

# Precision measurements of $\mu^+$ , $\mu^-H$ , and $\mu^-D$ lifetimes.

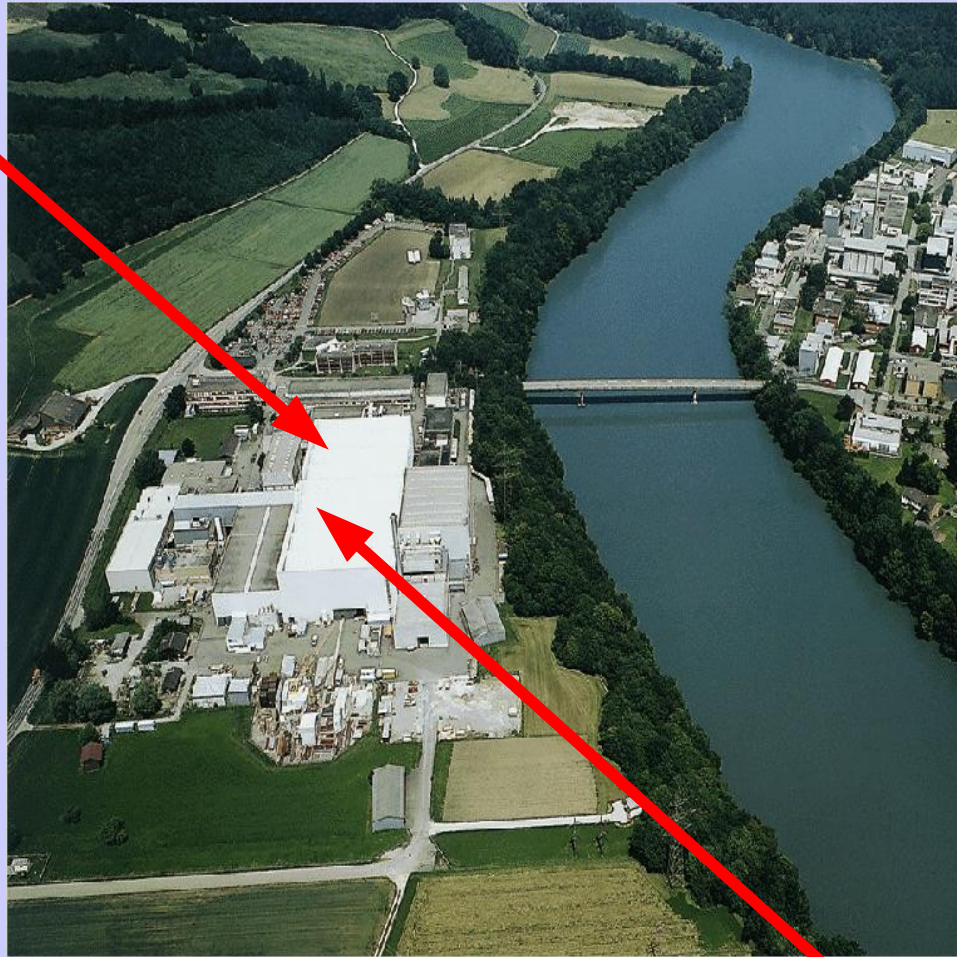
**Tim Gorringer, Univ. of Kentucky,  
for the MuLan, MuCap, MuSun Collaborations**

Elba XI, June 21-25

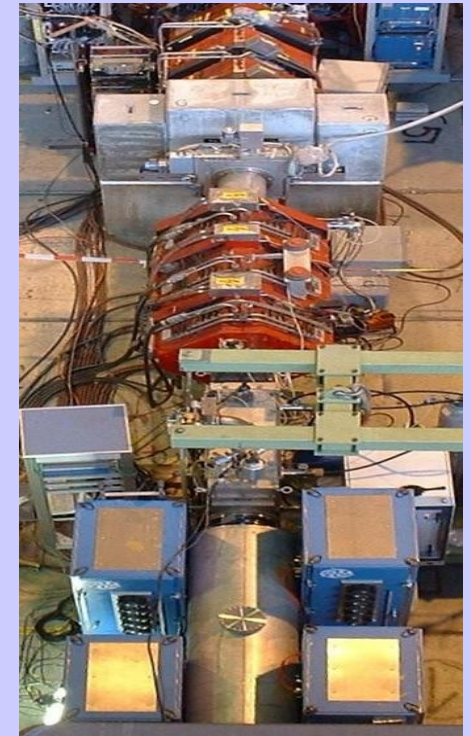
# Paul Scherrer Institute.



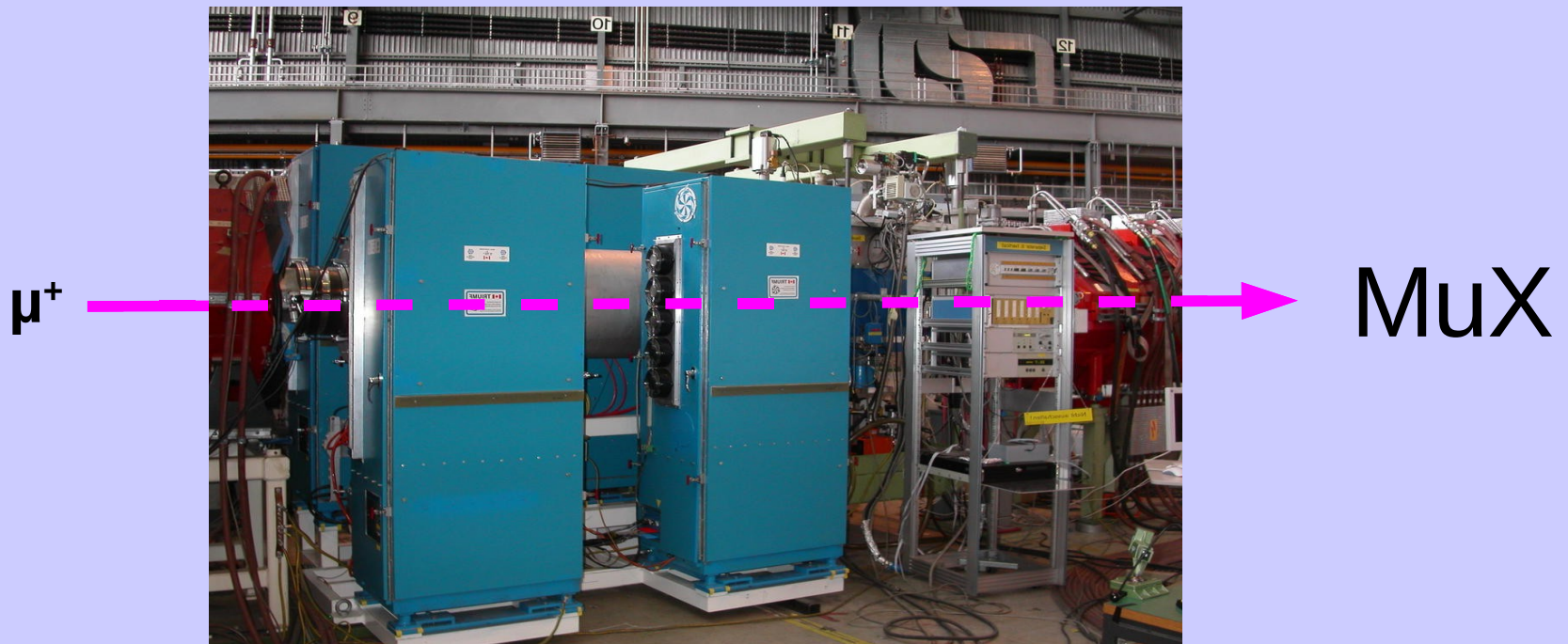
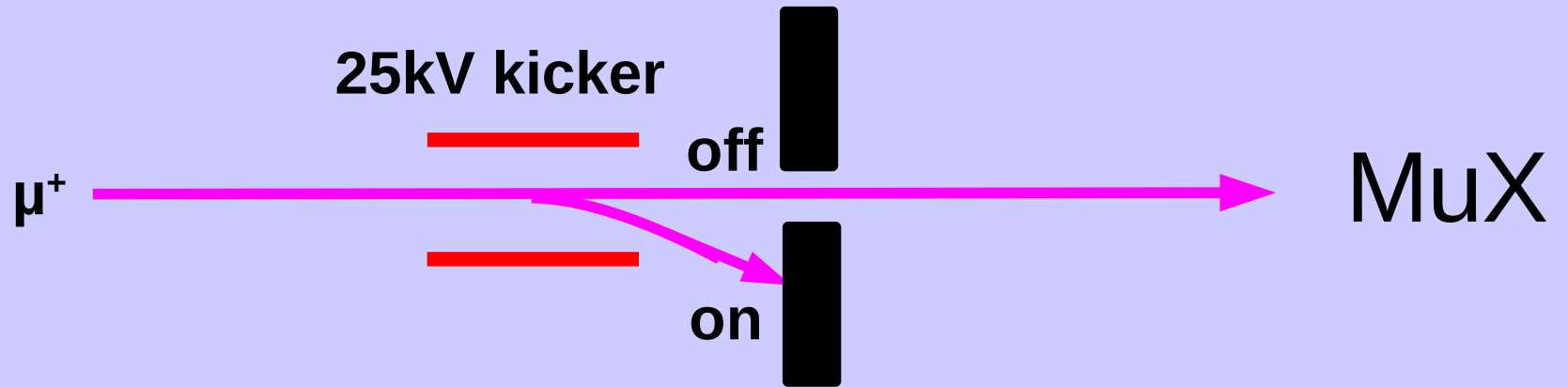
2.0mA, 590 MeV  
proton cyclotron



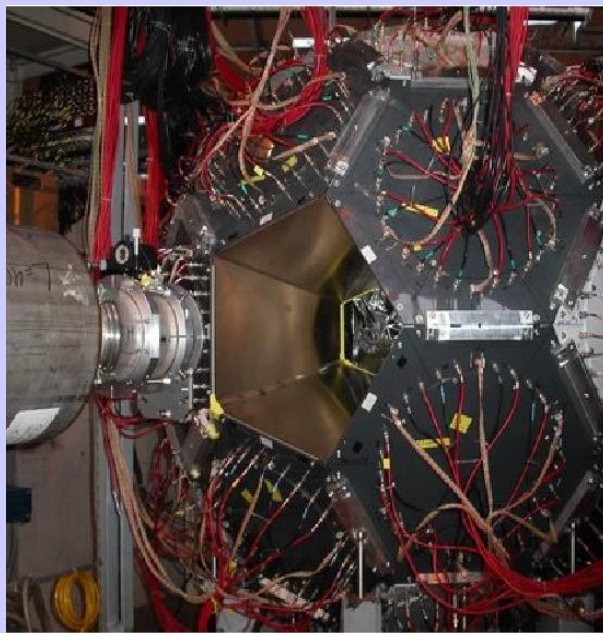
5 MeV, 30 MeV/c  
pulsed muon beam



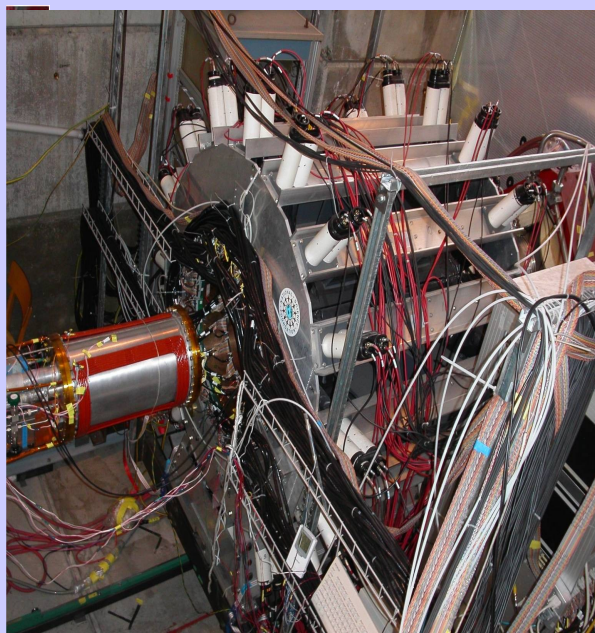
# Pulsed Muons and Muon On Request.



