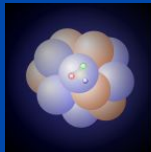


# Neutrino-Nucleus Interactions in Broad-Band Neutrino Experiments

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# Motivation and Contents

- Determination of neutrino oscillation parameters requires neutrino energy
- MiniBooNE QE puzzle, effects on energy reconstruction
- Neutrino interactions in the ‚shallow inelastic regime‘: determination of cross sections



# LBNE



Beam: 700 kW, 60-120 GeV, 5 years  $\nu$  + 5 years anti- $\nu$   
on-axis, wide band, upgradable to 2.3 MW  
Baseline: 1300 km FNAL to Homestake

# Neutrino Oscillations

- 2-Flavor Oscillation:

$$P(\nu_\mu \rightarrow \nu_e) = \sin^2 2\theta \sin^2 \left( \frac{\Delta m^2 L}{4E_\nu} \right)$$

Know:  $L$ , need  $E_\nu$  to determine  $\Delta m^2$ ,  $\theta$

# Neutrino Oscillations

## ■ 3-Flavor Oscillations:

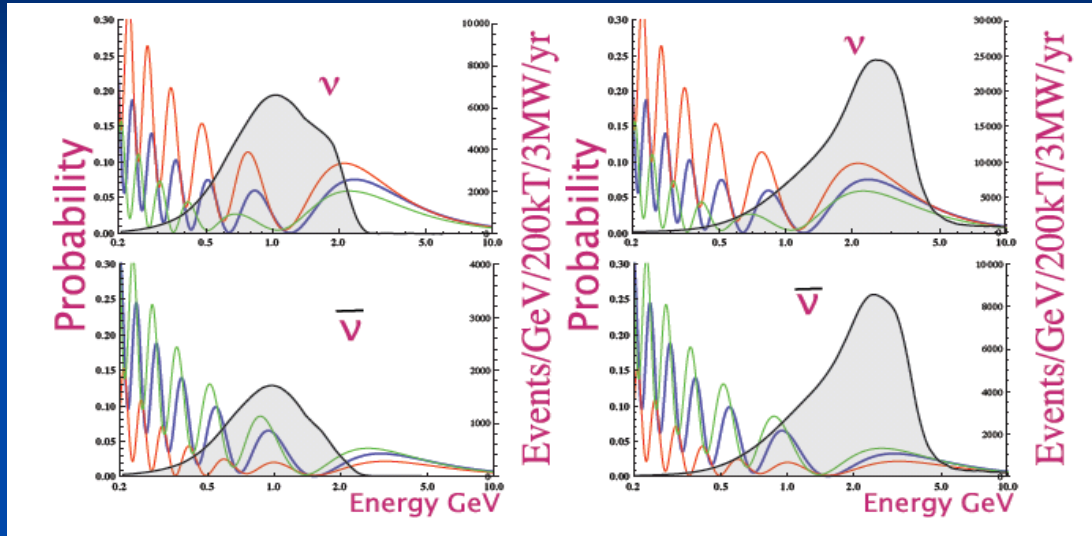
$$\nu_{lL}(x) = \sum_{j=1}^3 U_{lj} \nu_{jL}(x)$$

$$U = \begin{bmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta} & c_{23}c_{13} \end{bmatrix} \\ \times \text{diag}(1, e^{i\frac{\alpha_{21}}{2}}, e^{i\frac{\alpha_{31}}{2}}) .$$

$$c_{ij} = \cos \theta_{ij}, \quad s_{ij} = \sin \theta_{ij} \quad \theta_{ij} = [0, \pi/2]$$

CP violating phases:  $\delta = [0, 2\pi]$      $\alpha_{21}, \alpha_{31}$      $\delta$  goes with  $s_{13}$

# Project X, $\delta_{CP}$ sensitivity



8 GeV

60 GeV

proton energy

From:  
Bishai et al  
arXiv:1203.409

$$\delta_{CP} = 0$$

$$\delta_{CP} = \pi/2$$

$$\delta_{CP} = -\pi/2$$

Need energy to distinguish between different  $\delta_{CP}$



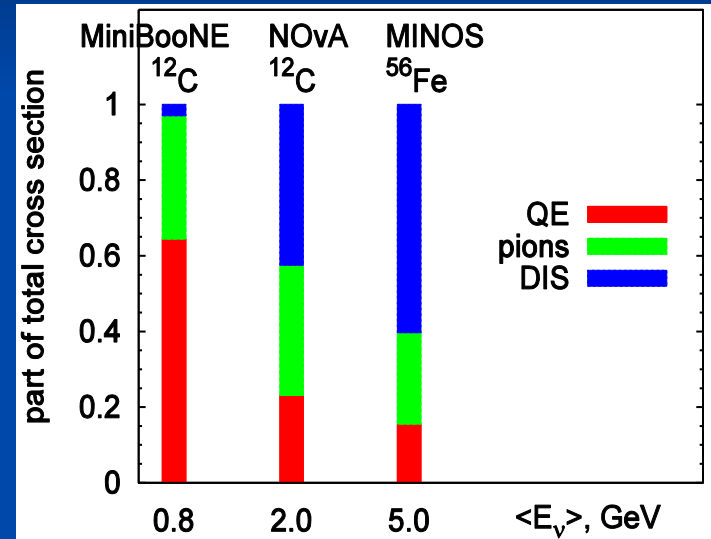
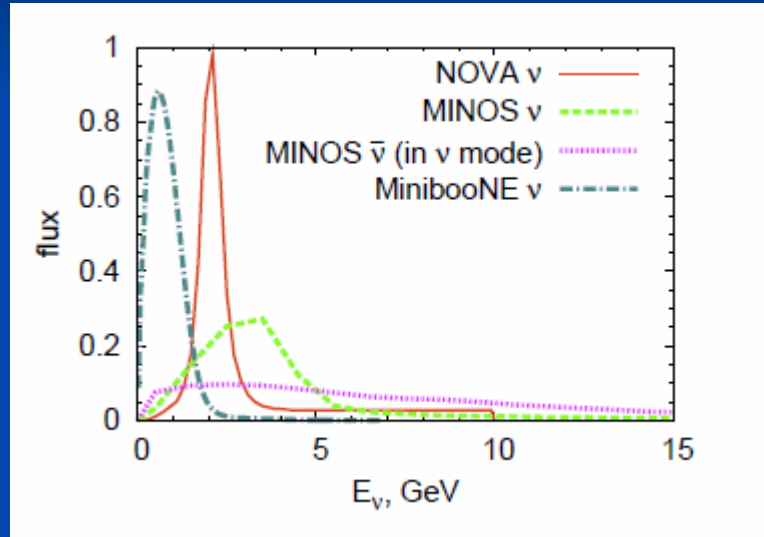
# Now to ongoing experiments





