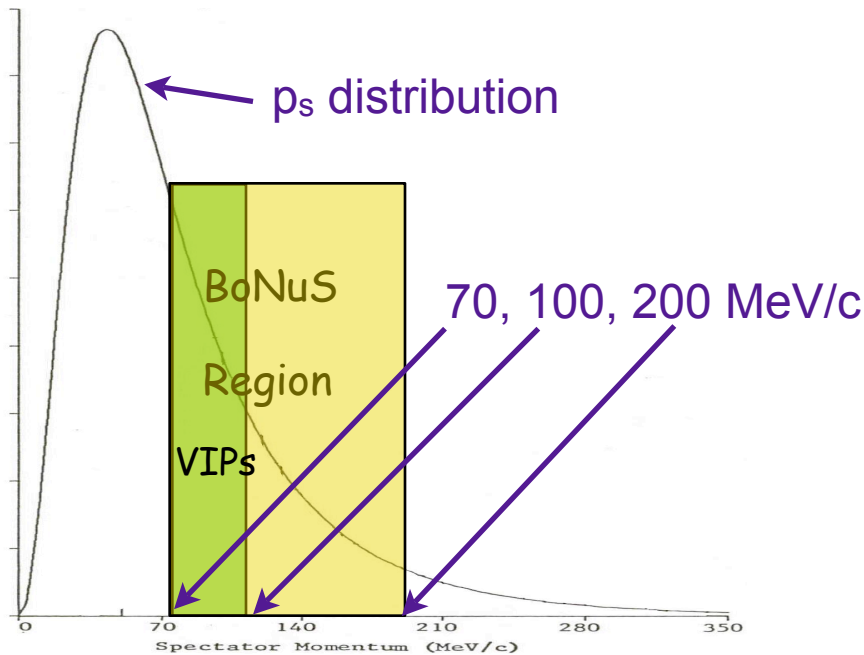


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# BoNuS Kinematic Correction

- Very Important Protons  $70 < p_s < 100$  MeV/c
- VIPs are 17% of the  $p_s$  distribution
- Corrections make resonances stand out
- $F_2^n/F_2^p$  can be measured at high  $x^*$





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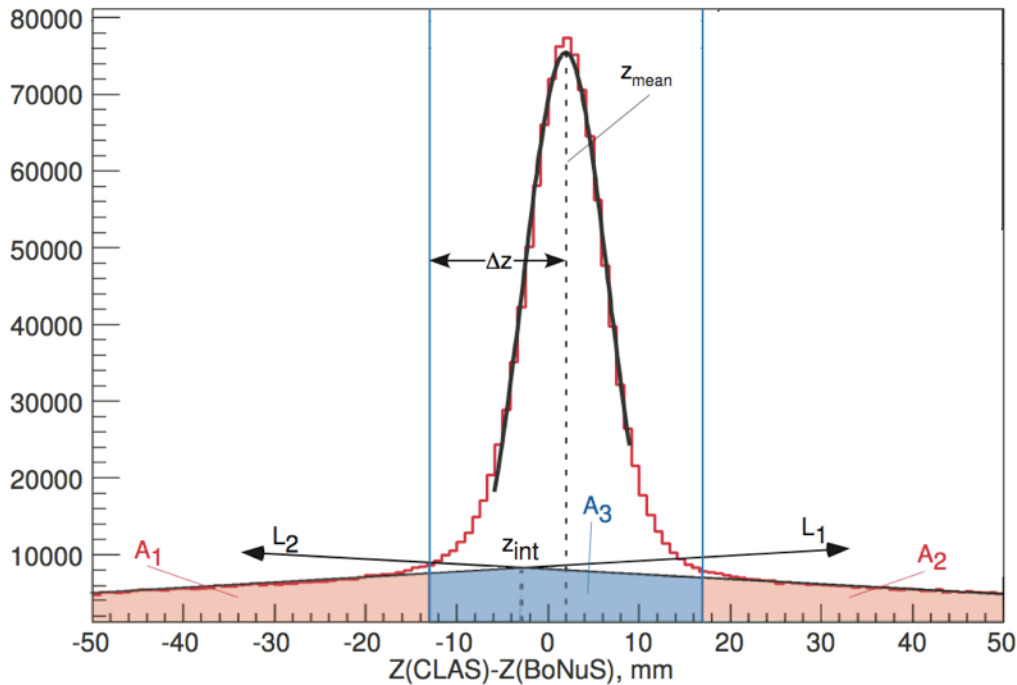
# Two Analysis Methods

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- The Ratio Method
  - ★ measure tagged counts divided by inclusive counts
  - ★ correct this ratio for backgrounds
  - ★ one scale factor gives  $F_2^n/F_2^d$
- The Monte Carlo Method
  - ★ measure tagged counts
  - ★ divide by spectator model Monte Carlo results
  - ★ multiply by  $F_2^n$  used in the model
- The two methods have different systematic errors, but give very similar results.



# Accidental Backgrounds



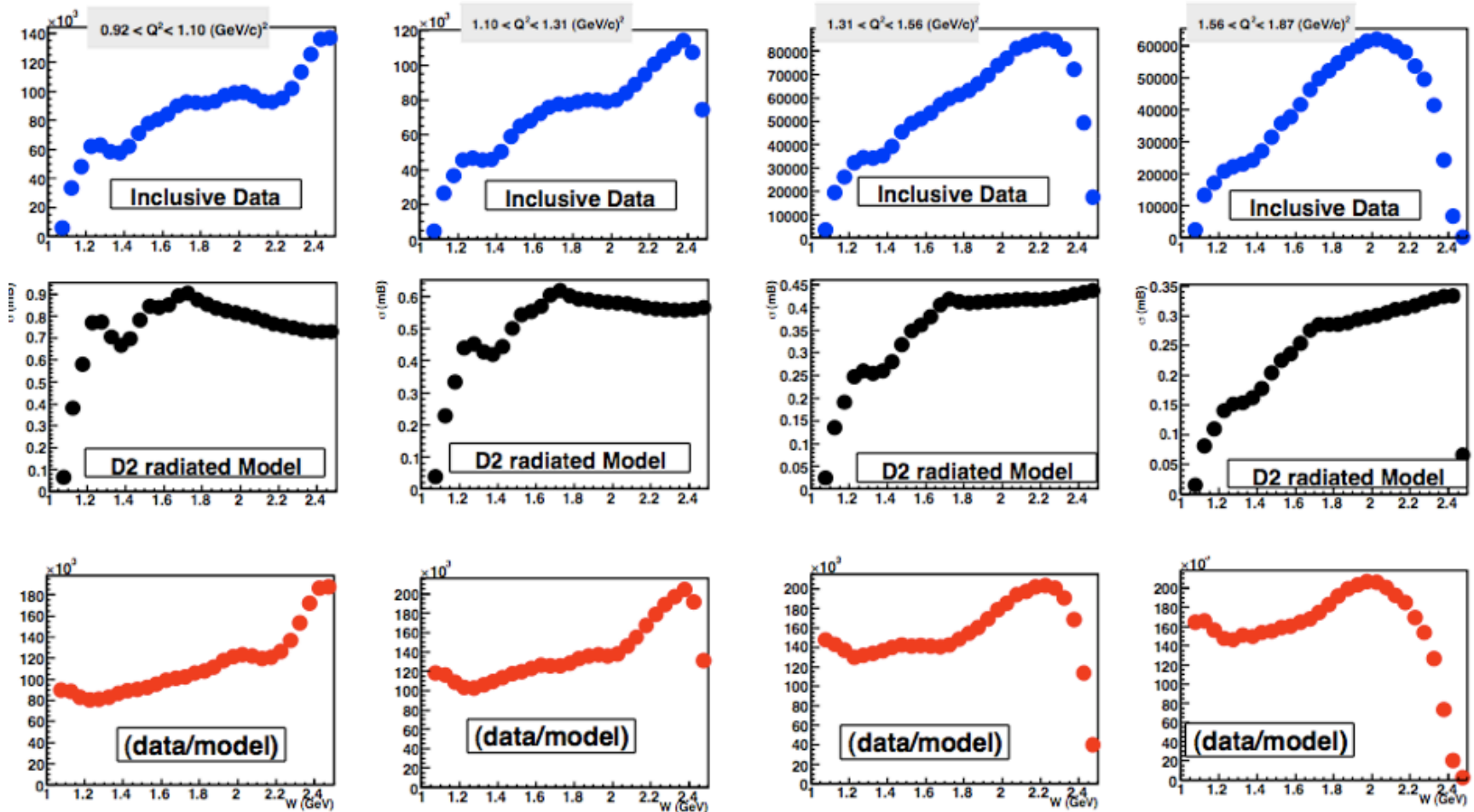
- $Z$  is the position along the beam direction
- Tracking of the electron gives  $Z(\text{CLAS})$
- Tracking of the spectator proton gives  $Z(\text{BoNuS})$
- $\Delta Z = Z(\text{CLAS}) - Z(\text{BoNuS})$  shows a coincidence peak and a triangular background
- Fits to the triangular background allows us to measure backgrounds underneath the peak
- Blue area =  $R_{bg}$  x Pink area
- $R_{bg}$  is independent of kinematics



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# CLAS Detection Efficiency



- Top Row: Raw inclusive  $ed$  scattering in CLAS [vs.  $W$ , 4 plots in  $Q^2$ ]
- Middle Row: Inclusive  $ed$  radiated cross sections from world data fit (Bosted)
- Bottom Row: Relative efficiency  $\varepsilon$  (i.e. Top Row / Middle Row)