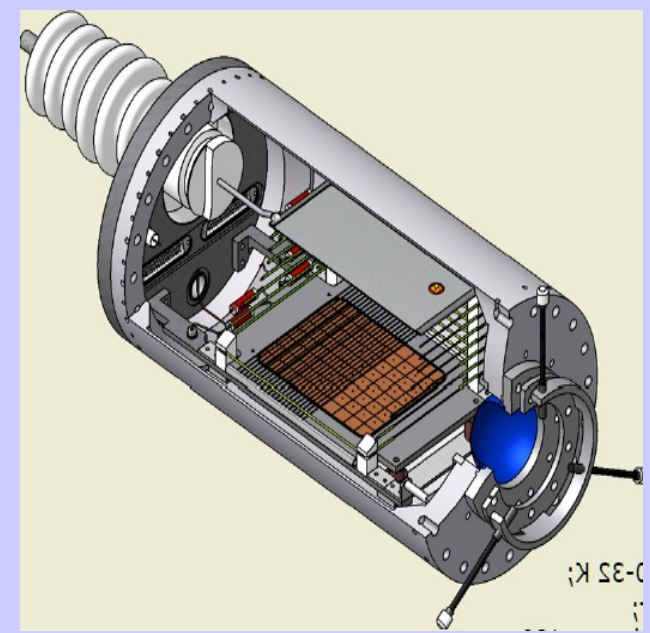




MuLan



MuCap



MuSun

scientific goals, experimental setups, experimental challenges, and results and status

*from the Fermi Constant...*

*to the proton's weak interaction...*

*and solar hydrogen burning*

*by part-per-million measurements of  $\mu^+$ ,  $\mu^-H$ , and  $\mu^-D$  lifetimes*

$$-\frac{\hbar}{i} \frac{\partial}{\partial t} = \frac{p^2}{2m} - \frac{Ze^2}{r}$$

$$\alpha = \frac{\hbar^2}{ec}$$

Muon — the muon lifetime  
and Fermi constant.



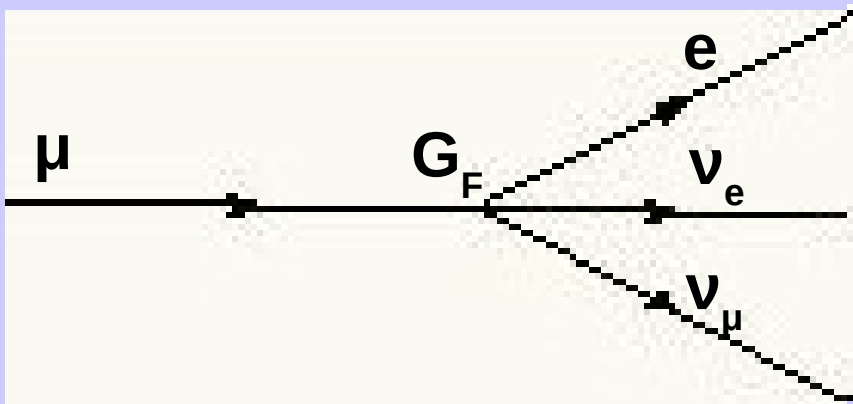
# Why we measure $\tau_{\mu^+}$ ?

knowledge of muon lifetime  $\tau_{\mu^+}$  allows precision measurements of weak nuclear interactions in muonic hydrogen, deuterium atoms.

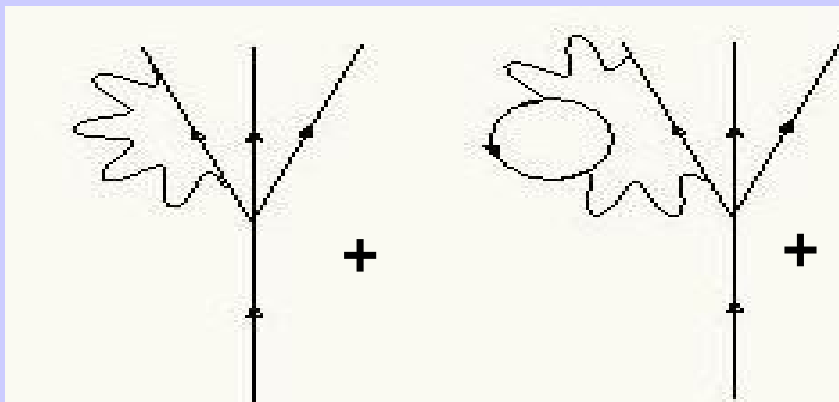
twenty-fold improvement in knowledge of fundamental constant  $G_F$  of weak interaction. [previously  $G_F (\pm 10 \text{ppm})$ ].

knowledge of  $\alpha$ ,  $G_F$ ,  $M_Z$  allows precision tests of standard model via measurements of Weinberg angle  $\Theta_W$ , W-boson mass  $M_W$ , ...

# How we determine $G_F$ ?



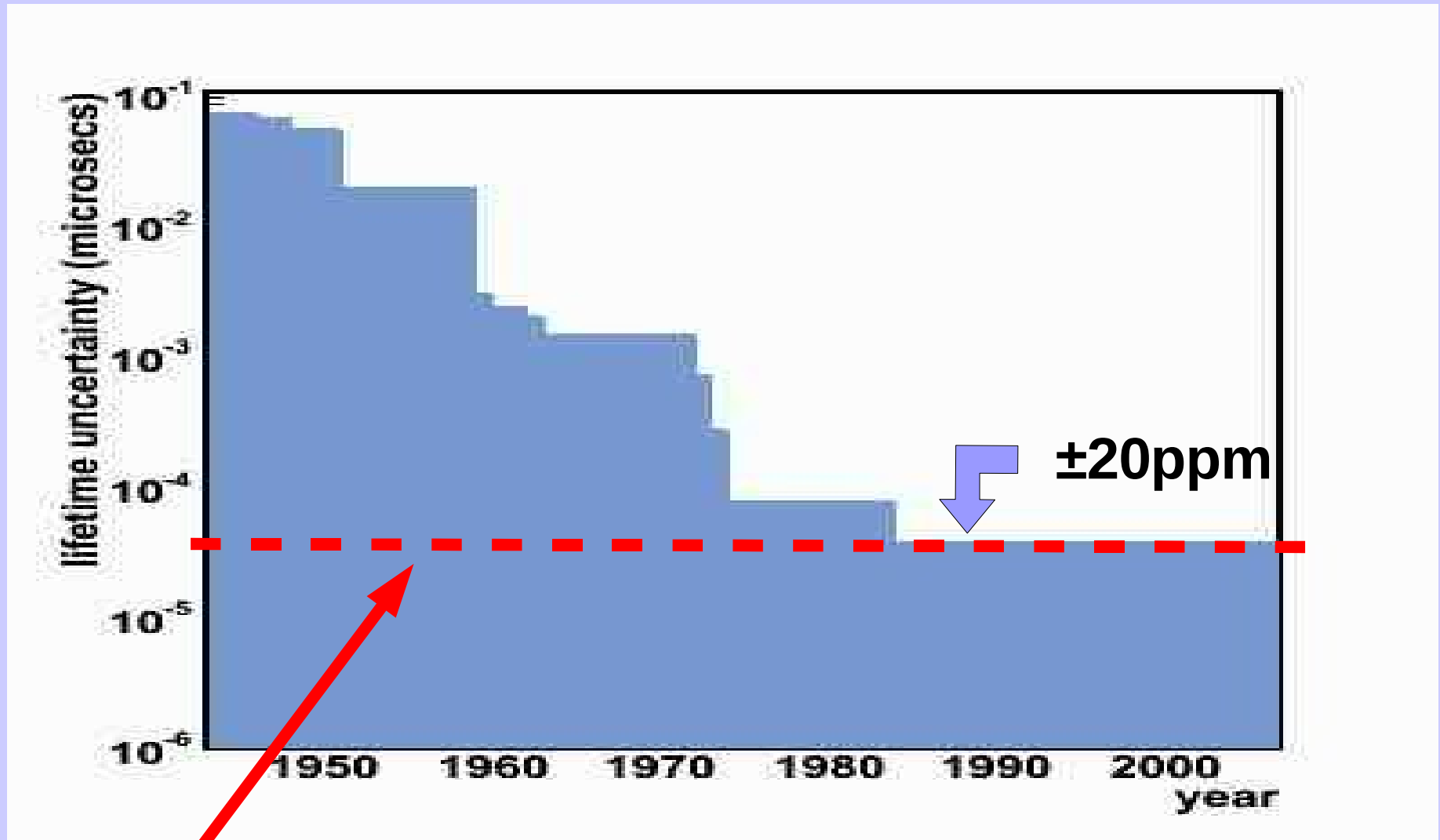
$$\frac{1}{\tau_\mu} = \frac{G_F^2 m_\mu^5}{192 \pi^2} (1 + \Delta q)$$



$\Delta q$  contains QED, QCD  
radiative corrections

$\sim \mathbf{0.1 \text{ ppm}}$  uncertainty in  $\mathbf{T_\mu - G_F}$  relationship from  $\mathbf{\Delta q, m_\mu}$

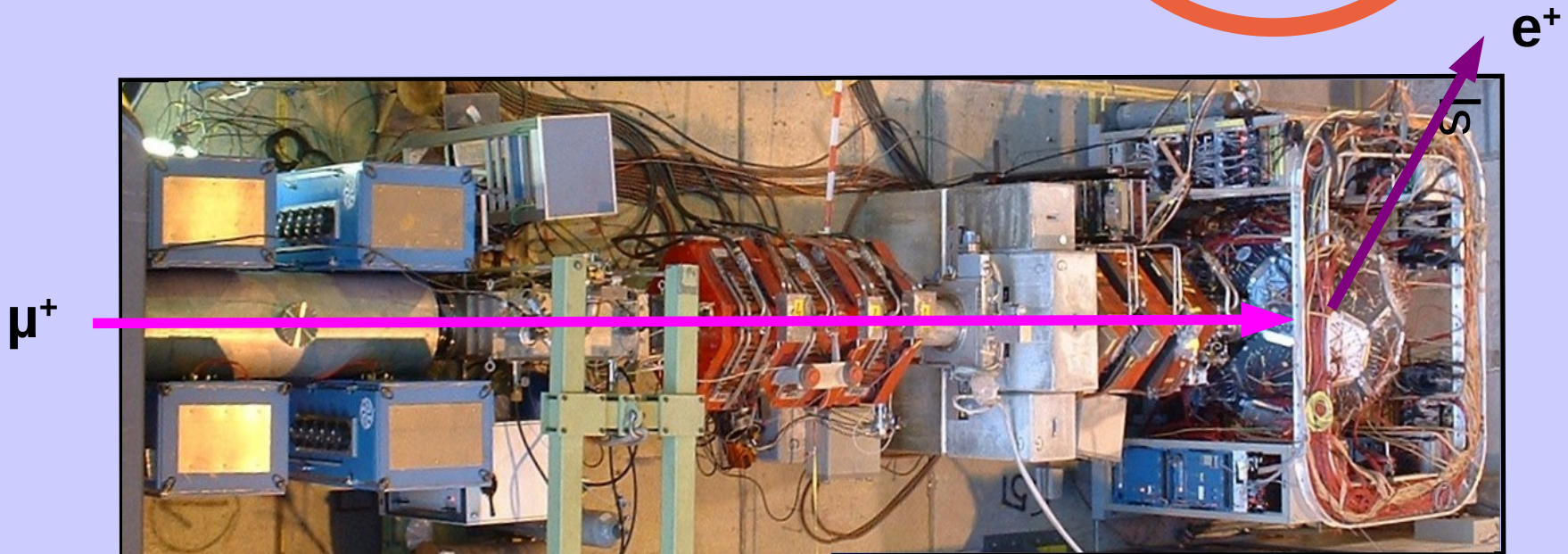
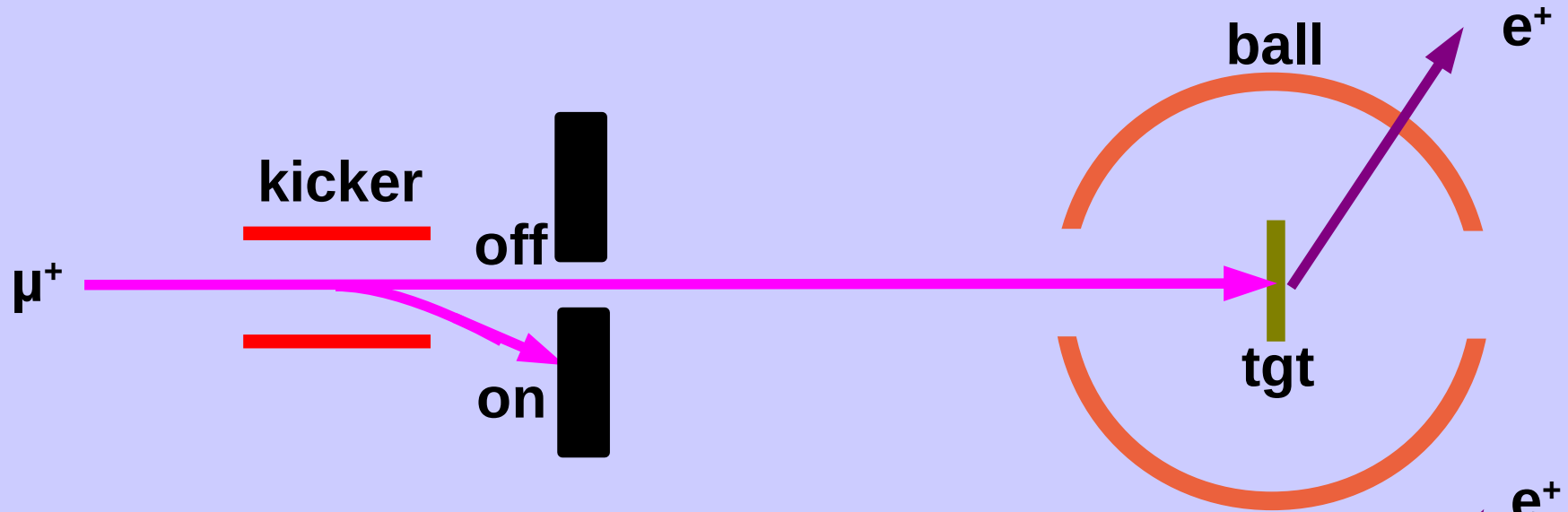
pre-MuLan history of  $\tau_\mu = 2.19703(4) \mu\text{s}$