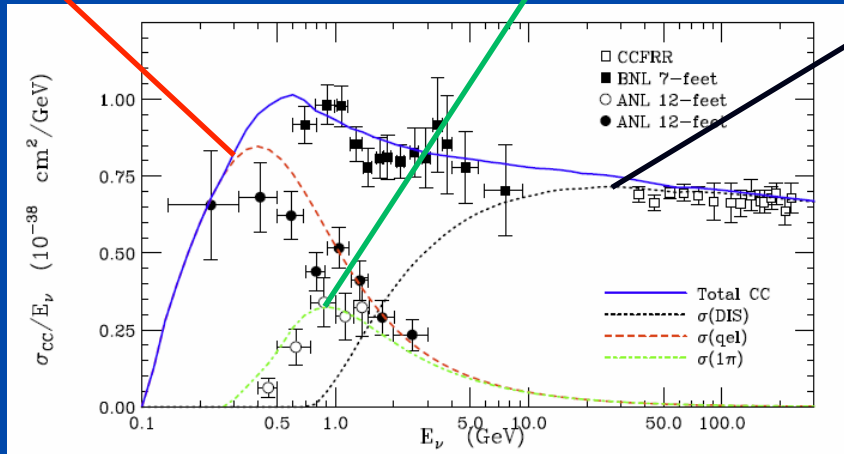
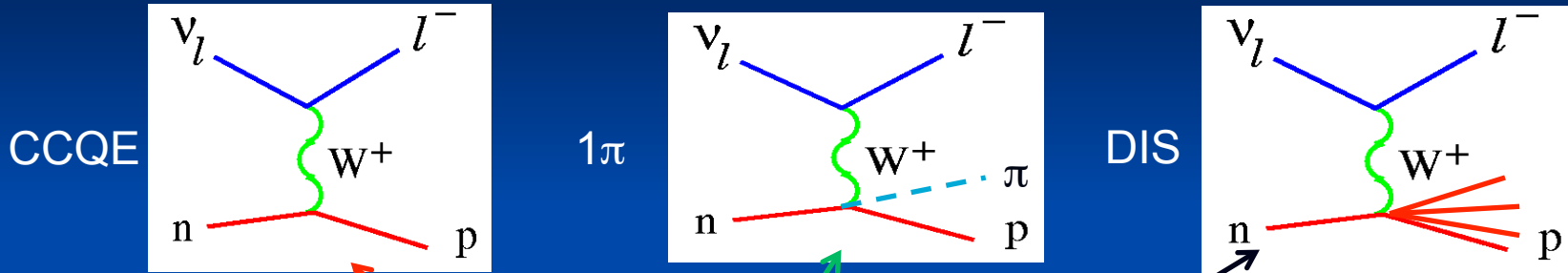
# Neutrino Beams

- Neutrinos do not have fixed energy:



Have to reconstruct energy from final state of reaction

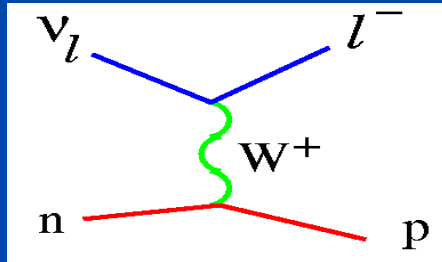
# Neutrino-nucleon cross section



note:  
 $10^{-38}$  cm $^2$  =  $10^{-11}$  mb

# Energy Reconstruction by QE

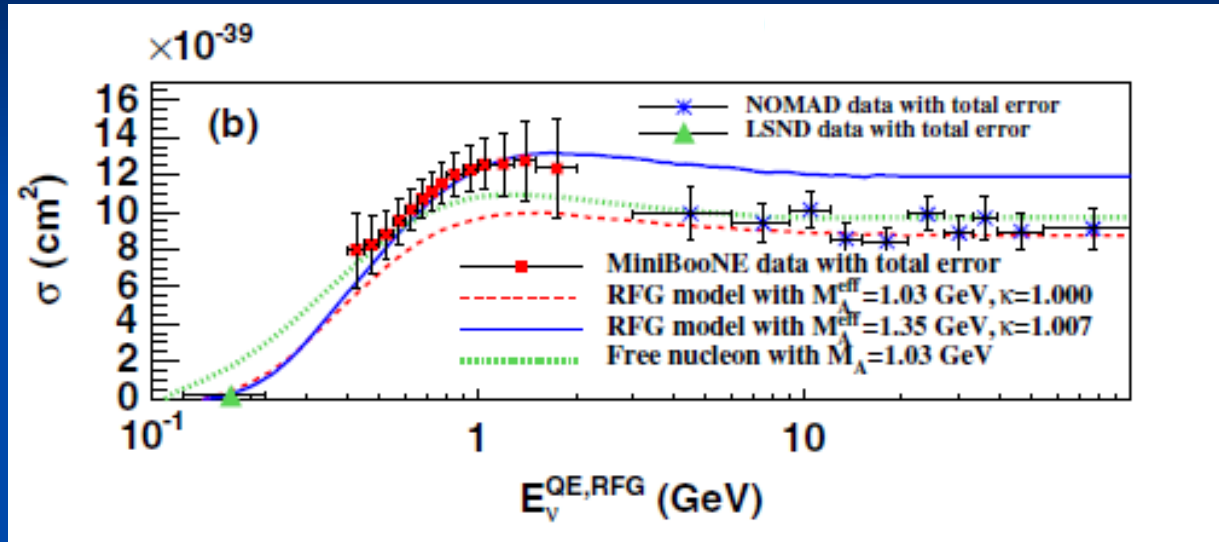
- In pure QE scattering on nucleon at rest outgoing lepton determines neutrino energy!