&amp;



# $F_2^n/F_2^d$ from Tagged/Untagged Events

$$R_{corr} = \frac{\sum_{i=1}^{N_{tag}(W^*, Q^2)} \frac{1}{\epsilon_i(W, Q^2)} - R_{bg} \sum_{j=1}^{N_{bg}(W^*, Q^2)} \frac{1}{\epsilon_j(W, Q^2)}}{\sum_{k=1}^{N_{untag}(W, Q^2)} \frac{1}{\epsilon_k(W, Q^2)}}$$

$$\frac{F_2^n}{F_2^d} = (R_{corr})(C_{e^+})(C_{\pi^-})(r_{rc})(n)$$

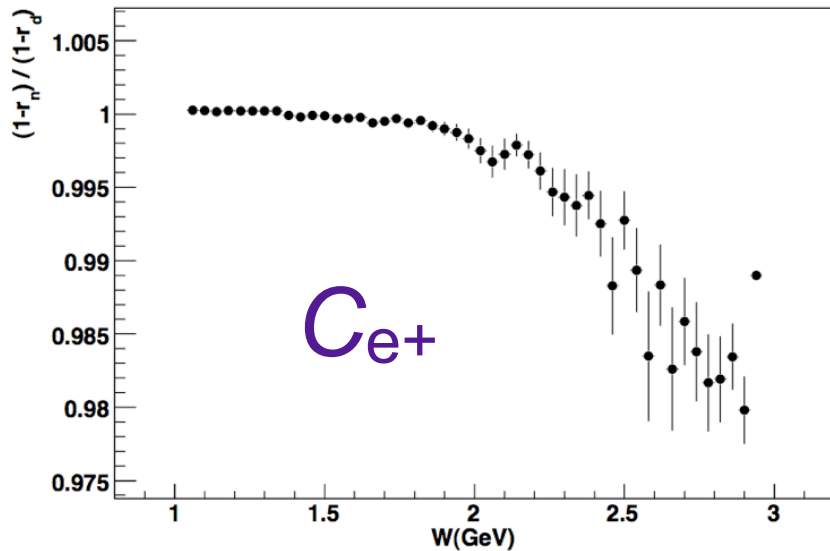
- $R_{corr}$  is the tagged to untagged ratio corrected for CLAS efficiency and accidentals
- $C_{e^+}$  and  $C_{\pi^-}$  are corrections for pair-symmetric and  $\pi^-$  backgrounds
- $r_{rc}$  is the radiative correction
- $n$  is an overall normalization constant that ensures agreement with world data at  $x=0.3$



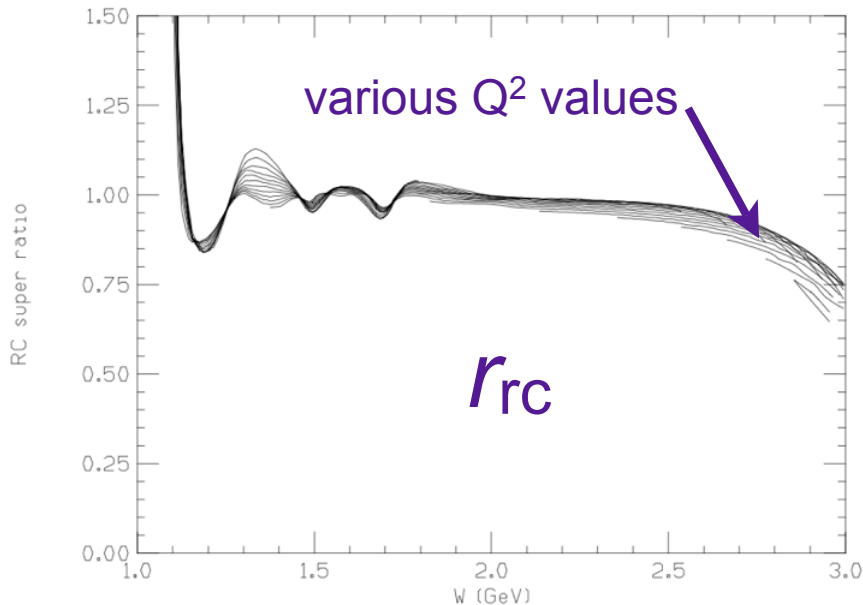
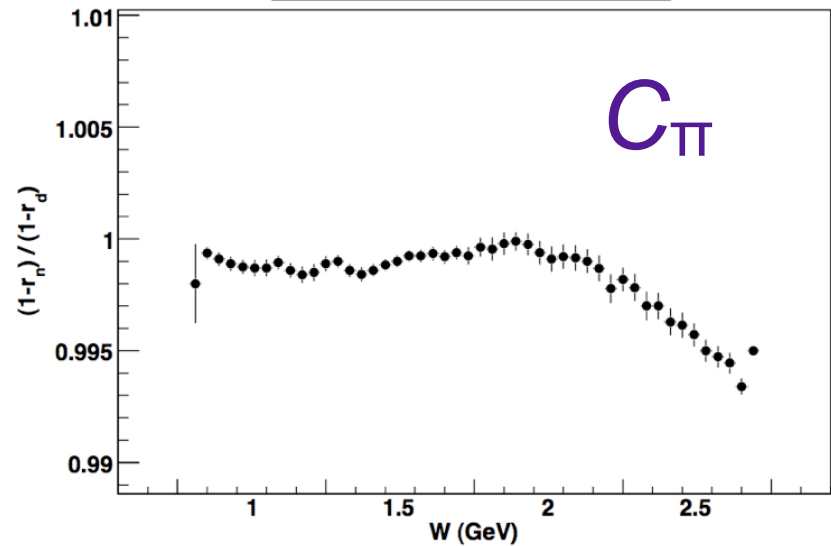


# Corrections $C_{e^+}$ , $C_{p^-}$ , and $r_{rc}$

Pair Sym Background Correction



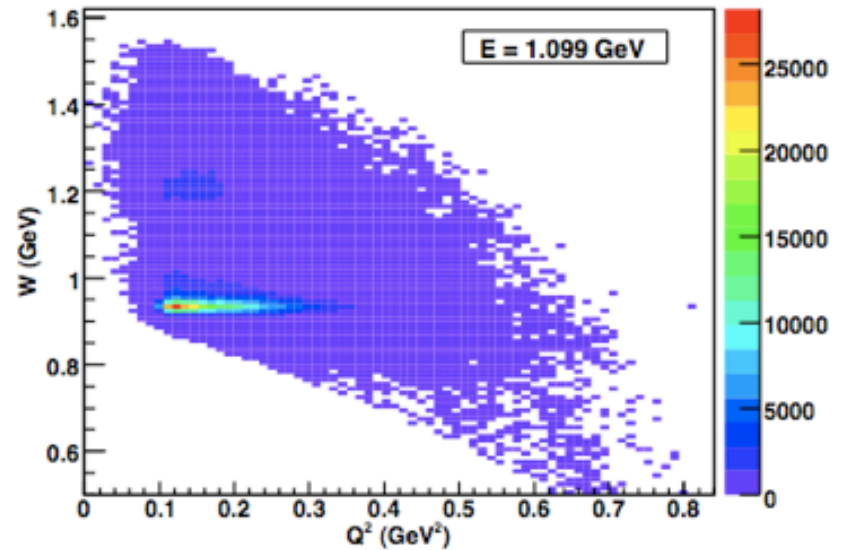
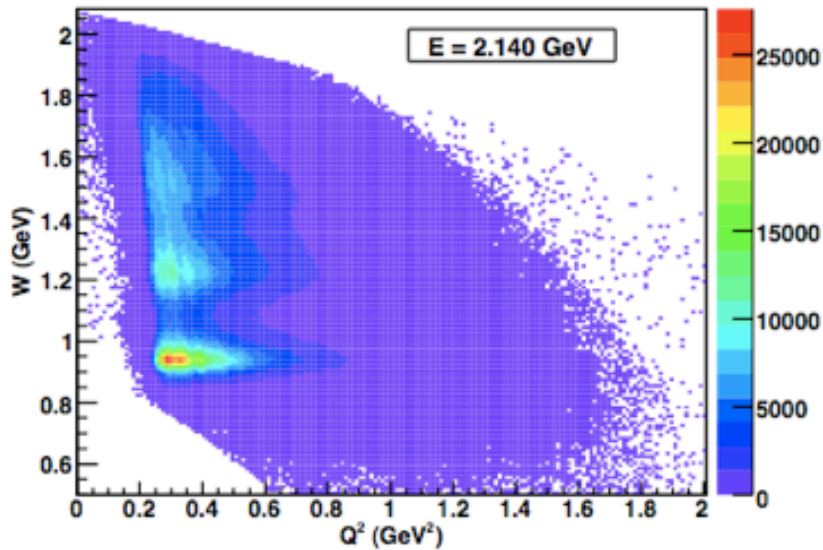
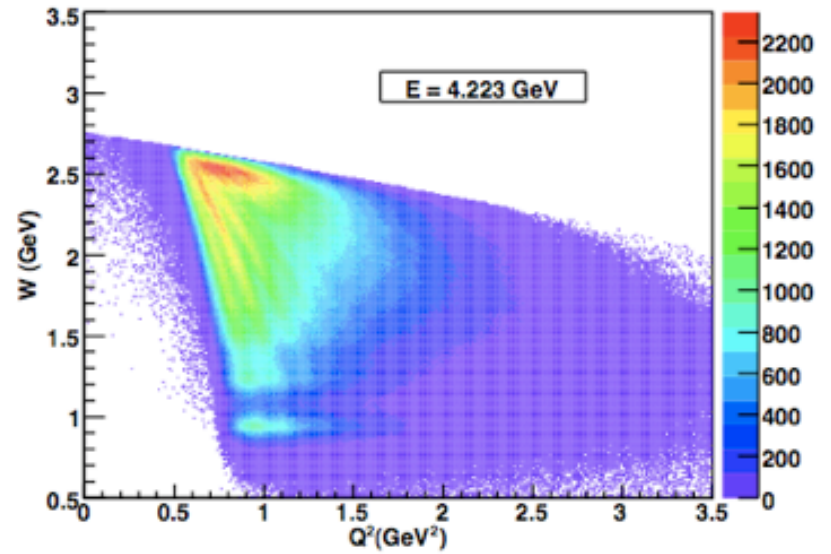
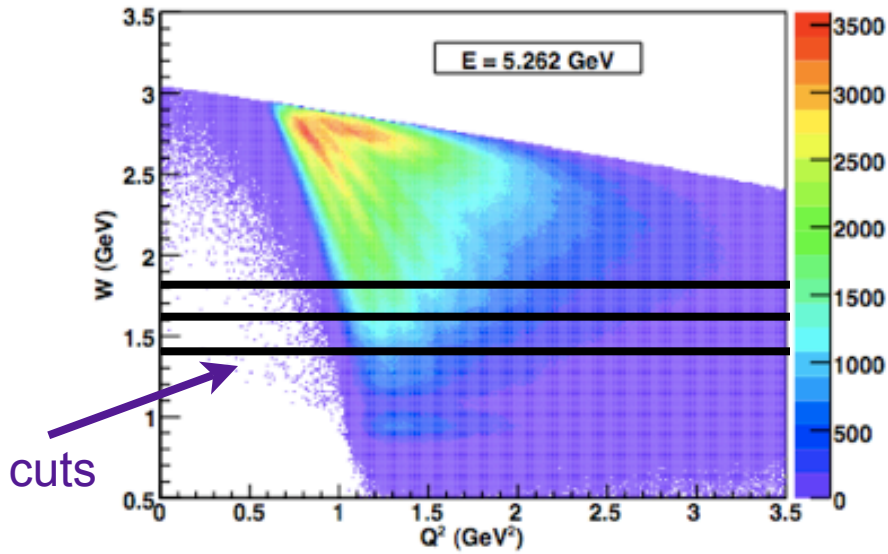
Pion Background Correction