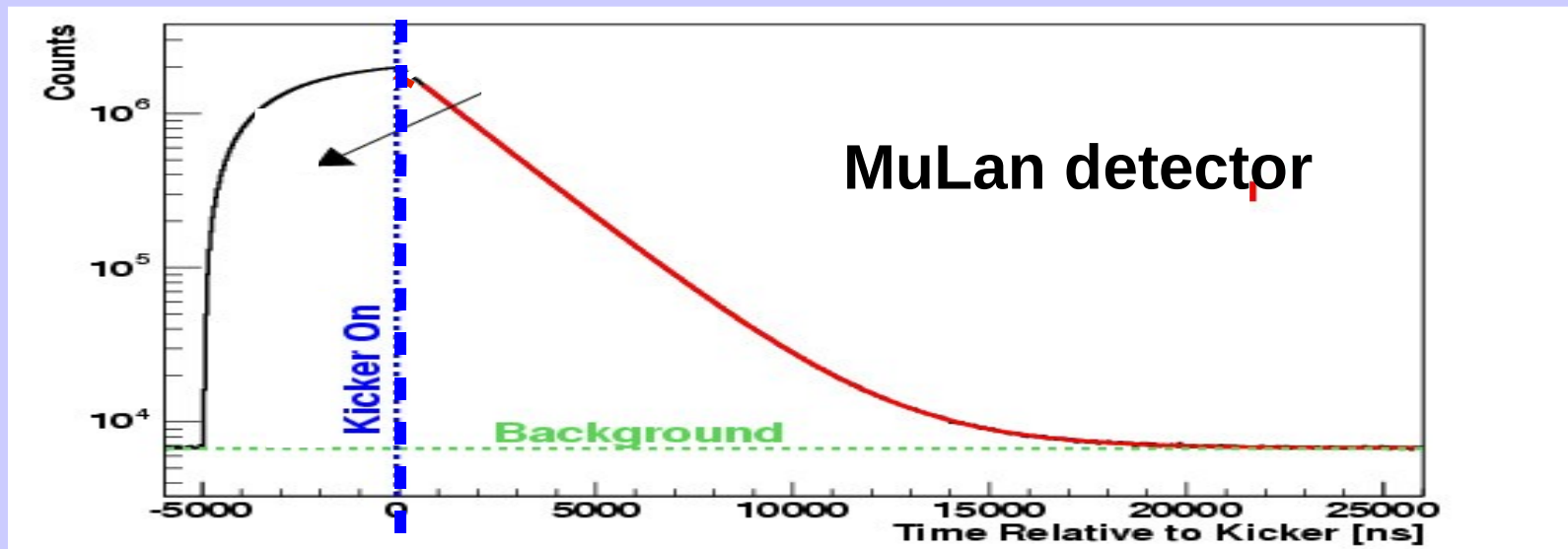
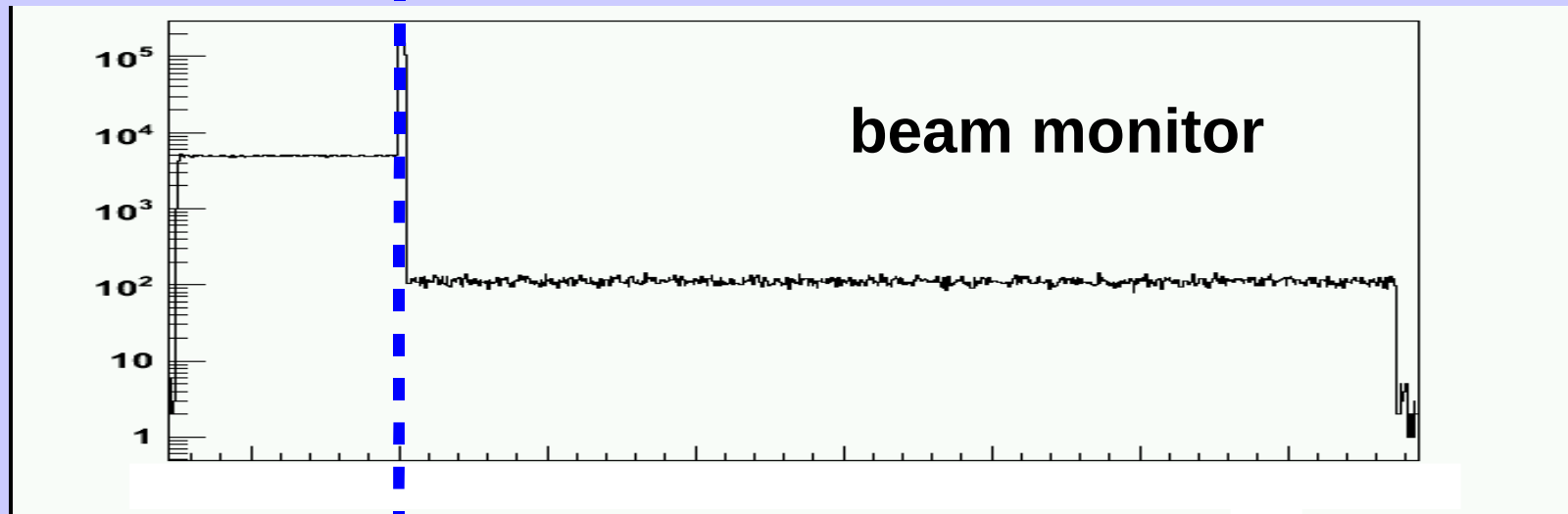
one-by-one muon experimental limit



accumulating  $\mu^+$ 's and measuring  $e^+$ 's



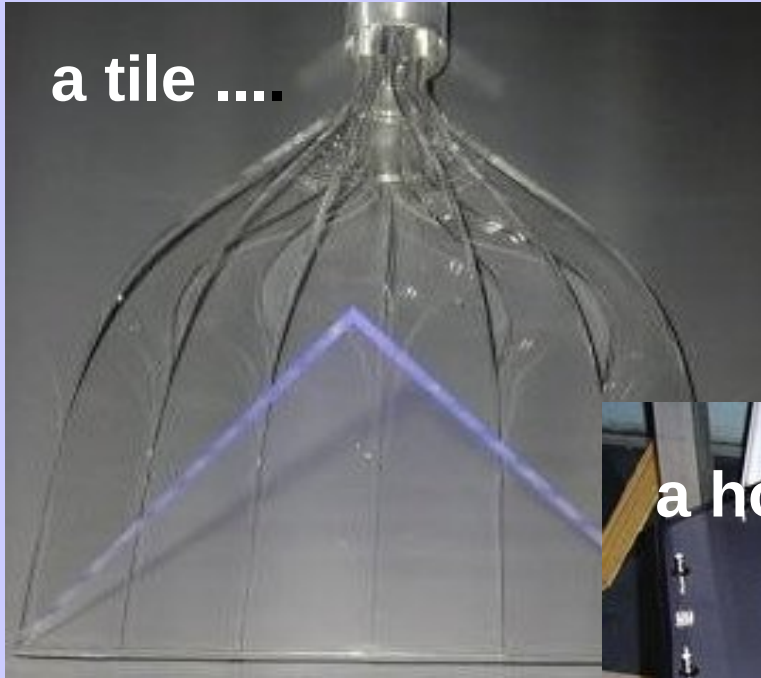
accumulating  $\mu^+$ 's and measuring  $e^+$ 's



beam on

beam off

a tile ....



a house ..