$$E_\nu = \frac{2(M_N - E_B)E_\mu - (E_B^2 - 2M_N E_B + m_\mu^2)}{2((M_N - E_B) - E_\mu + p_\mu \cos \theta_\mu)}$$

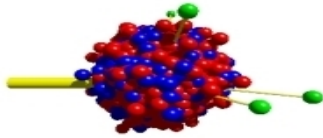
- **BUT:** all modern experiments contain nuclei as targets  $\rightarrow$  expect effects of binding energy and Fermi motion

# MiniBooNE QE puzzle



World average  
axial mass:  
 $M_A = 1.03$  GeV

MB employs Cerenkov counter: identifies QE by muon and zero pion,  
corrects for 'stuck pions'



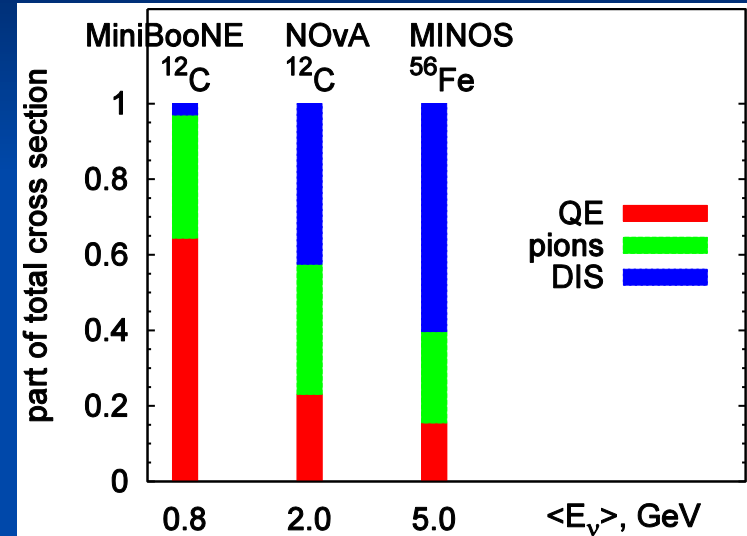
- **GiBUU : Event Generator based on an approx. solution of Kadanoff-Baym equations -> contains off-shell transport**
- general information (and code available): Phys. Rept. 512 (2012) 1 <http://theorie.physik.uni-giessen.de/GiBUU/>
- GiBUU describes (within the same unified theory and code)
  - heavy ion reactions, particle production and flow
  - pion and proton induced reactions
  - low and high energy photon and electron induced reactions
  - neutrino induced reactions

.....using the same physics input! And the same code!



# Model Ingredients

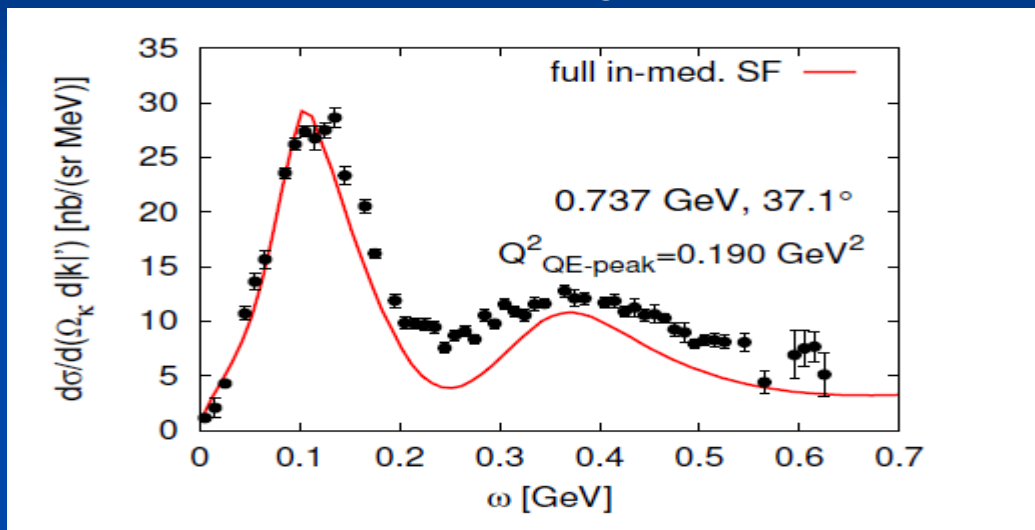
- Processes included:
  - CC + NC QE scattering
  - Resonance excitation
  - DIS
- CC FSI for all produced particles