- $C_{e^+}$  correction < 2 %
- $C_{\pi}$  correction < 1/2 %
- $r_{rc}$  correction < 10% in the region  $1.2 < W < 2.7$  GeV
- $1/n = 0.02535 \pm 3.37\%$

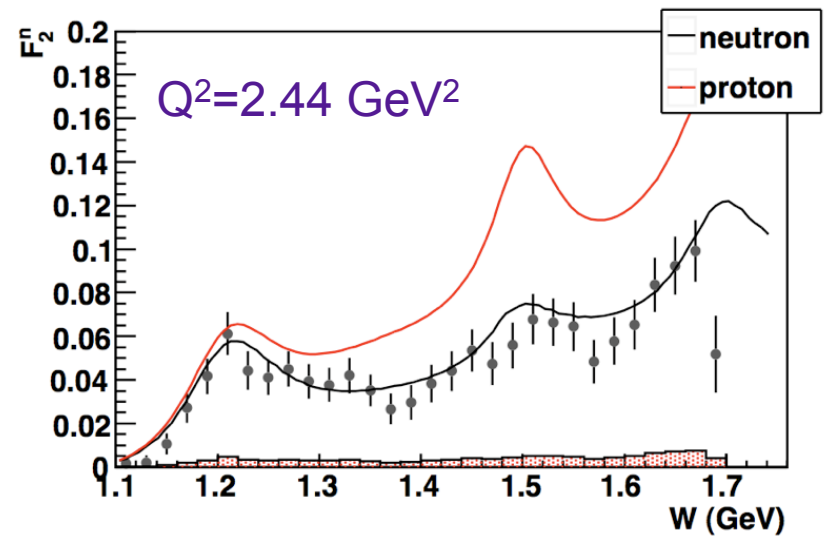
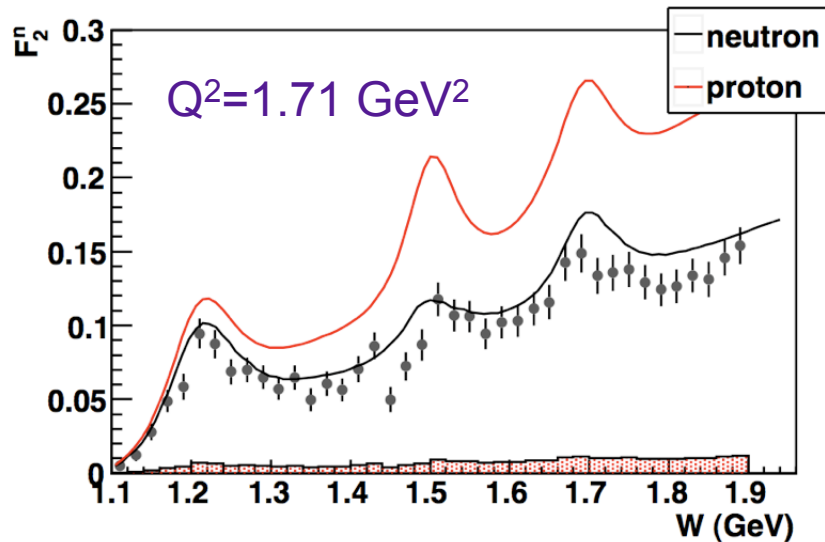
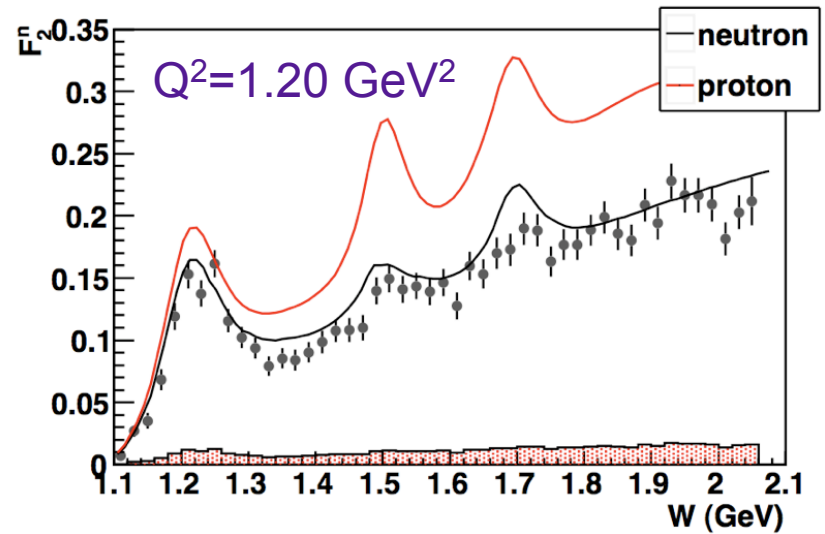
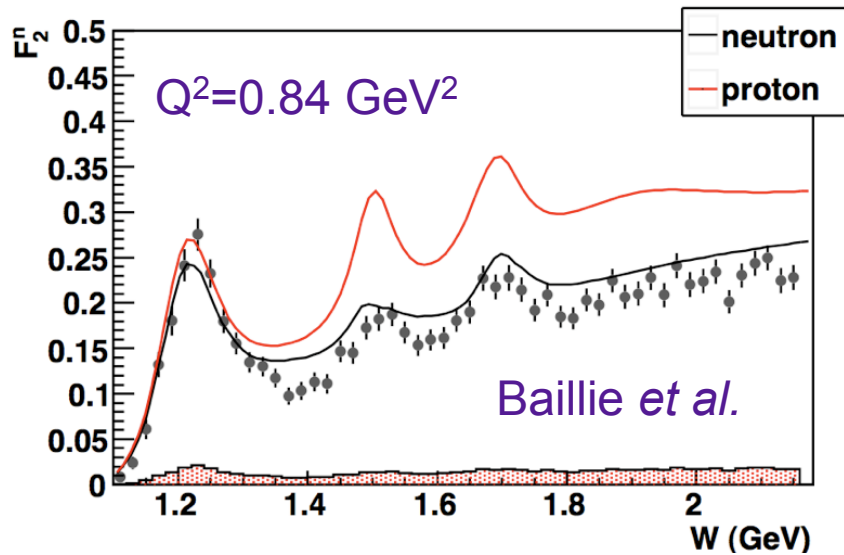


# Kinematic Coverage





# BoNuS $F_2^n$



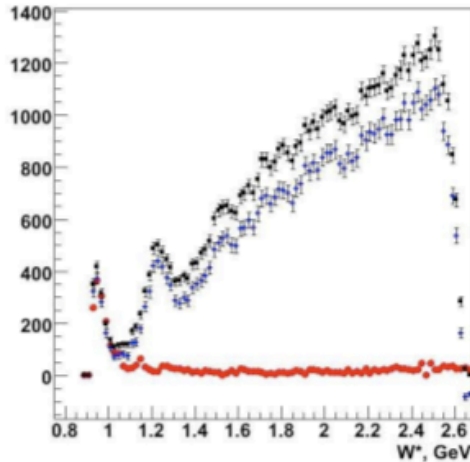
4 of 16 spectra:  $0.8 < Q^2 < 4.5$ ;  $E_{\text{beam}} = 4.2 \text{ \& } 5.3 \text{ GeV}$ ; Bosted/Christy world fits