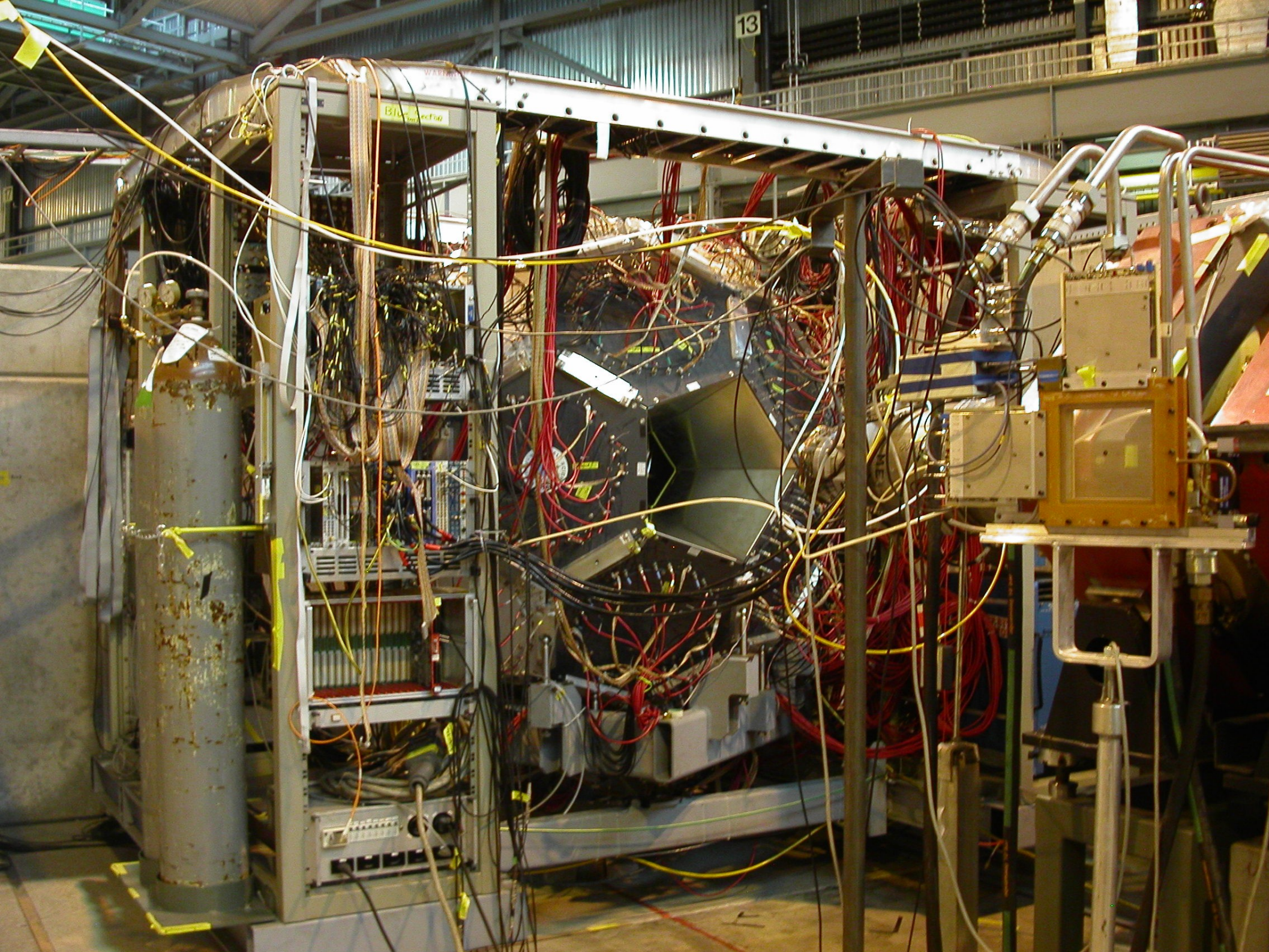


# MuLan detector

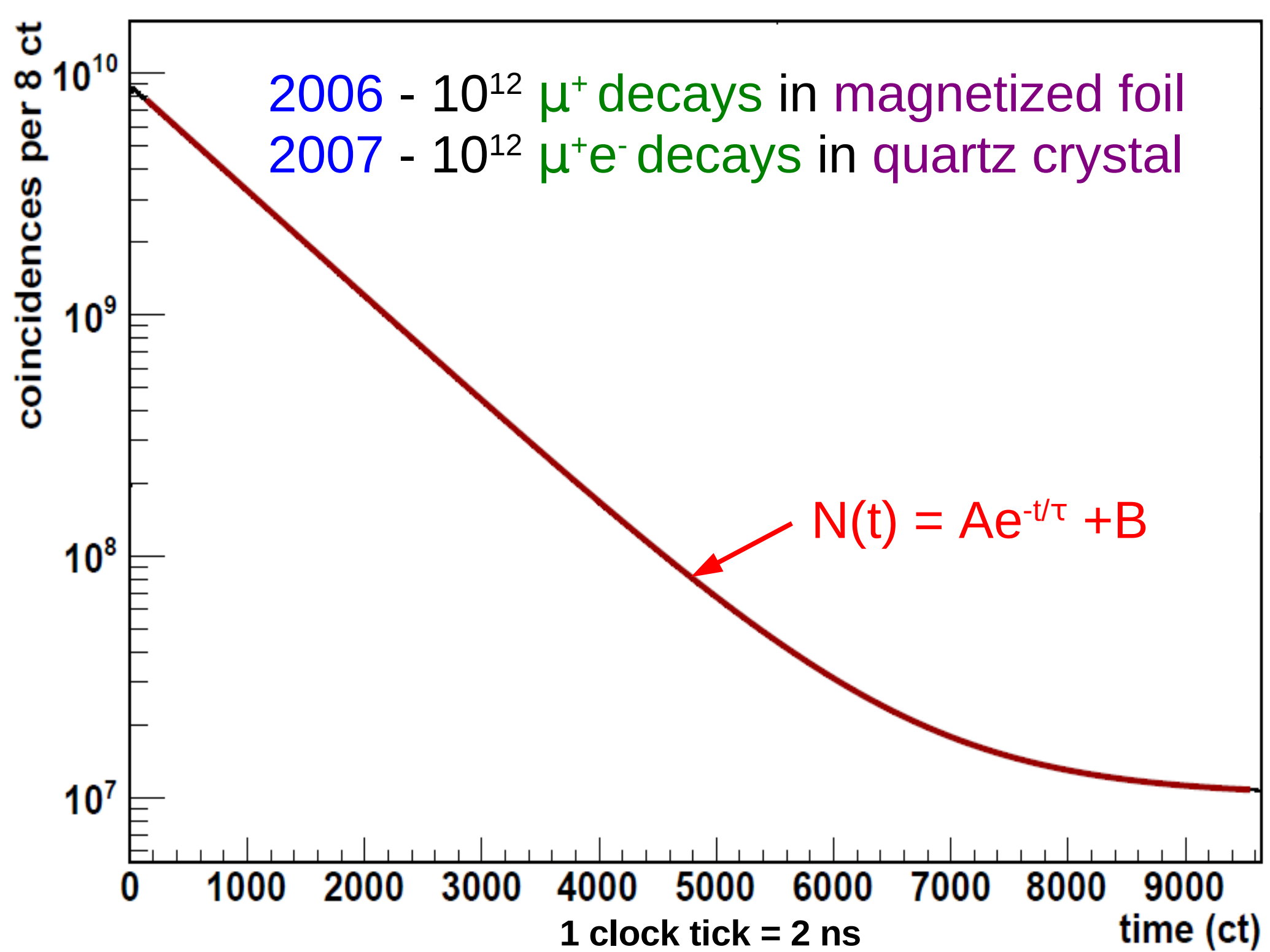
the ball.



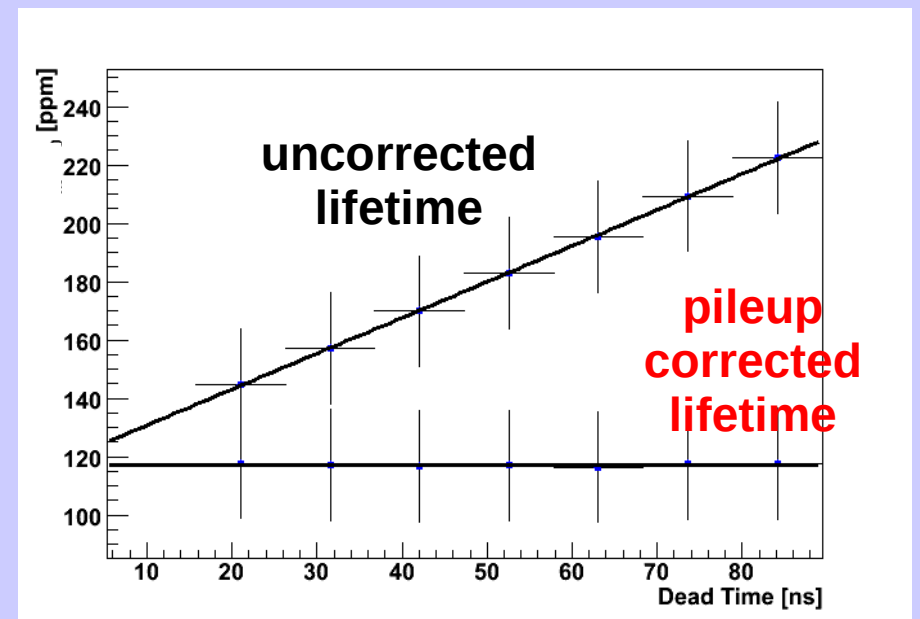
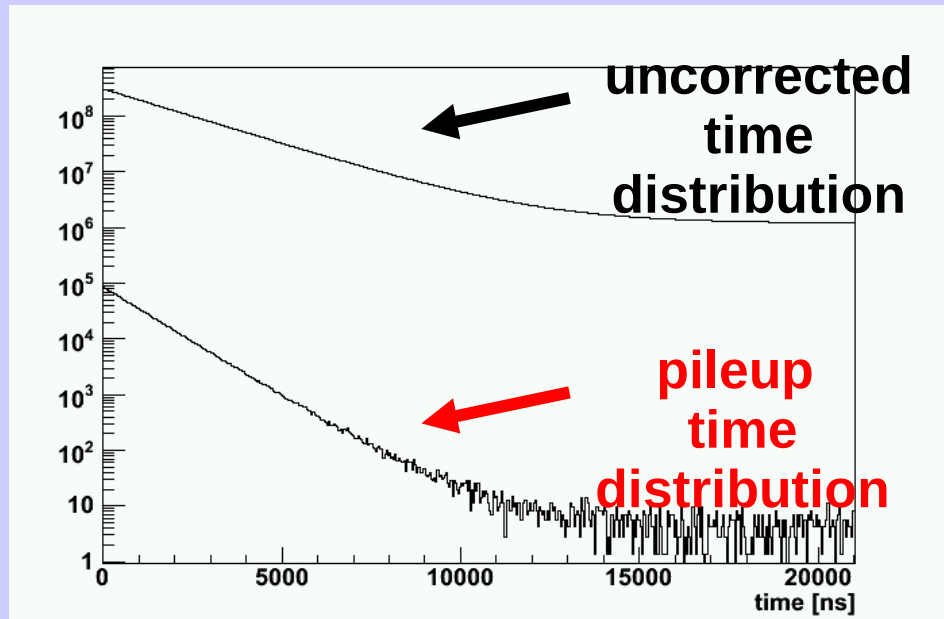
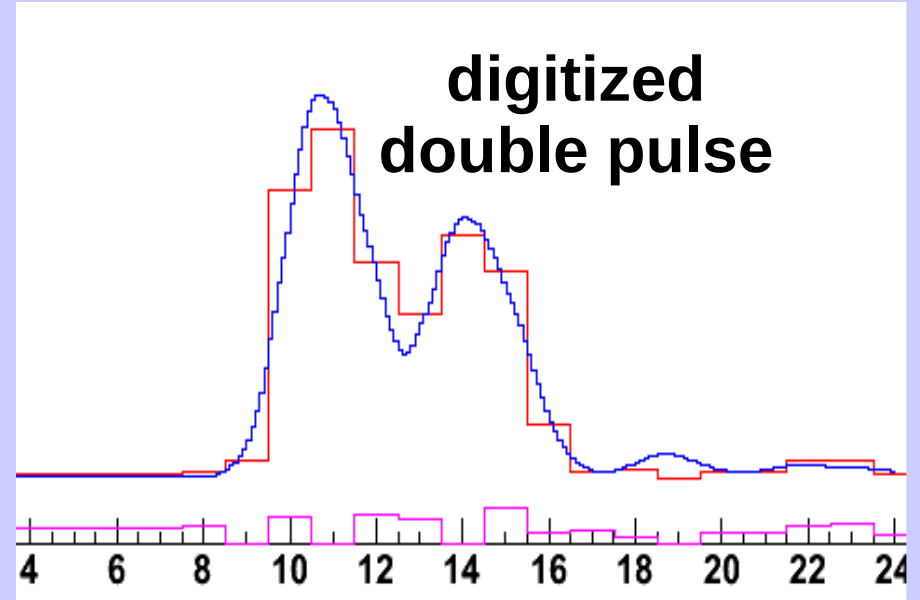
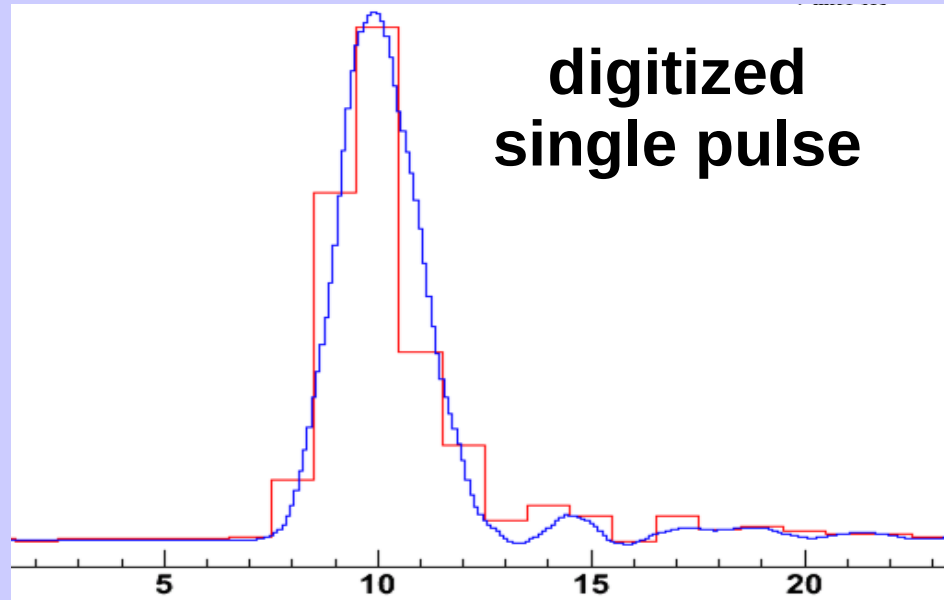