A complete model has to describe all of them

# Electrons as Benchmark for GiBUU

Electron scattering on C

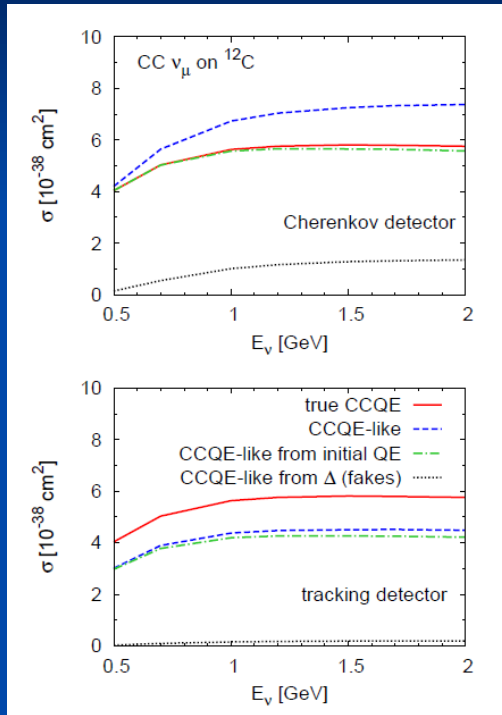


Red curve:  
GiBUU

Res. Props  
from MAID  
UU

Difficulty to separate processes if neutrino energy is not known

# QE-Pion Entanglement



- Cerenkov detector (MiniBooNE, K2K 1kt, T2K) defines QE by:

$$\begin{array}{l} \text{CCQE: } 1\mu^- \ 0\pi^+ \ 0\pi^- \ 0\pi^0 \ xp \ xn \\ \text{CC1}\pi^+: 1\mu^- \ 1\pi^+ \ 0\pi^- \ 0\pi^0 \ xp \ xn \end{array}$$

Too high QE: misidentifies about 20%,  
pion-induced fakes

- Tracking detector (Sci-BooNE, K2K, SciFi, T2K) defines QE by

$$\begin{array}{l} \text{CCQE: } 1\mu^- \ 0\pi^+ \ 0\pi^- \ 0\pi^0 \ 1p \ xn \\ \text{CC1}\pi^+: 1\mu^- \ 1\pi^+ \ 0\pi^- \ 0\pi^0 \ xp \ xn \end{array}$$

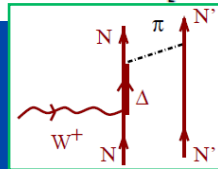
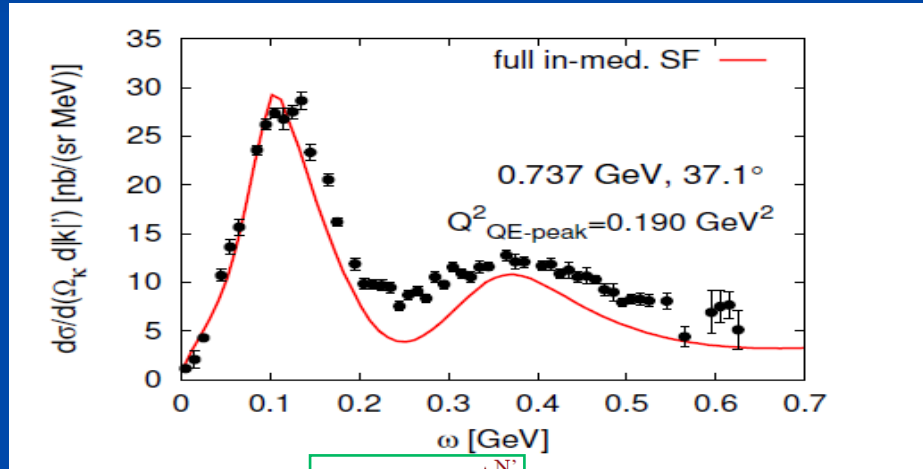
QE identification is clean, but 30% of total  
QE cross section is missed



# The MiniBooNE QE Puzzle

## Explanations

- QE scattering has to be identified for energy reconstruction formula to work.



Difficult to separate QE,  
 $\Delta$  excitation and 2p-2h

# The MiniBooNE QE Puzzle

## Explanations

- Various explanations for MB puzzle:
  - Larger axial mass  $M_A \approx 1.3 \text{ GeV}$  (exp)
  - Change of axial FF (Hill)
  - Change of vector FF (Bodek)
  - 2p-2h (Ericsson, Martini)



# The MiniBooNE QE Puzzle

## Explanations

- A Toy Model for  $\nu + p_1 + p_2 \rightarrow p_3 + p_4 + \mu$  (no recoil)

$$\frac{d^2\sigma}{dE'_l d(\cos\theta')} \propto \frac{k'}{k} \int_{NV} d^3r \int \prod_{j=1}^4 \frac{d^3p_j}{(2\pi)^3 2E_j} f_1 f_2 \overline{|M|^2} (1-f_3)(1-f_4) \delta^4(p)$$

with flux averaged matrixelement

$$\overline{|M|^2} = \int \Phi(E_\nu) L_{\mu\nu} W^{\mu\nu} dE_\nu$$

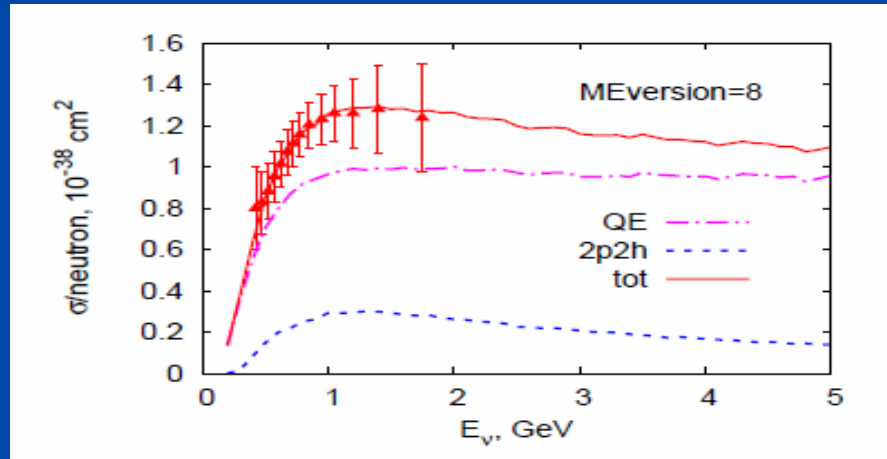
Flux smears out details in  $M$   
 $M$  contains 2p-2h and poss. RPA effects