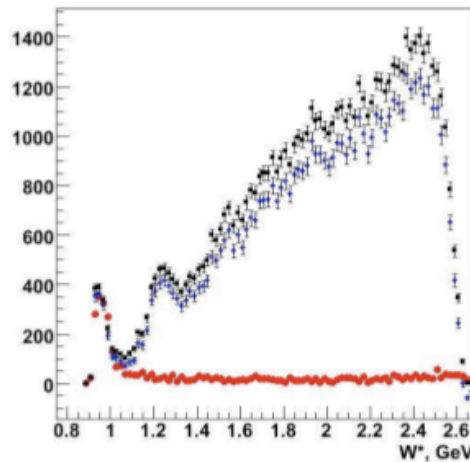
# Monte Carlo Method

$$R(\text{data}/MC) = \frac{F_{2n}^{eff}(W^*, Q^2, \vec{p}_s)}{F_{2n}^{model}(W, Q^2)}$$

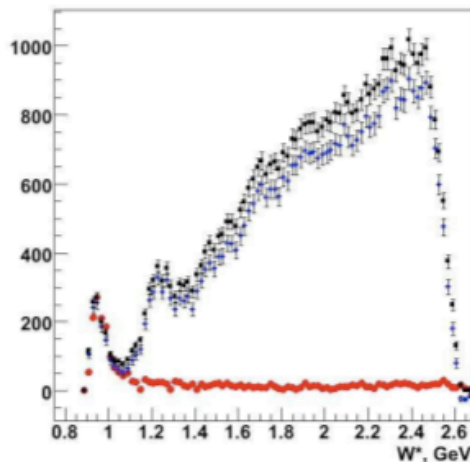
Q2 1.66, cos -0.60, p\_s from 0.070 to 0.085



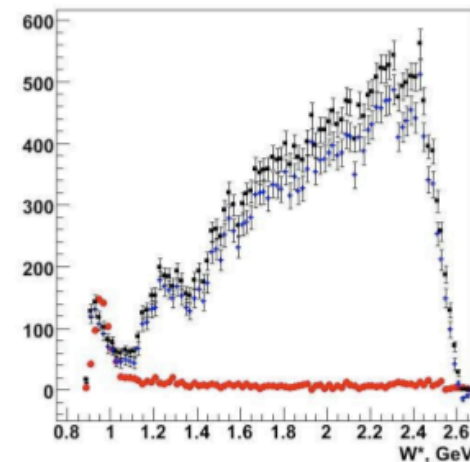
Q2 1.66, cos -0.60, p\_s from 0.085 to 0.100



Q2 1.66, cos -0.60, p\_s from 0.100 to 0.120



Q2 1.66, cos -0.60, p\_s from 0.120 to 0.150



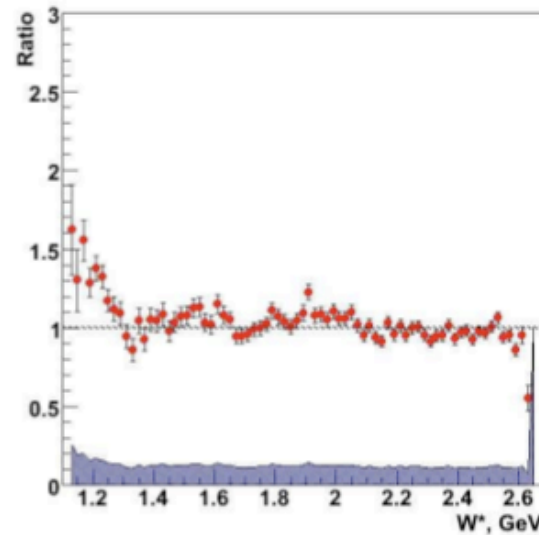
Left: Black=raw tagged data; blue=accidental subtracted data; red=elastic and radiative tail

Tkachenko *et al.*

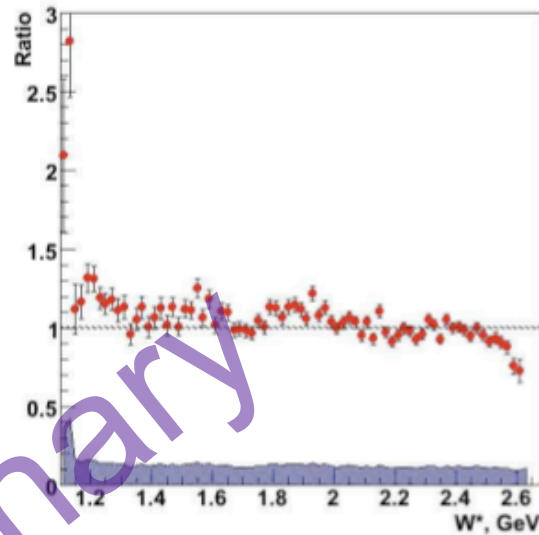


# Data / MC vs $W^*$ for Different $p_s$

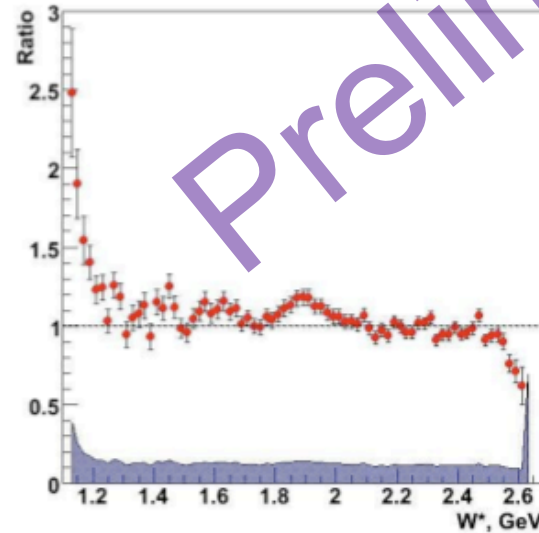
Q2 1.66,cos -0.60, $p_s$  from 0.070 to 0.085



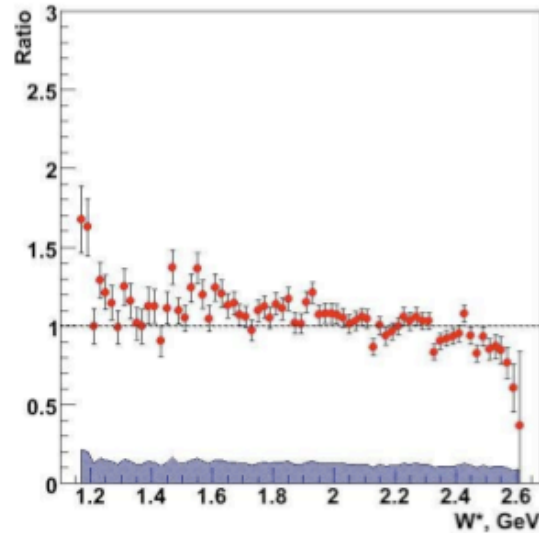
Q2 1.66,cos -0.60, $p_s$  from 0.085 to 0.100



Q2 1.66,cos -0.60, $p_s$  from 0.100 to 0.120



Q2 1.66,cos -0.60, $p_s$  from 0.120 to 0.150



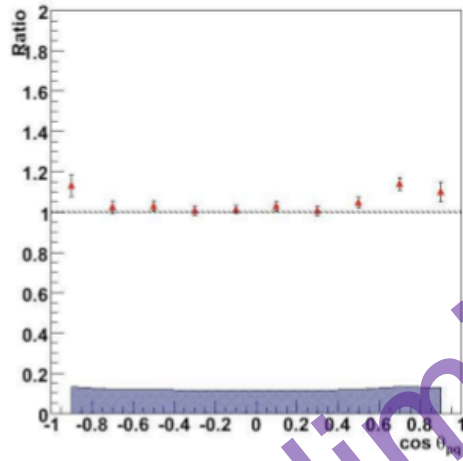
- Deviations from unity at low  $W^*$  comes from difficulties of getting the model right for the resonances
- Generally the ratio is close to unity
- Perhaps some effects at high  $p_s$