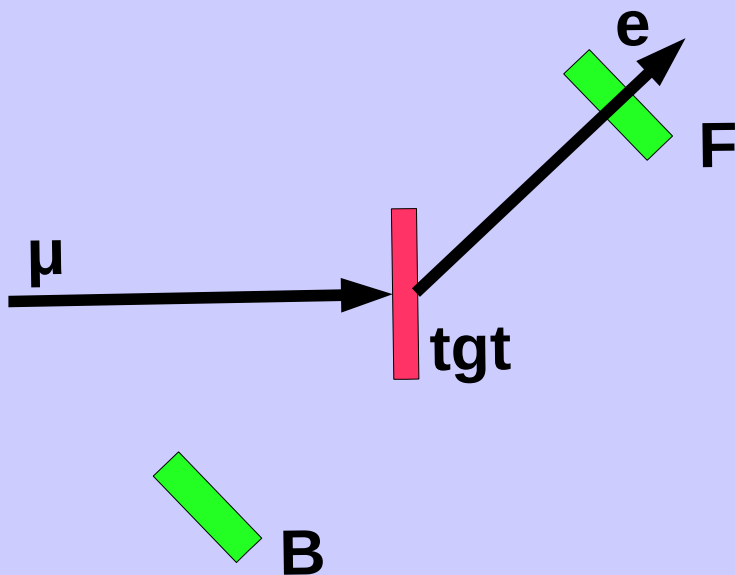
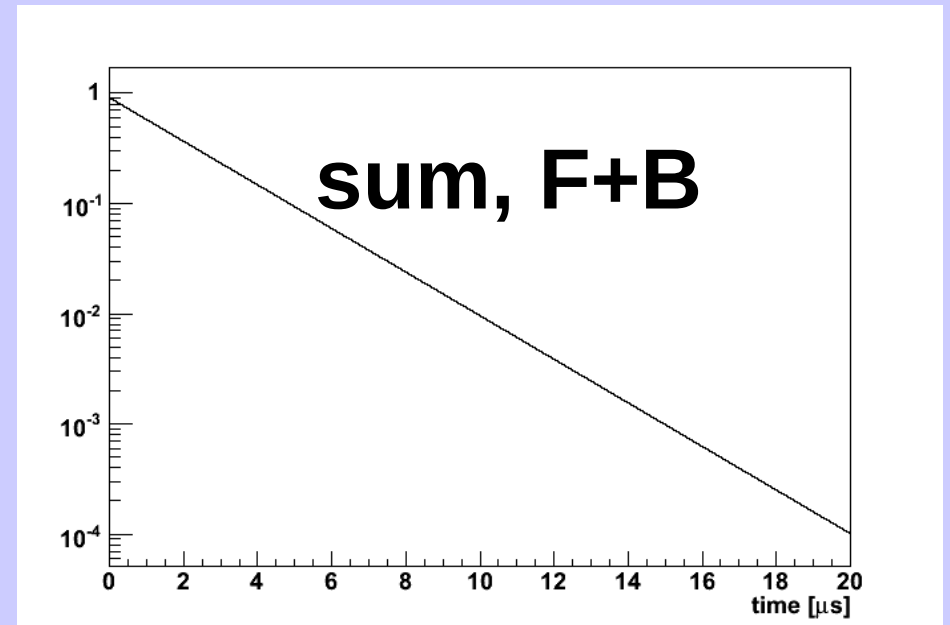
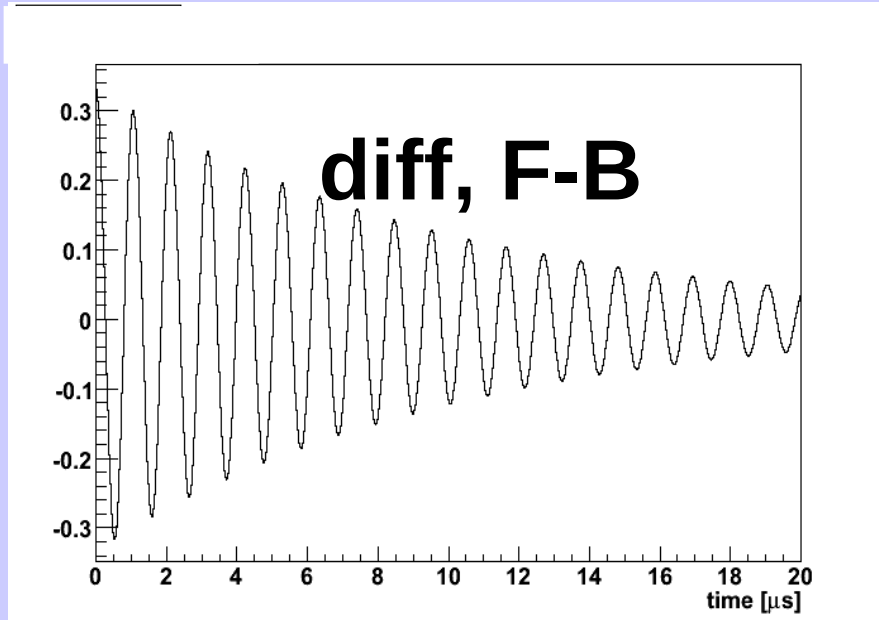




# - most worrisome systematics - positron pulse pile-up



# - most worrisome systematics - muon spin rotation



## TARGETS

**magnetized ferromagnetic foil**  
(high internal B-field, fast  $\mu^+$  precession)

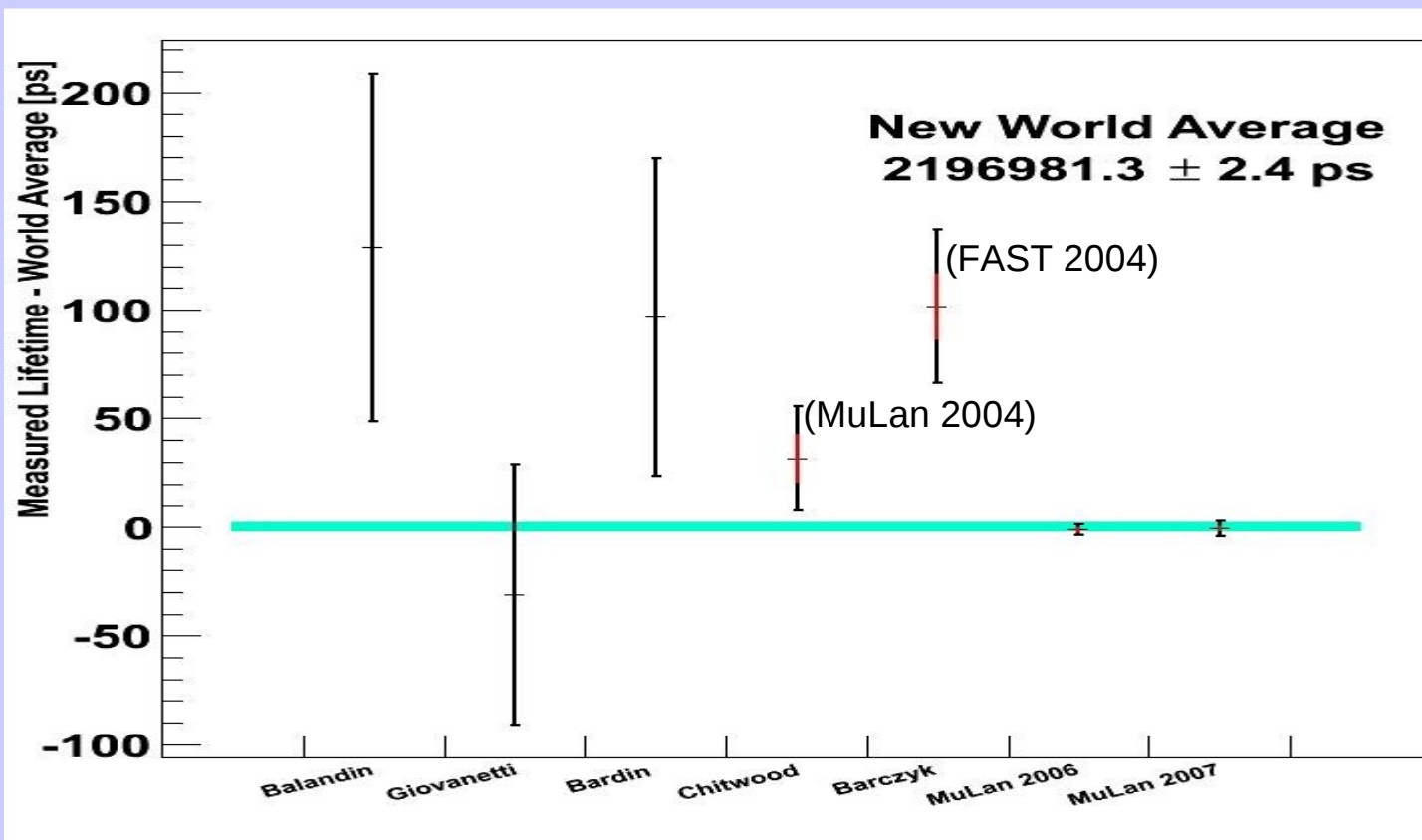
**single quartz crystal**  
(moderate external B-field, fast  $\mu^+e^-$  precession)

# MuLan Results

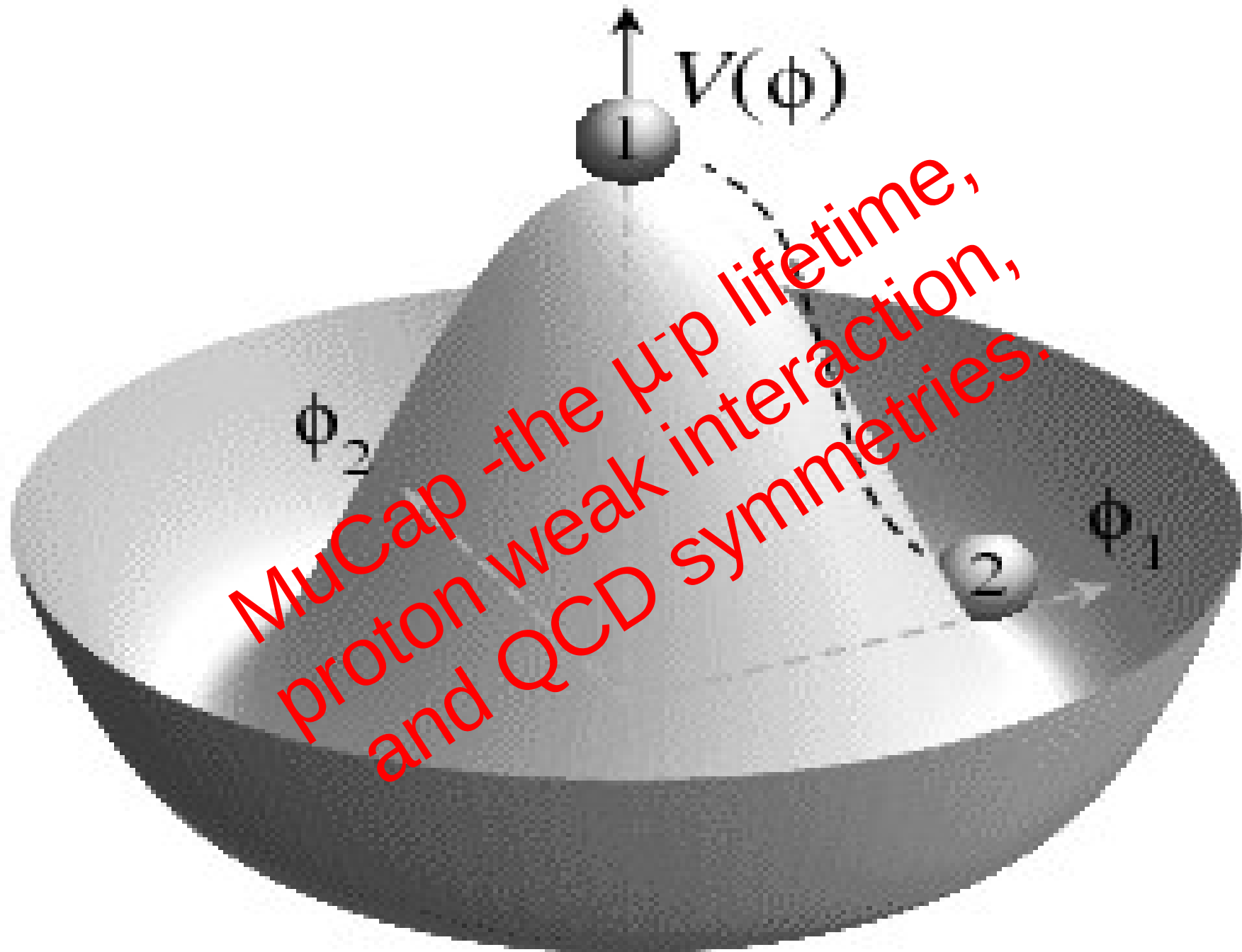
2006:  $\tau_\mu = 2196980.1 \pm 2.5(\text{stat}) \pm 1.2(\text{sys})$  ps

2007:  $\tau_\mu = 2196980.7 \pm 3.7(\text{stat}) \pm 1.2(\text{sys})$  ps

$$G_F = 1.166\,381\,8\,(7) \times 10^{-5} \text{ GeV}^{-2} \text{ (0.6 ppm)}^*$$



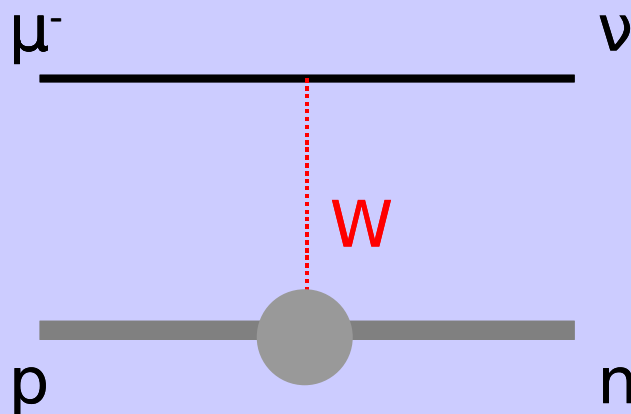




MuCap - the  $\mu$ -p lifetime,  
proton weak interaction,  
and QCD symmetries.