# The MiniBooNE QE Puzzle

## Explanations

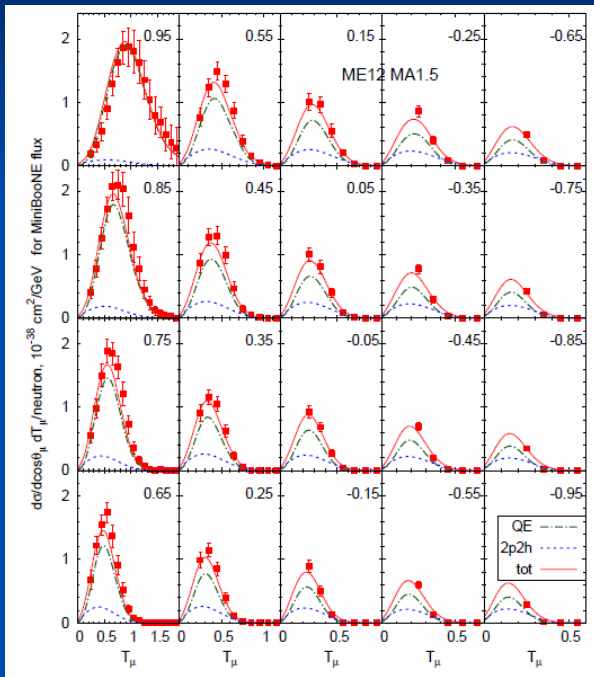
- Educated guess for flux-averaged matrixelement

$$M = M(E, q), w^{\mu\nu} \sim P_T^{\mu\nu}(q)$$



Absolute value fitted to data.

# The MiniBooNE QE Puzzle Explanations



MB flux averaged

Data corrected  
for pion production  
followed by  
pion absorption!

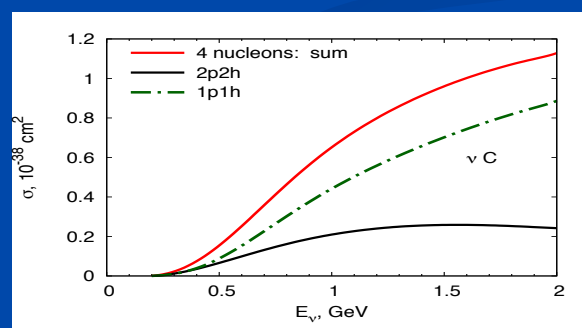
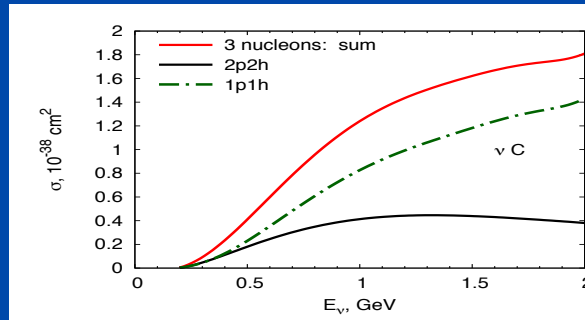
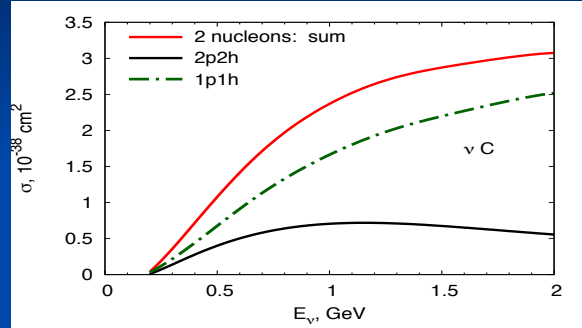
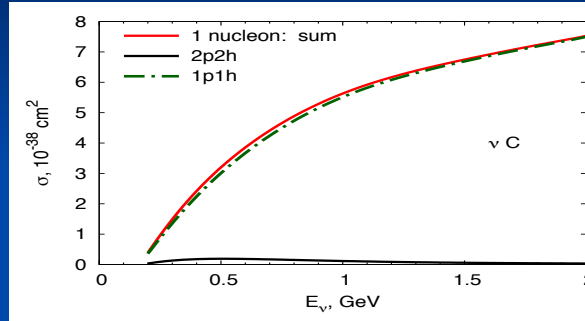
Inclusive double-differential  
X-sections insensitive to  
details of interaction

# The MiniBooNE QE Puzzle

## Explanations

- Angle dependence:
  - Transverse 2p-2h contrib increases with angle
  - QE contrib decreases strongly with angle
    - ➔ Ratio 2p-2h increases steeply with angle
- Inclusive Cross section insensitive to specifics of 2p-2h interaction model
  - ➔ Need experimental check