Tkachenko *et al.*

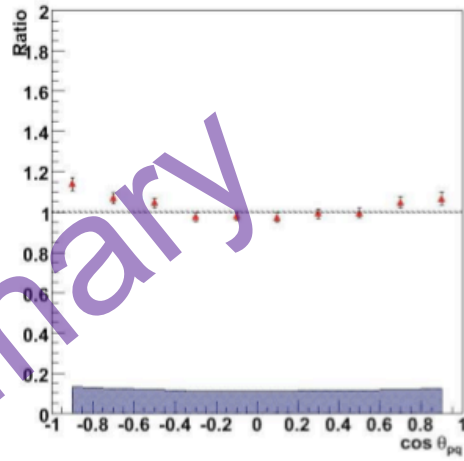


# $\cos\theta$ distributions / MC

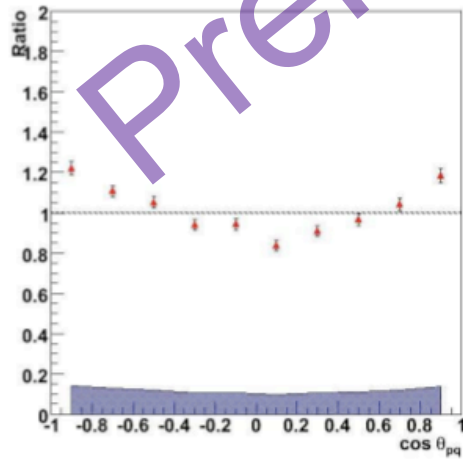
Q2 1.66,  $W^*$  1.73,  $p_s$  0.078



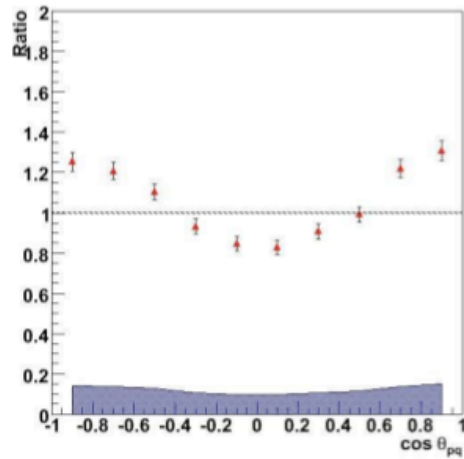
Q2 1.66,  $W^*$  1.73,  $p_s$  0.093



Q2 1.66,  $W^*$  1.73,  $p_s$  0.110



Q2 1.66,  $W^*$  1.73,  $p_s$  0.135



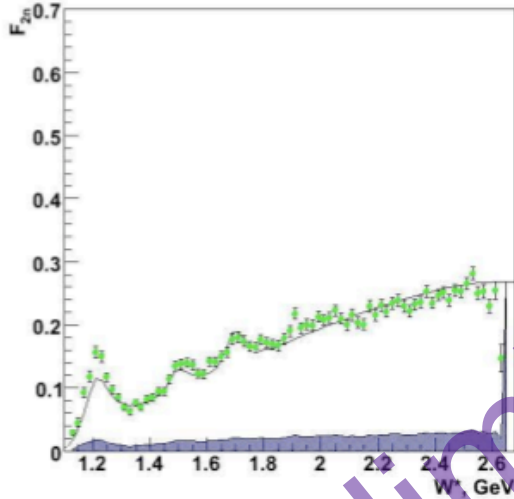
- At low  $p_s$  the data agree with the spectator model quite well
- At higher  $p_s$  the distributions deviate significantly from unity, indicating that VIP particles should have  $p_s < 100$  MeV/c

Tkachenko *et al.*

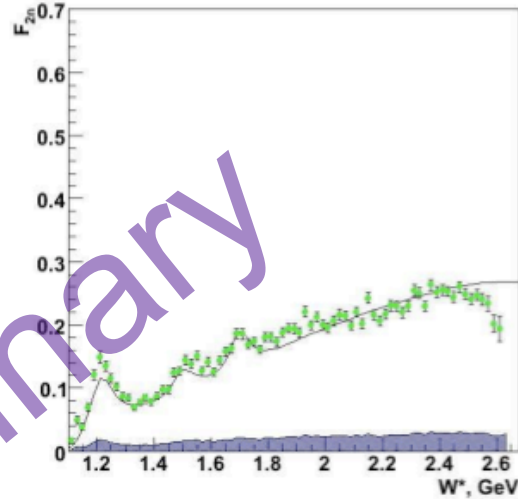


# $F_2^n$ for various $p_s$

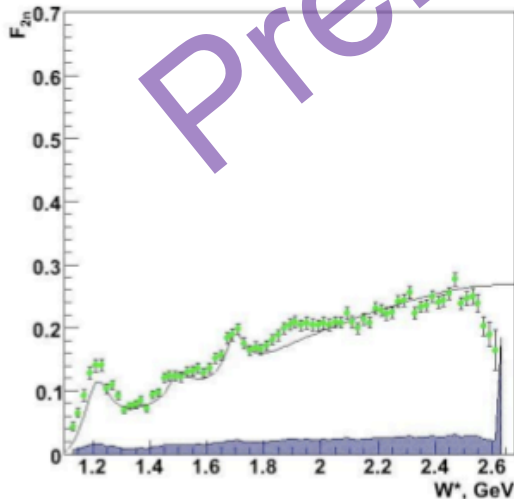
Q2 1.66, cos -0.60,  $p_s$  from 0.070 to 0.085



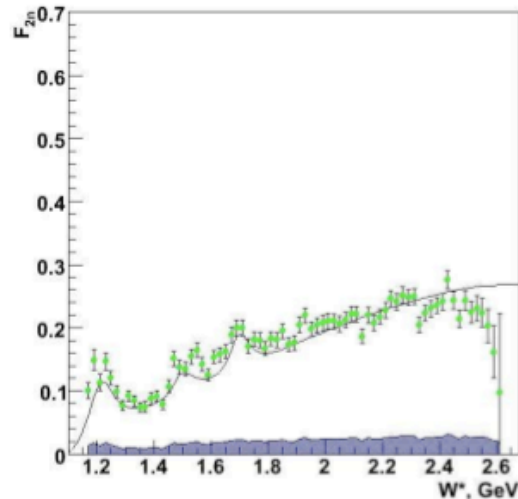
Q2 1.66, cos -0.60,  $p_s$  from 0.085 to 0.100



Q2 1.66, cos -0.60,  $p_s$  from 0.100 to 0.120



Q2 1.66, cos -0.60,  $p_s$  from 0.120 to 0.150

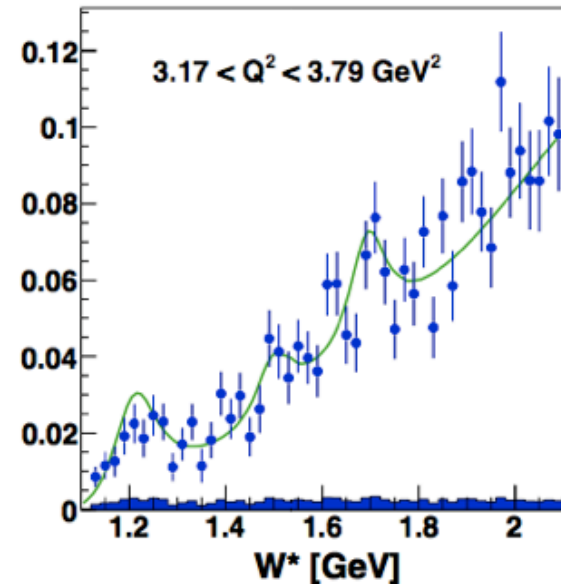
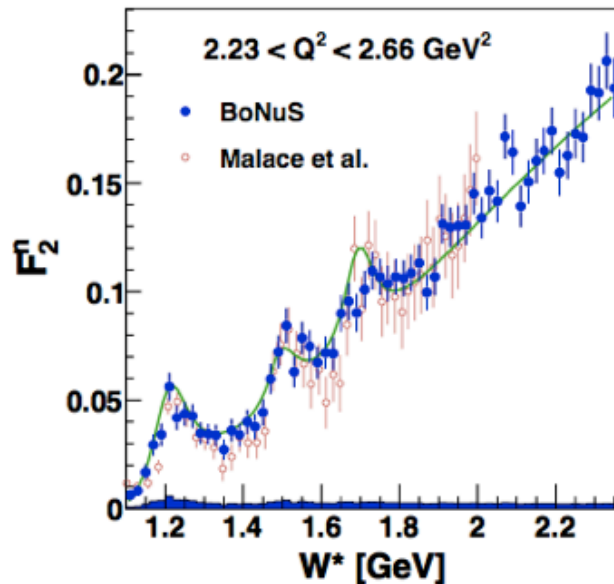
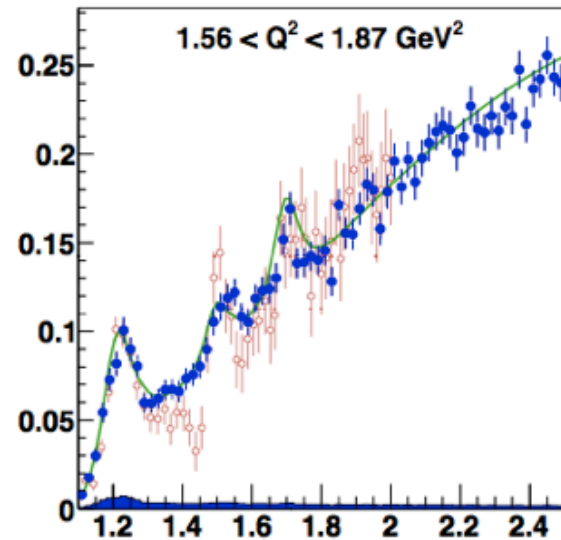
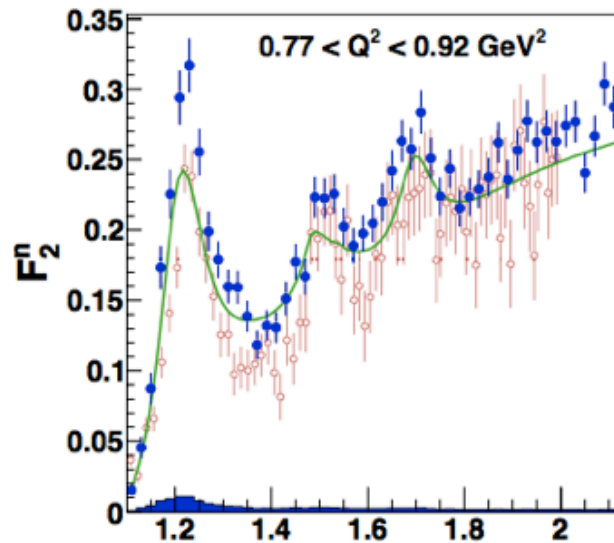


- Data show resonance peaks.
- Data agree quite well with resonance model of world data
- Dependence on spectator momentum is slight

Tkachenko *et al.*



# Final Data



Various data compared to a state of the art nuclear physics extraction of neutron structure functions from deuterium (red points, Malace, et al.)