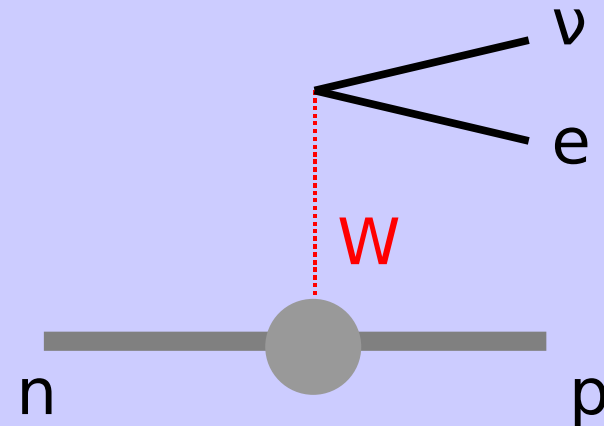
# Why we measure $\tau_{\mu p}$ ?

muon capture,  
 $\mu^- p \rightarrow \nu n$



proton's weak couplings  
 $g_v, g_a, g_m, g_p$

beta decay,  
 $p \rightarrow n e^+ \nu$



proton's weak couplings  
 $g_v, g_a$

knowing  $g_v, g_a, g_m$  determine  $g_p$ ,  
the poorly known **proton induced pseudoscalar coupling**

# Why we determine $g_p$ ?

fundamental quantity describing the proton's weak interaction

the approximate conservation of axial current enforces a rigorous relation between the weak couplings  $g_p$ ,  $g_a$

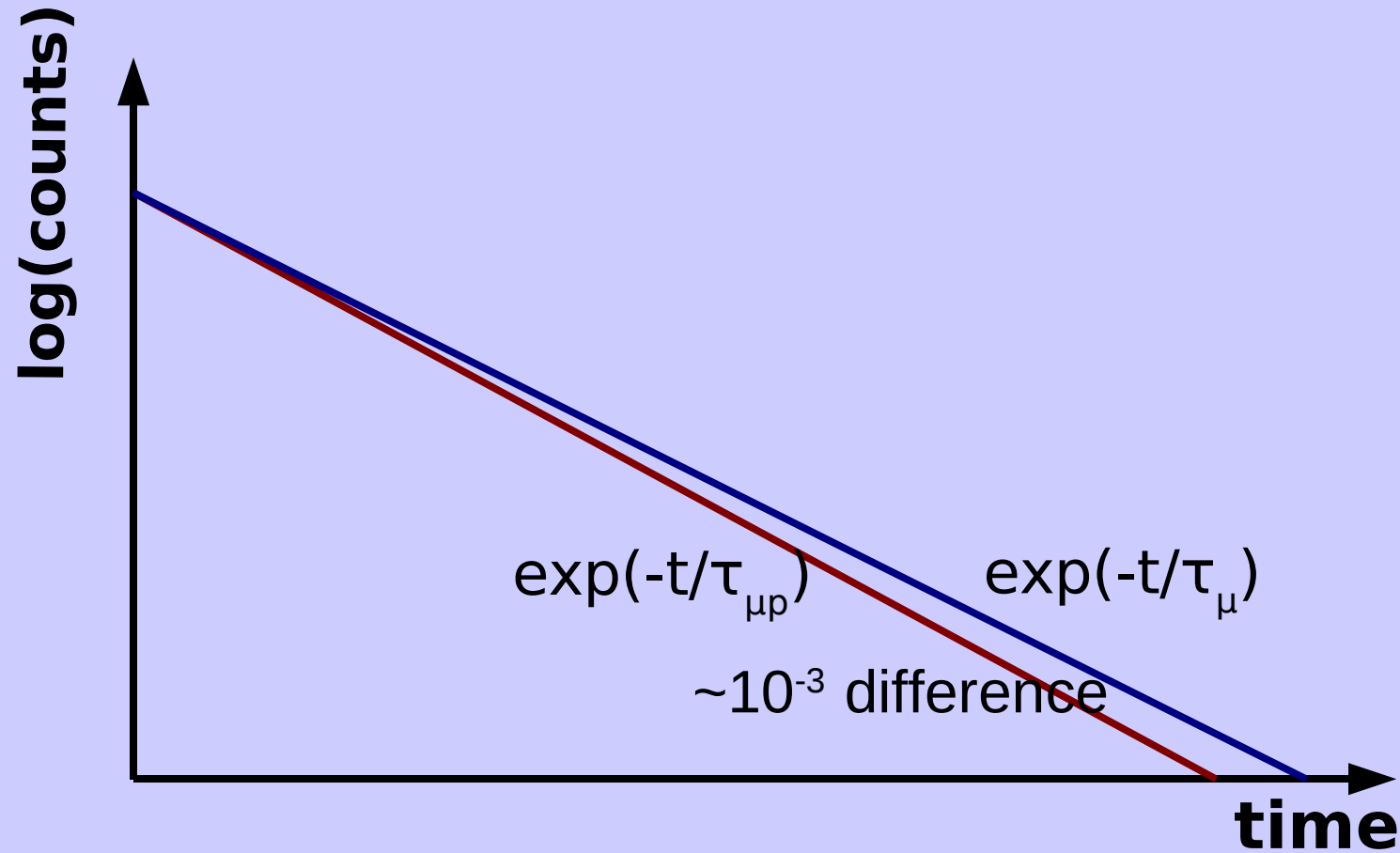
$$g_p(q^2 = -0.9m_\mu^2) = (6.47 \pm 0.18) g_a(0) = 8.26 \pm 0.23$$

Verification represents an important test of QCD symmetries

knowledge of  $g_p$  (with  $g_v$ ,  $g_a$ ,  $g_m$ ) allows precision studies of weak nuclear interactions through nuclear muon capture (e.g.  $\mu$ -D experiment).

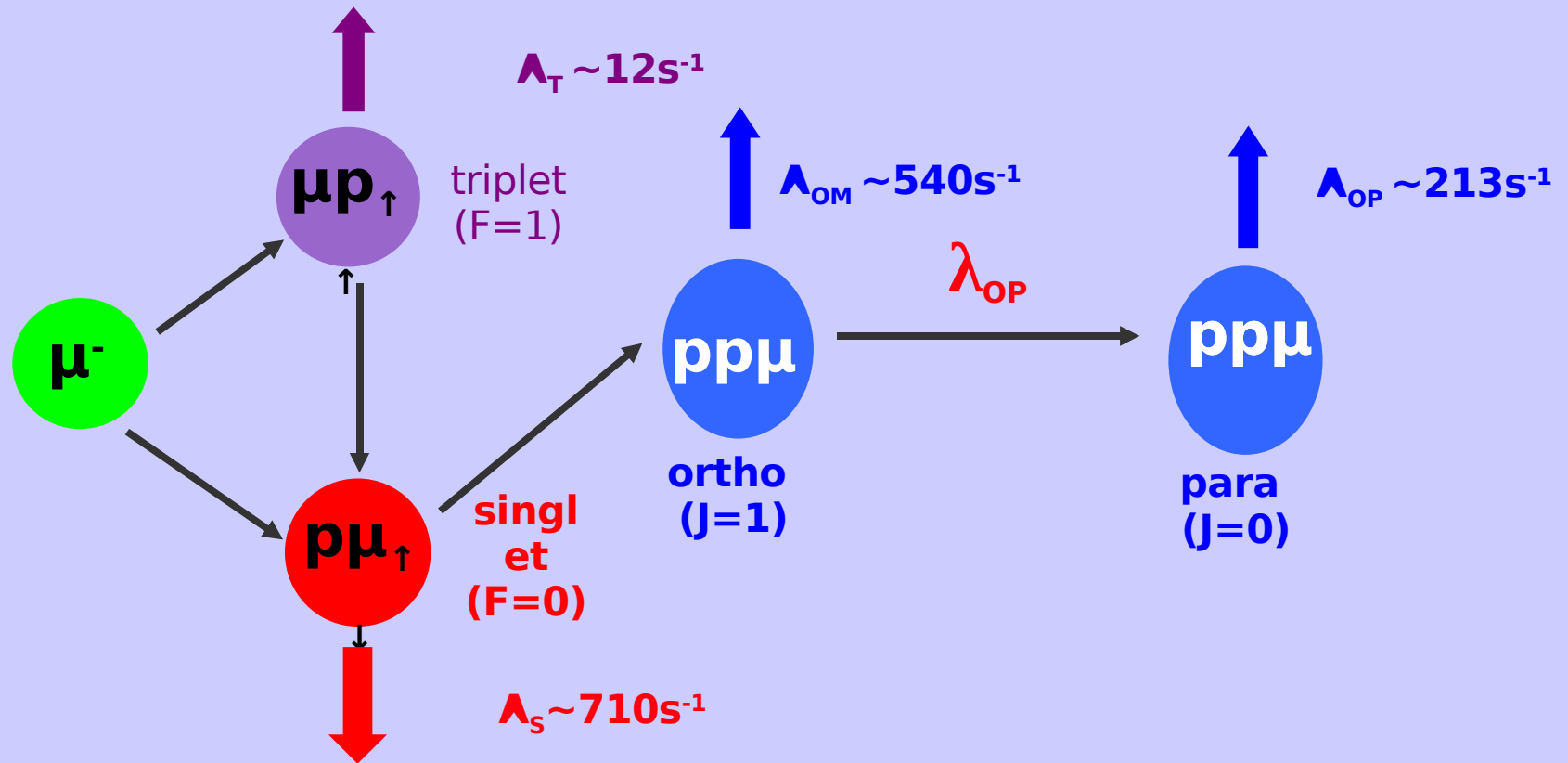
# How we determine $g_p$ ?

determine the  $\mu^-p \rightarrow \nu n$  rate  
by  $\Lambda = 1/\tau_\mu - 1/\tau_{\mu p}$