# The MiniBooNE QE Puzzle Knock-Out



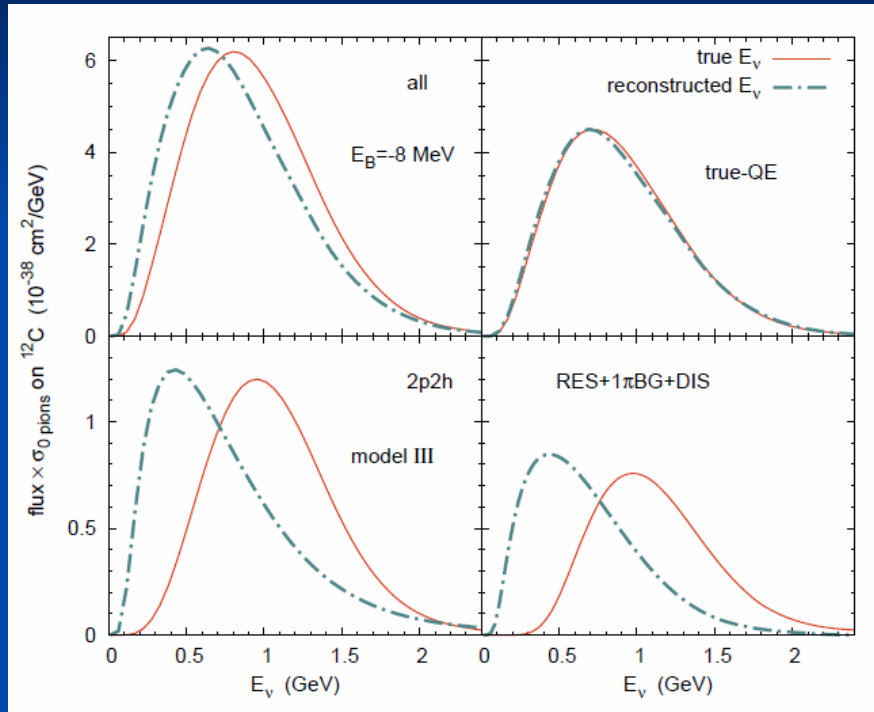
# Energy Reconstruction by QE

- All modern experiments use heavy nuclei as target material: C, O, Fe → nuclear complications
- Quasifree kinematics used for QE on bound nucleons: Fermi-smearing of reconstructed energy expected
- For nuclear targets QE reaction must be identified to use the reconstruction formula for  $E_\nu$
- But: exp. definition of QE cannot distinguish between true QE (1p-1h),  $N^*$  and 2p-2h interactions



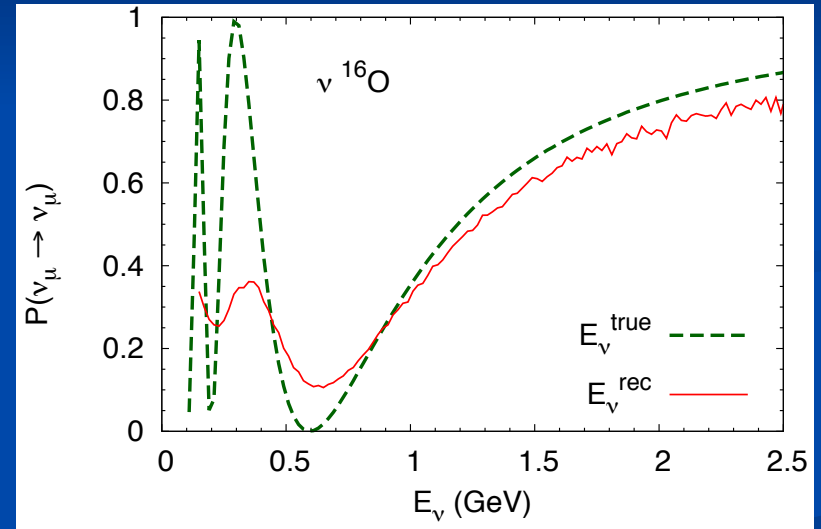
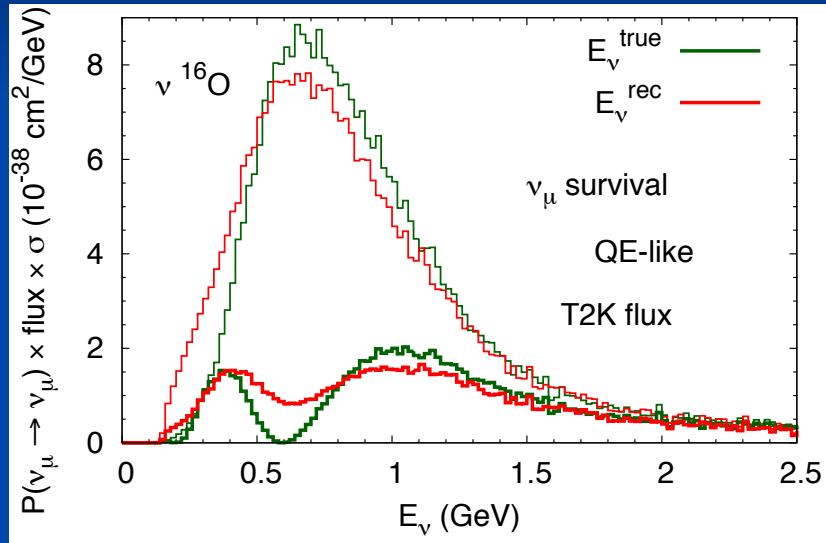


# Energy reconstruction in MB



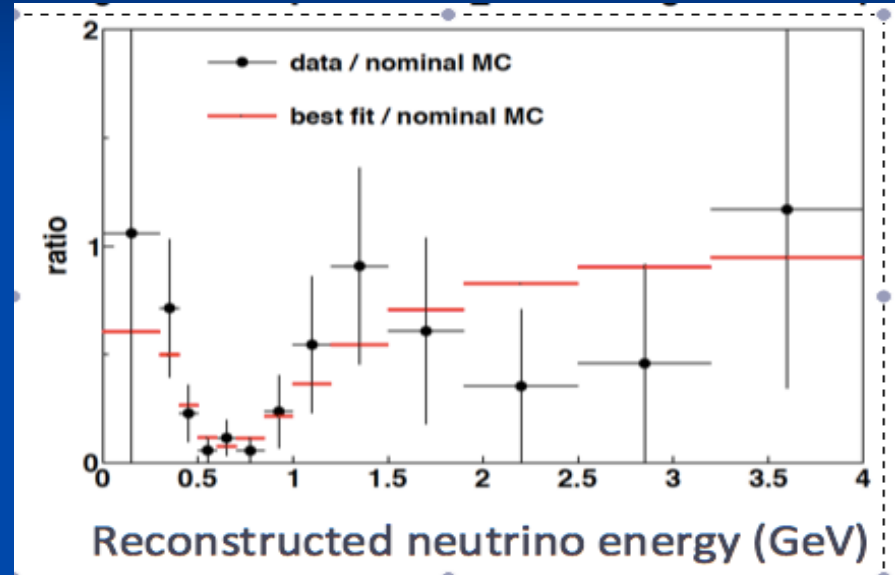
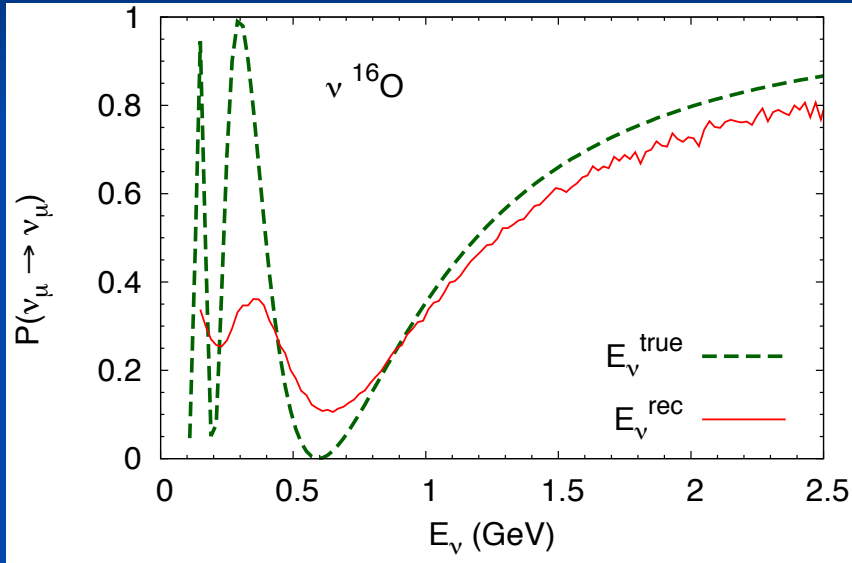
Reconstructed energy shifted to lower energies for all processes beyond QE