Baillie *et al.*, PRL **108**(12)142001

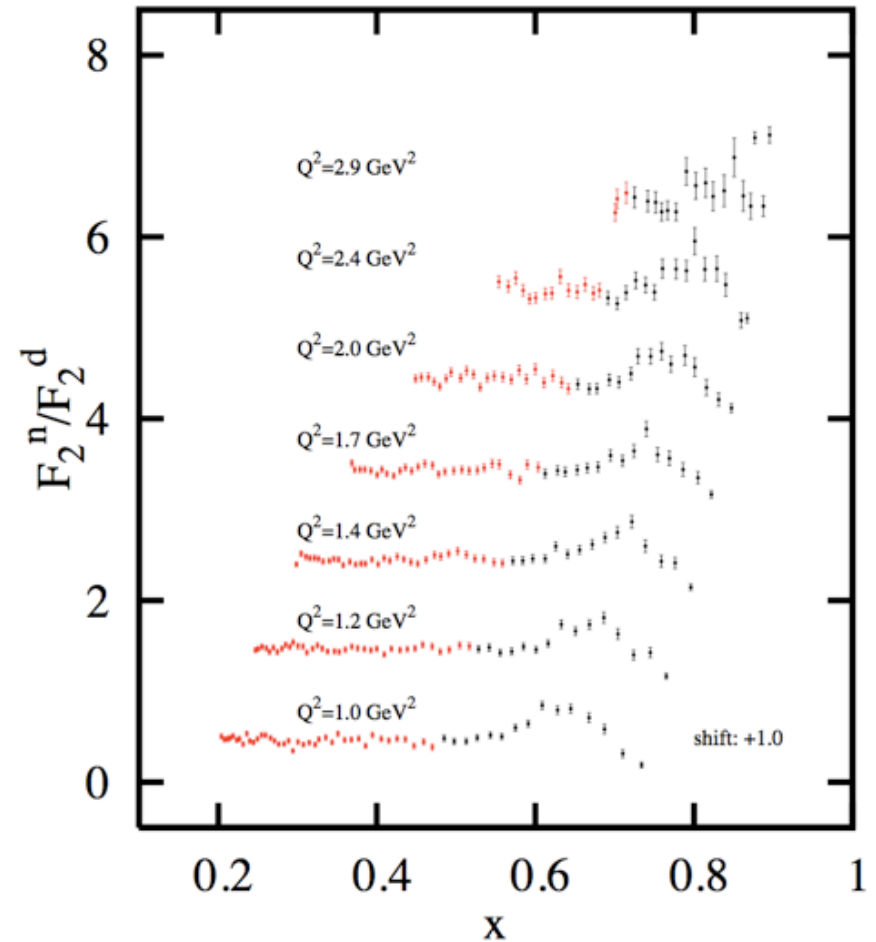
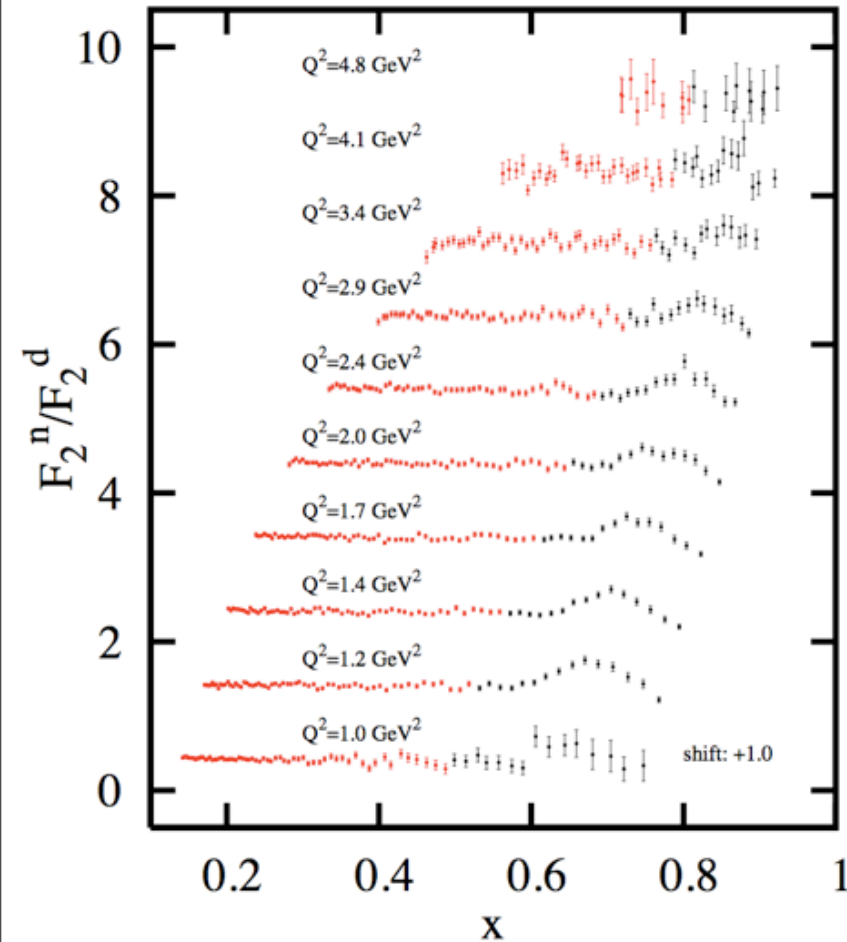




# $F_2^n/F_2^d$

## 5 GeV Data

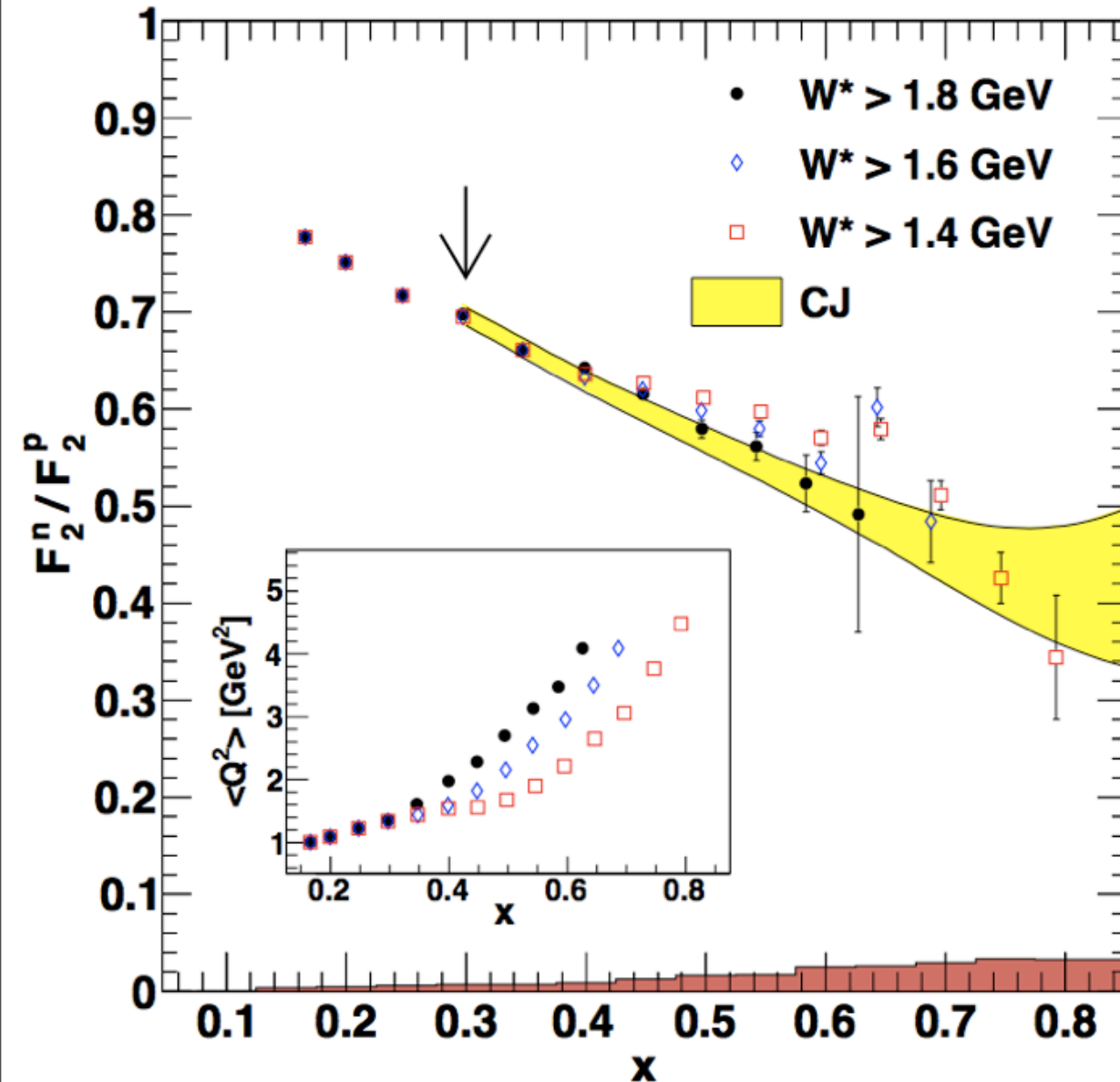
## 4 GeV Data



BoNuS primary results: n/d structure function ratios for  $Q^2 > 1 \text{ GeV}^2$



# BoNuS $F_2^n/F_2^p$



- $F_2^n/F_2^p = (F_2^n/F_2^d)_{\text{exp}}(F_2^d/F_2^p)_{\text{world}}$   
 Bosted/Christy fits:  
 PRC77(08)065206,  
 PRC81(10)055213
- Curves are CJ error bands [Accardi, *et al.*, PRD 84(11)014008]
- CJ cuts off at low  $x$  because  $Q^2$  is too low
- Lower cuts in  $W^*$  yield higher  $x$  values but the inclusion of resonance contributions.
- Results are consistent with CJ trends at high  $x$ .