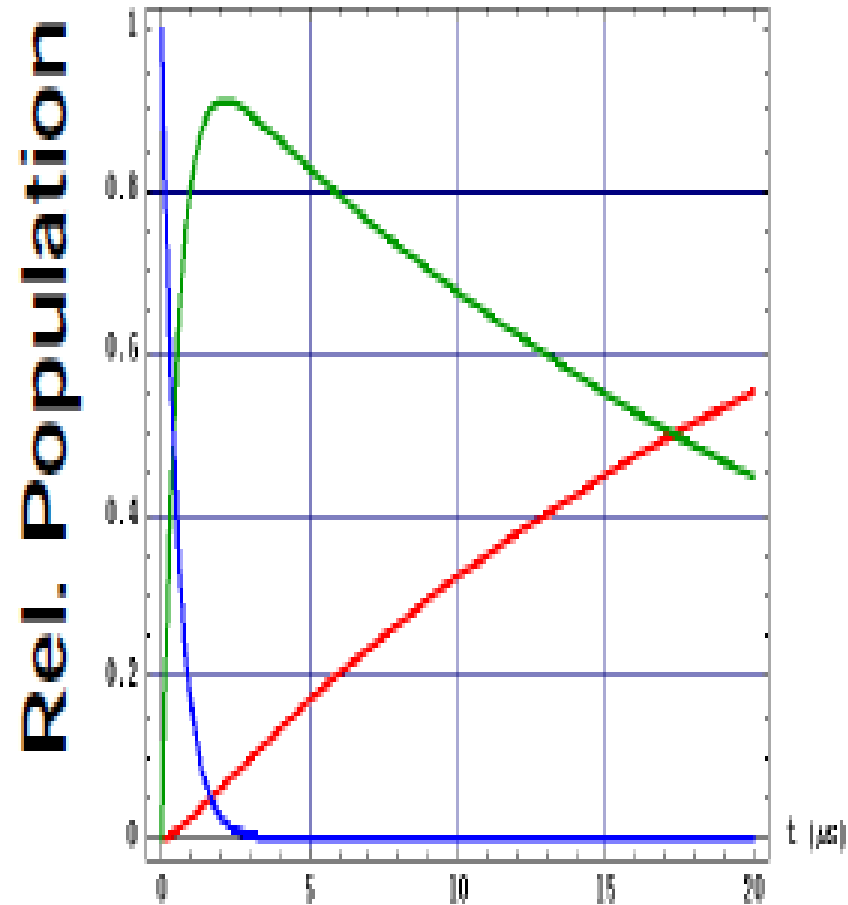
# $\mu$ chemistry, a complication



use ultra-pure (chemically, isotopically  
10 bar  $H_2$  (1% liquid hydrogen density))

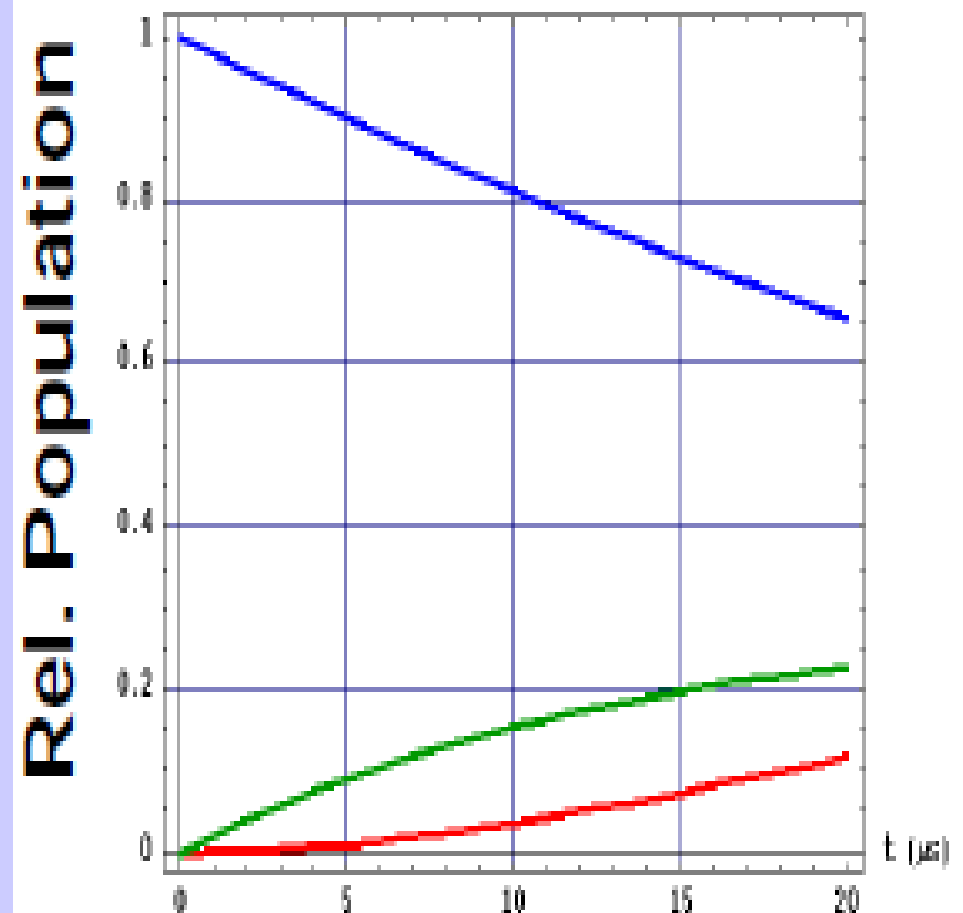
Relative populations of  
singlet atoms, ortho molecules, para molecules  
in liquid and gas

$\phi = 1$  (Liquid)



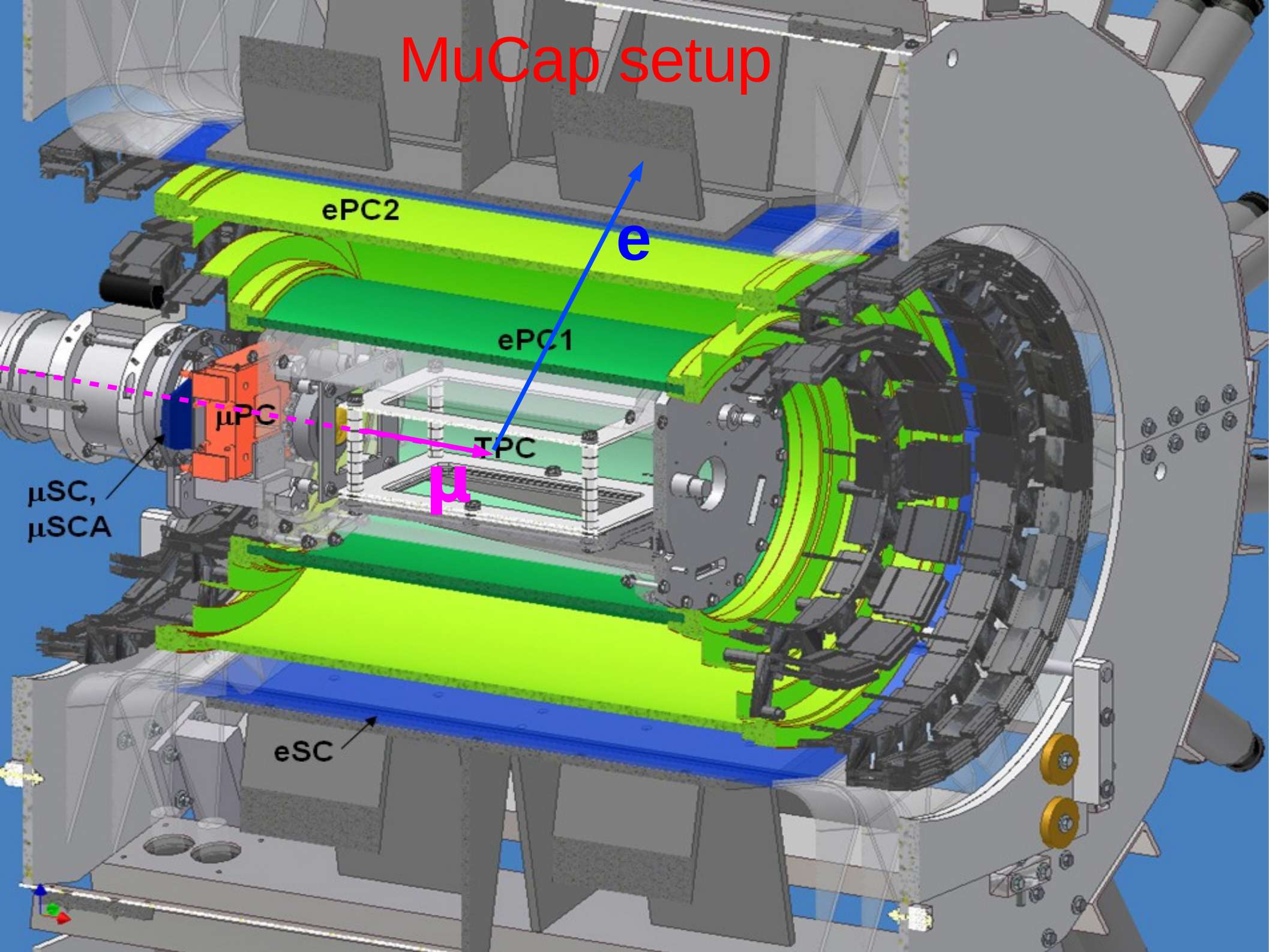
Time after  $\mu$ p Formation

$\phi = 0.01$  (~10 bar gas)