# Energy reconstruction and Oscillation signal in T2K

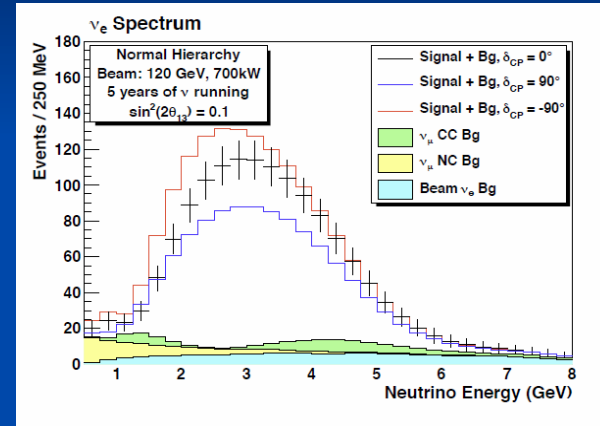
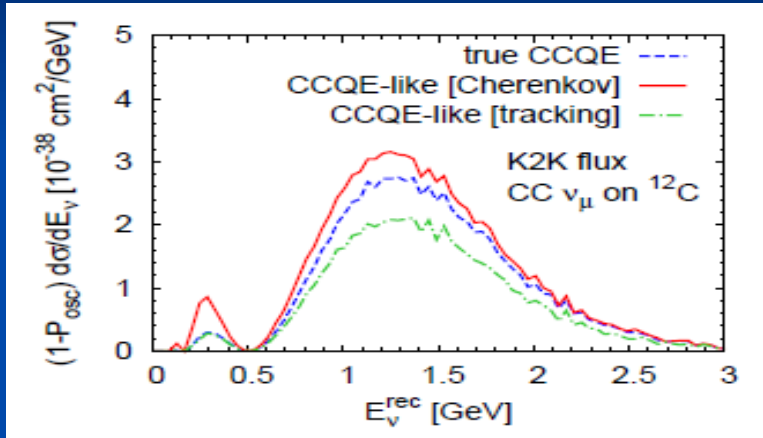


Ratio = oscillation probability

# Energy reconstruction and Oscillation signal in T2K

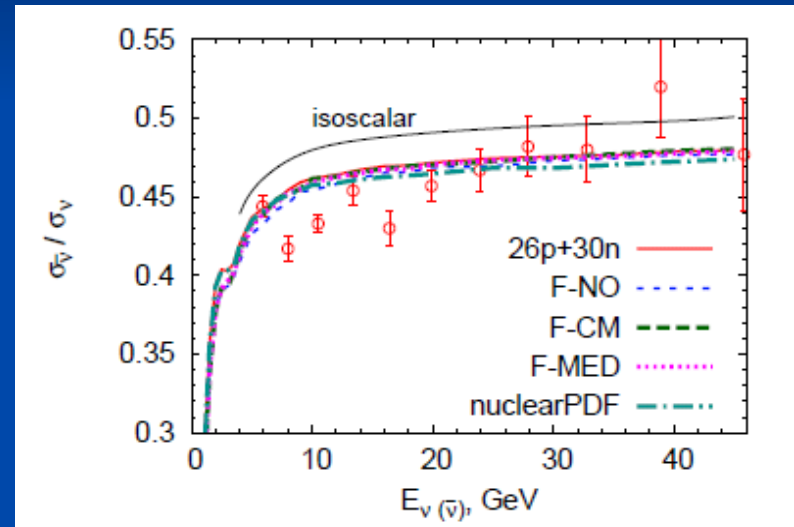
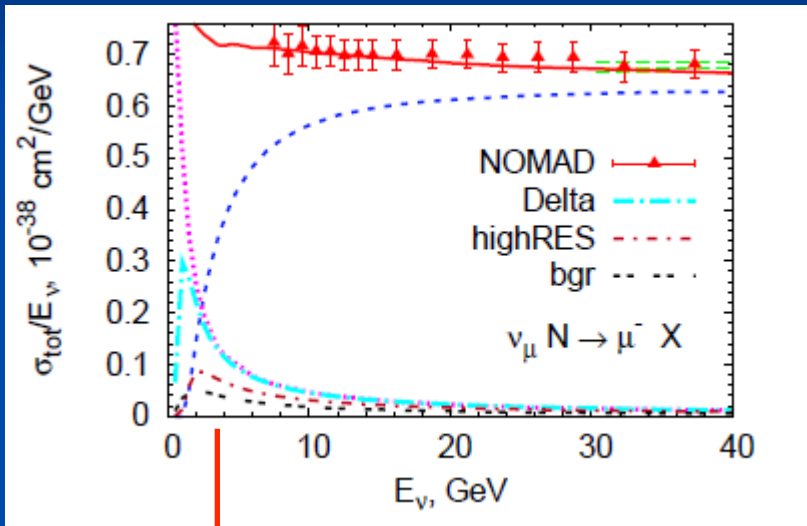