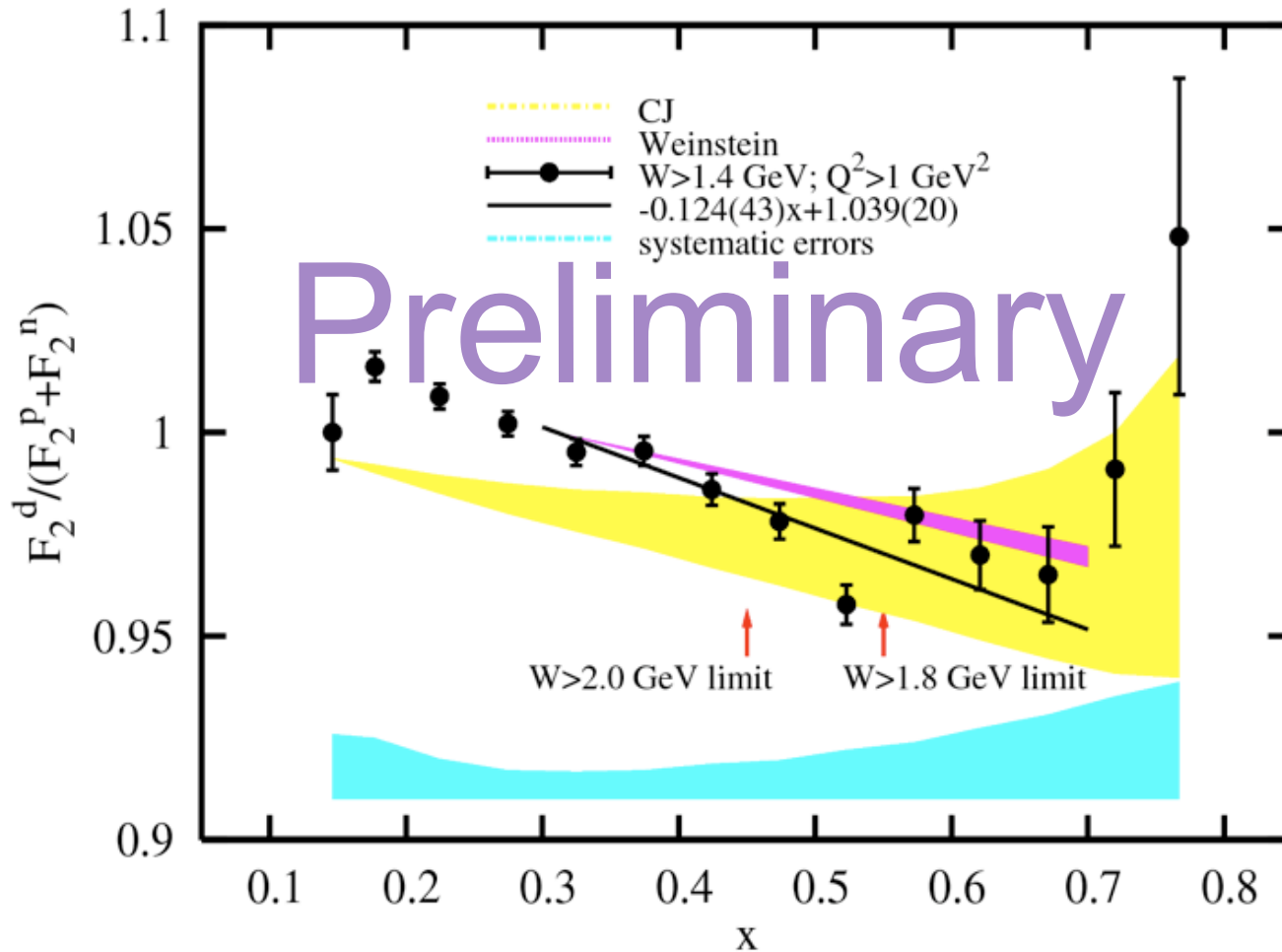
Baillie *et al.*, PRL  
 108(12)142001



# EMC Effect

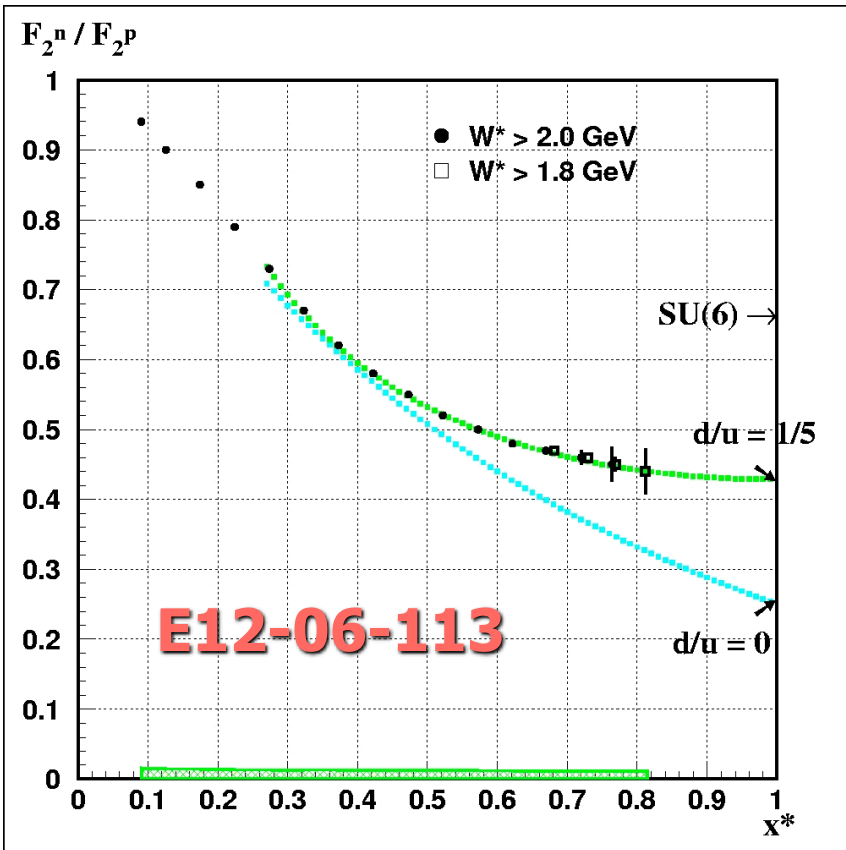
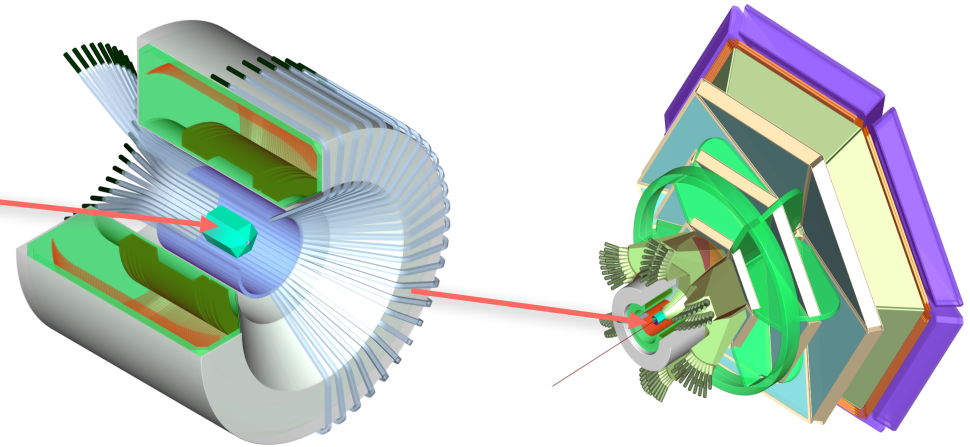
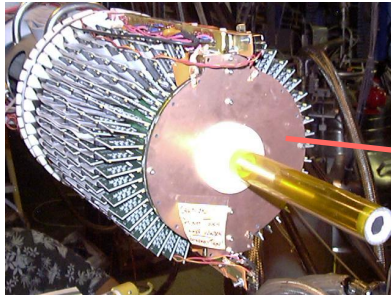
EMC ratio for the deuteron:  $[(F_2^n/F_2^d)_{\text{exp}} + (F_2^p/F_2^d)_{\text{world}}]^{-1}$

Normalization: unity at  $x = 0.31$  (the world EMC average for nuclei)





# BoNuS Plans for 12 GeV



## Data taking:

- 35 days on  $D_2$
- 5 days on  $H_2$
- $\mathcal{L} = 2 \times 10^{34} \text{ cm}^{-2} \text{ sec}^{-1}$

## DIS region:

- $Q^2 > 1 \text{ GeV}^2$
- $W^* > 2 \text{ GeV}$
- $p_s < 100 \text{ MeV}/c$
- $\theta_{pq} > 110^\circ$
- $x^*_{\text{max}} = 0.80$

$W^* > 1.8 \text{ GeV}$ :  $x^*_{\text{max}} = 0.83$



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# Conclusions

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- BoNuS has measured  $F_2^n$  on a “free” neutron target
- Virtually no effects from Fermi motion and final-state interactions
- No evidence for off-shell structure for  $p_s < 100$  MeV/c
- $F_2^n/F_2^p$  behaves at high  $x$  much like CJ high- $x$  fits
- $F_2^n$  resonance data will significantly improve the world’s data set, which up to now came from  $d$  with nuclear corrections
- In the works: a long paper with details of the off-shell study (S. Tkachenko), a paper on  $D(e, e' \pi^- p_s p)$  (J. Zhang), and a paper on the deuteron EMC effect.



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END OF TALK

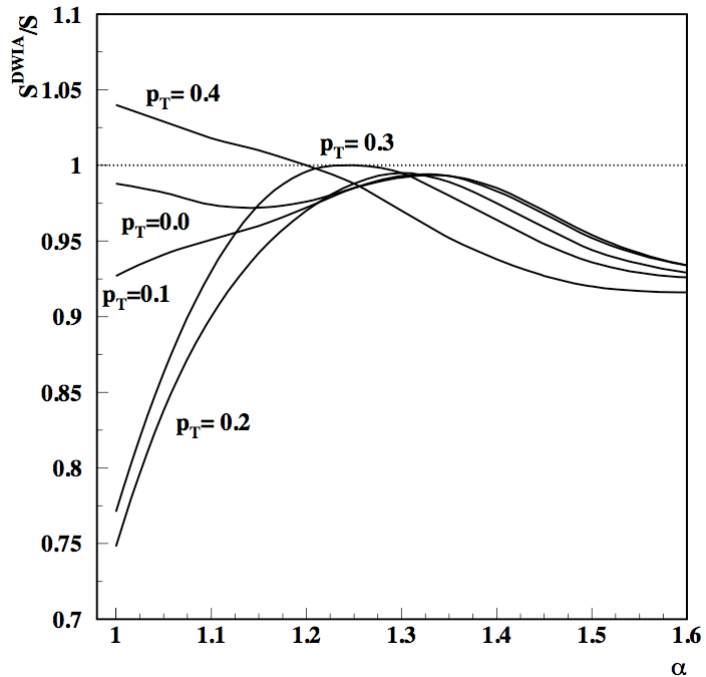
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END

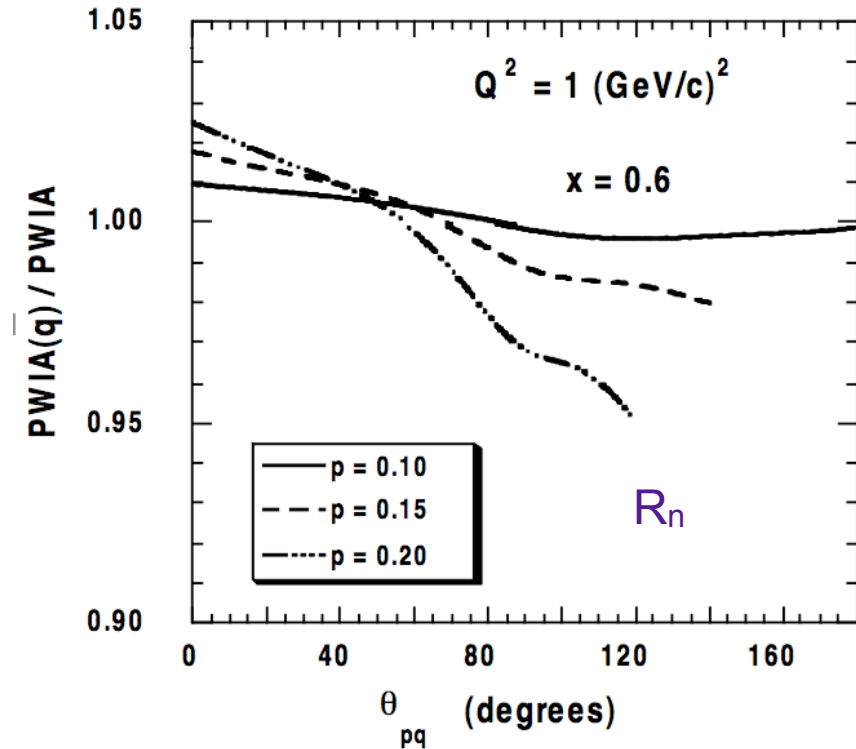


# Spectral Functions

Melnitchouk *et al.*, ZPA359(97)99

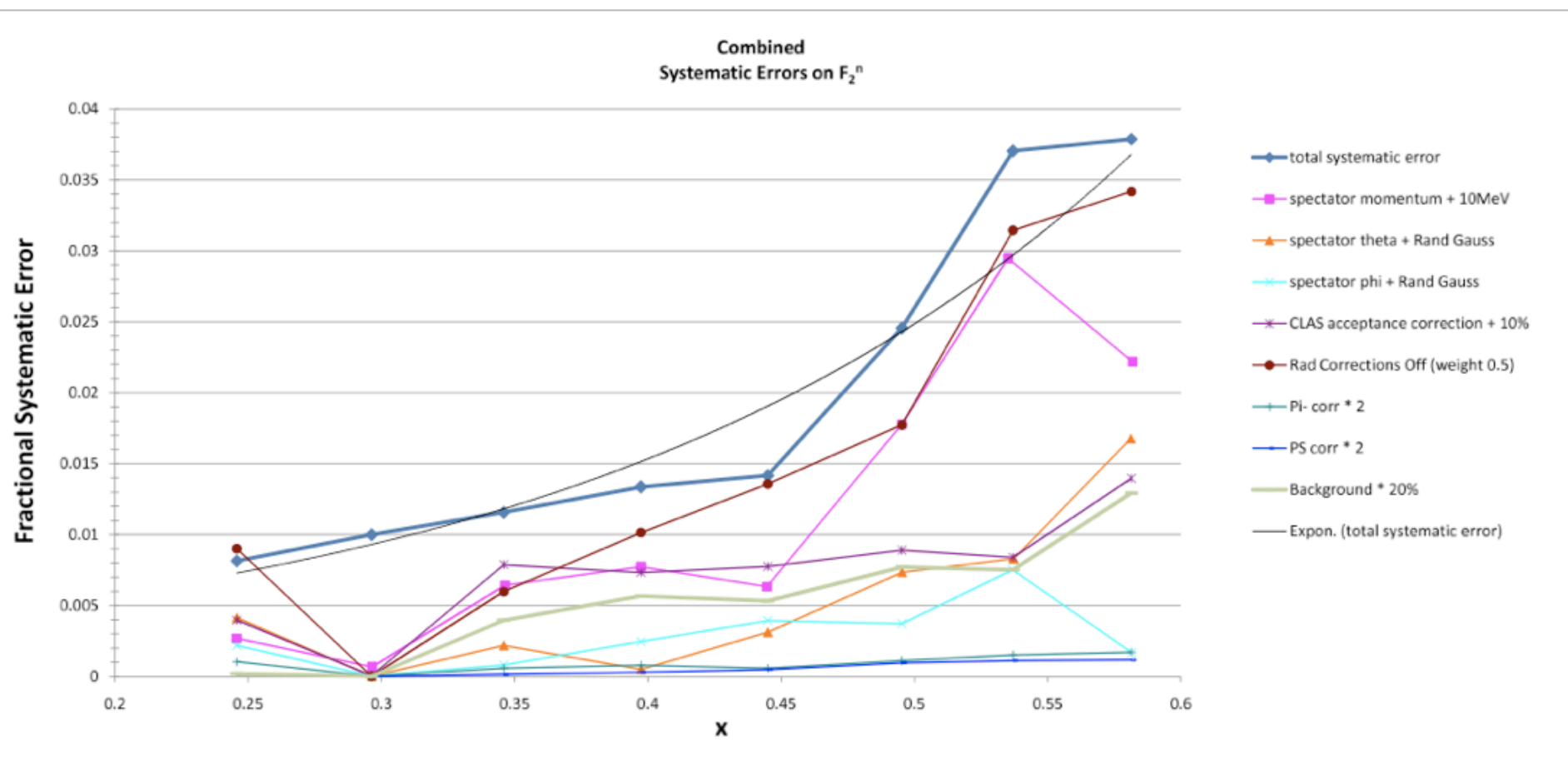


Heller & Thomas, PRC41(90)2756





# Systematic Errors



- Full analysis of  $F_2^n$  is done after shifting or broadening various quantities
- $\Delta F_2^n = 0$  at  $x=0.3$  where normalization takes place (total value there is interpolated)
- Blue line, all changes are made at once; total error rises from 1% to 4% vs  $x$ .





# Ratio and MC Method Comparison

VIP region, F2n