# $\delta_{CP}$ with LBNE



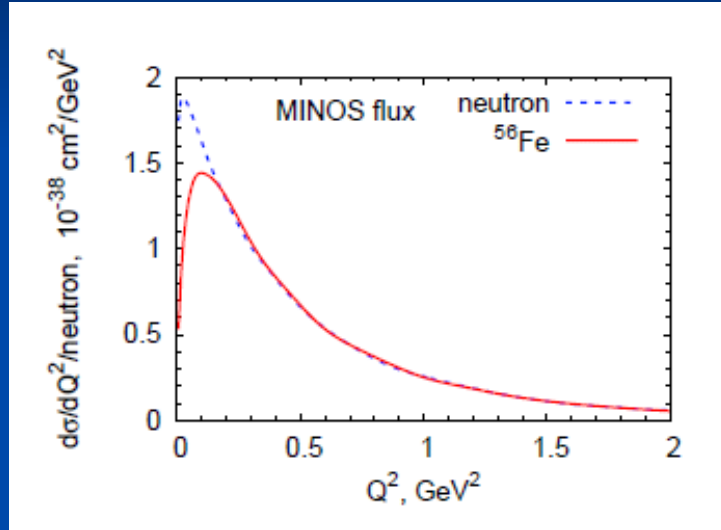
Uncertainties at the oscillation maximum due to detector as large as dependence on CP violating phase

# Experiments at higher energies



Shallow Inelastic Region

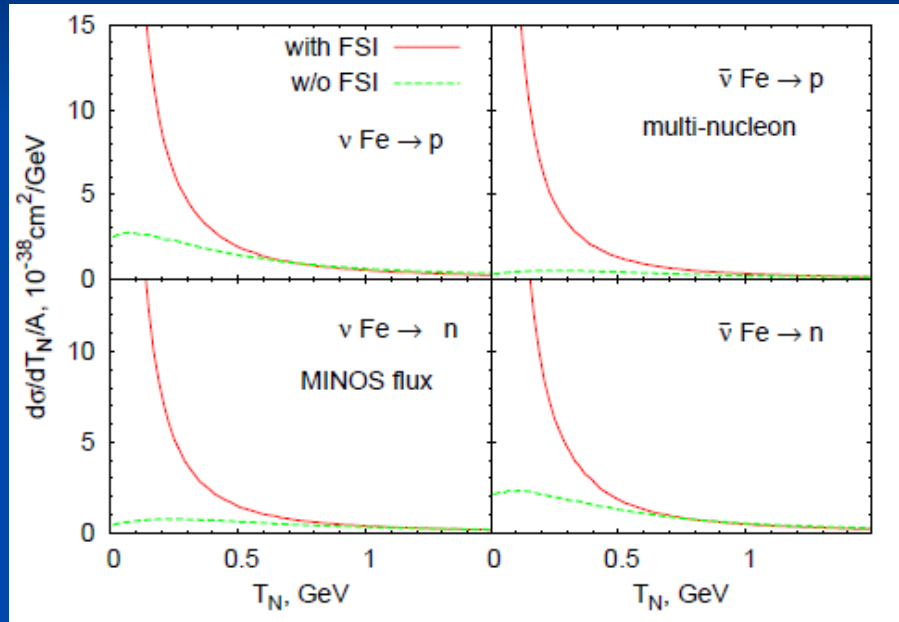
# Experiments at higher energies



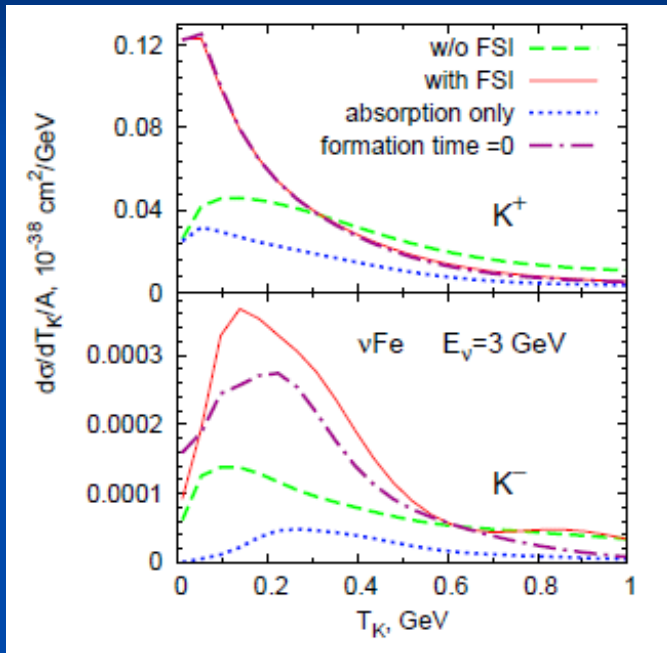
$Q^2$  dependence similar to lower-energy MB experiment

# Experiments at higher energies

## Knock-out Nucleons



# Experiments at higher energies



Lesson for Minerva:

The particles you measure are not always those that the neutrino produced



# Summary

- Event generators for neutrino-nucleus interactions have to describe QE,  $\pi$  production and DIS simultaneously
- Due to flux average reaction types are closely entangled
- MB puzzle of high axial mass explained:  
2p-2h processes fitted in terms of 1p-1h model
- Energy reconstruction based on QE leads in Cerenkov detectors to downward shift of reconstructed distribution
- FSI are extremely important, may make the extraction of elementary neutrino-particle production rates impossible