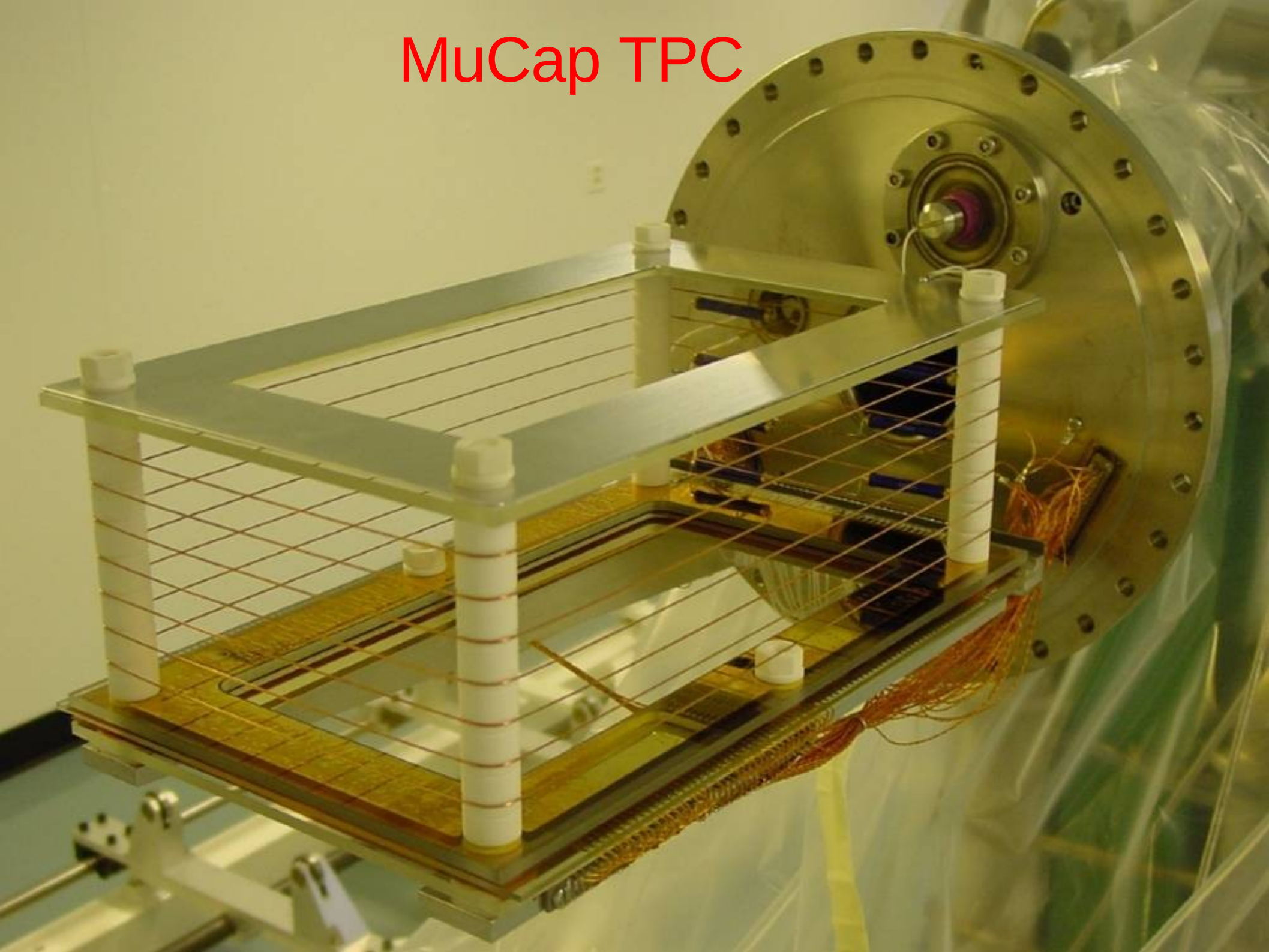
Time after  $\mu$ p Formation

# MuCap setup



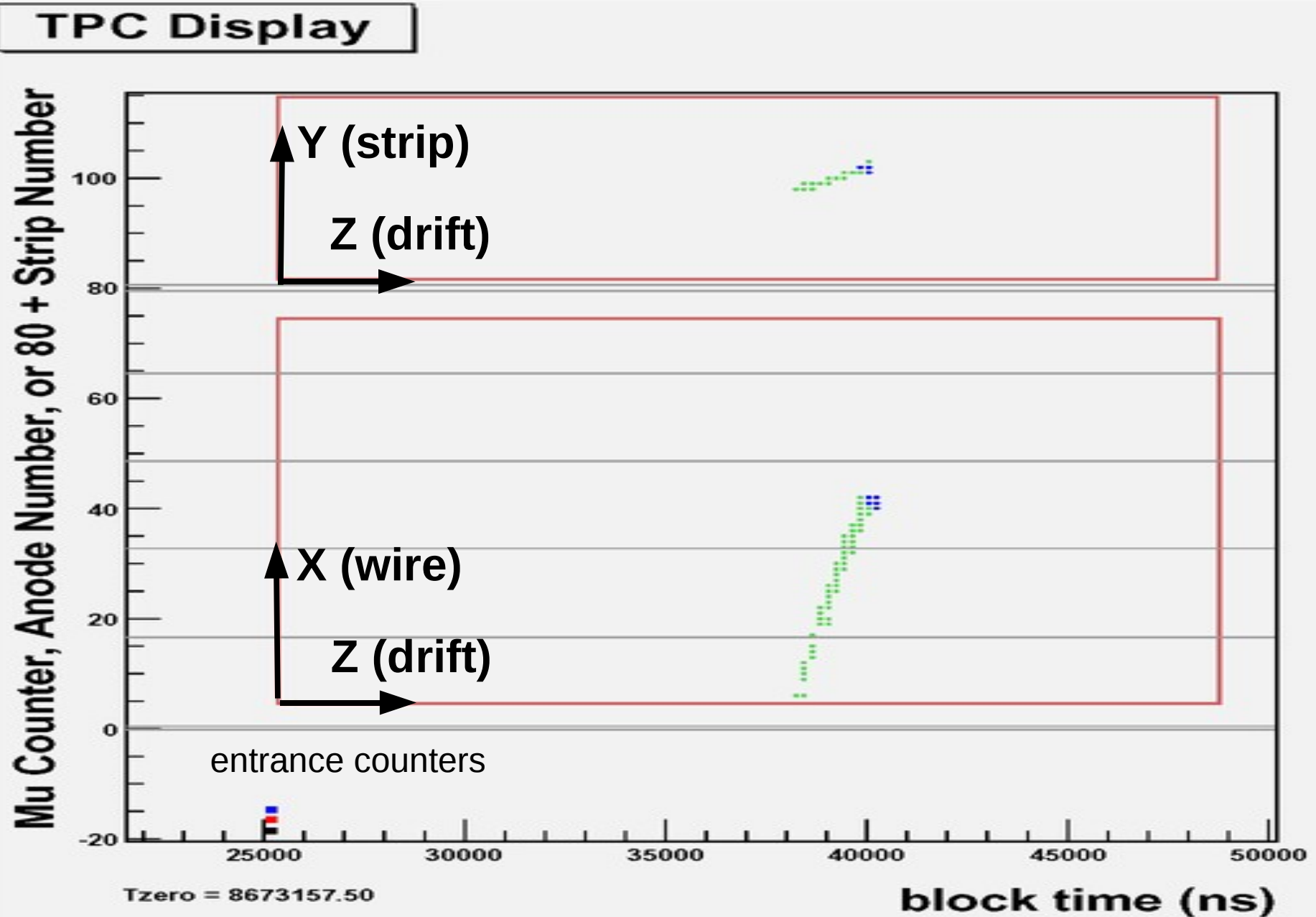


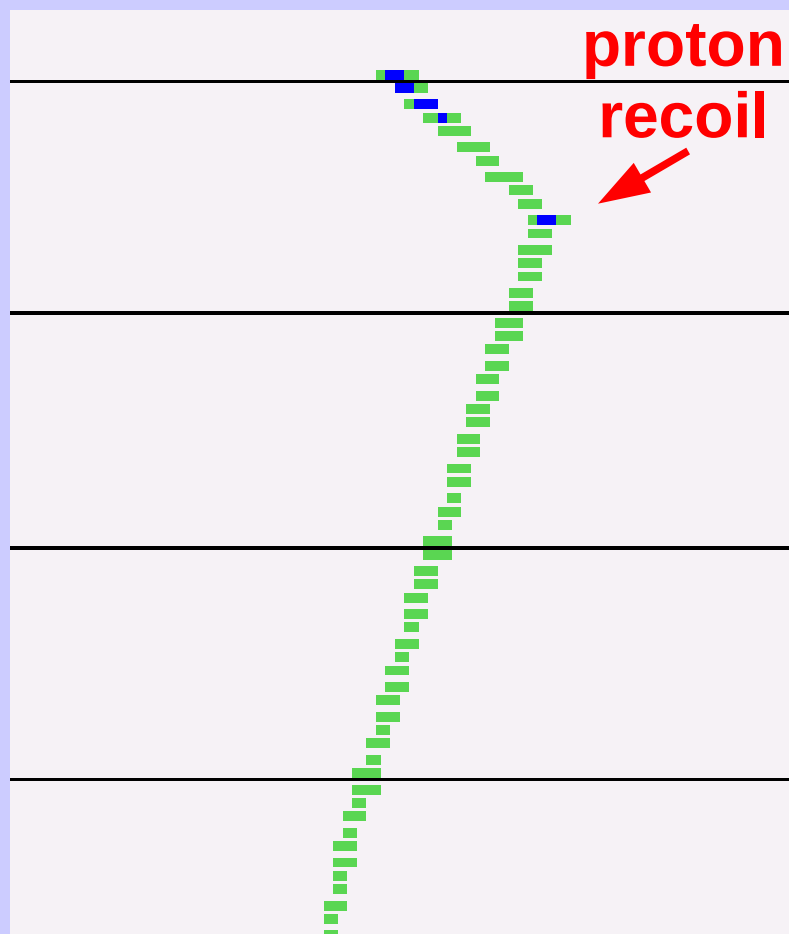
# MuCap TPC



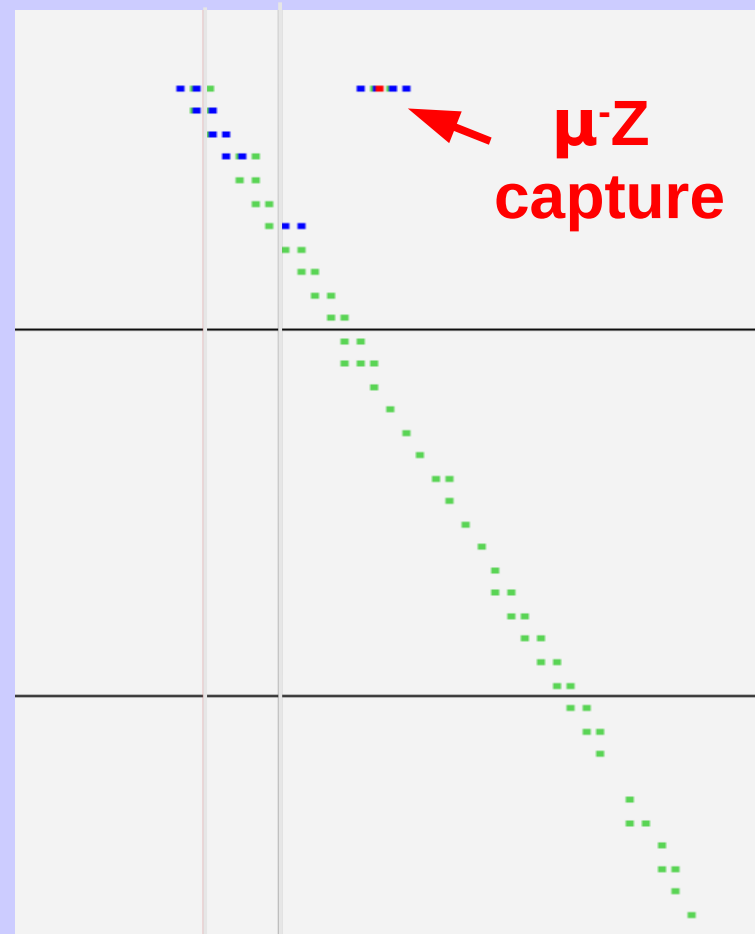


# Event display of $\mu$ stop in $\text{H}_2$ gas

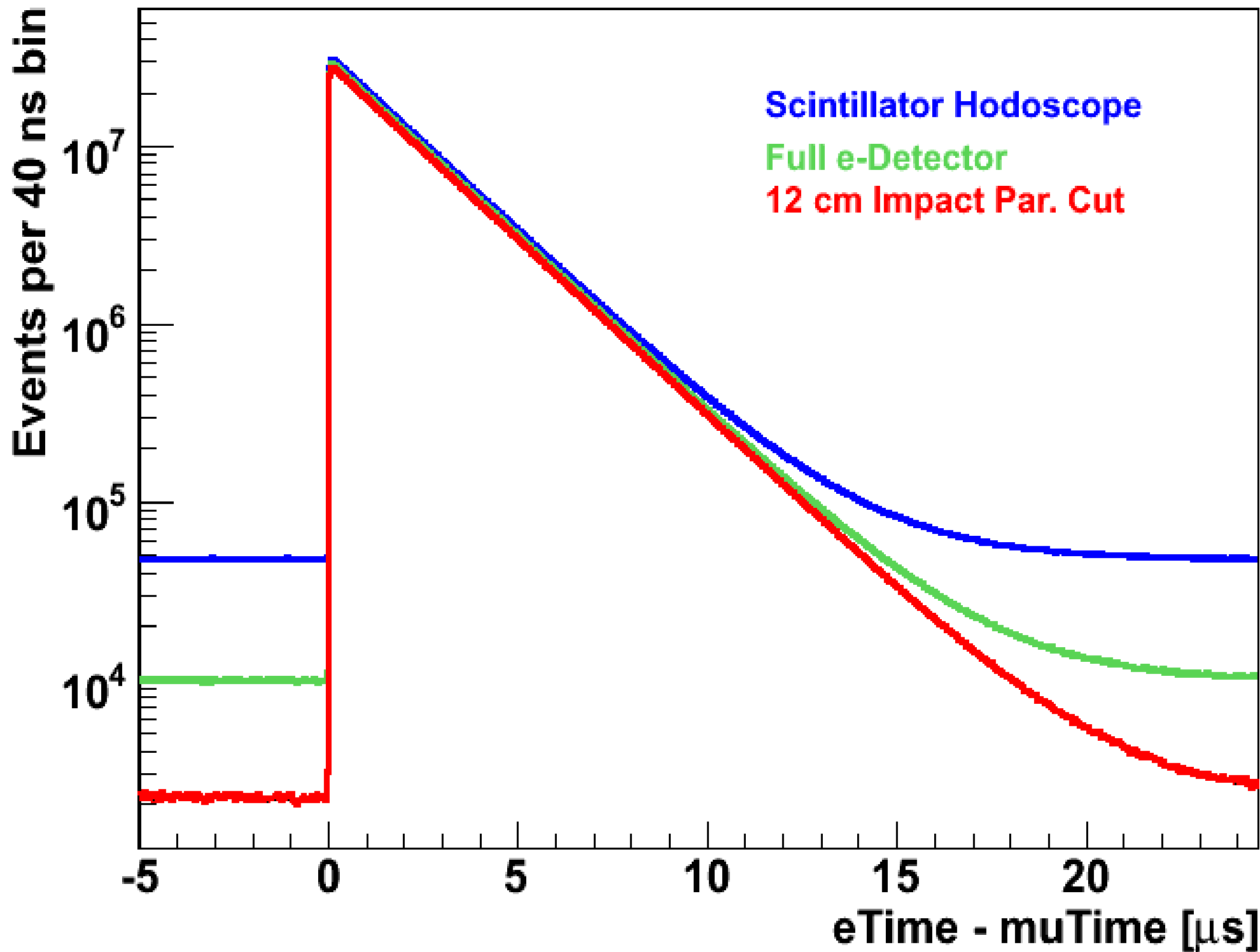




Rare  $\mu$  scatter



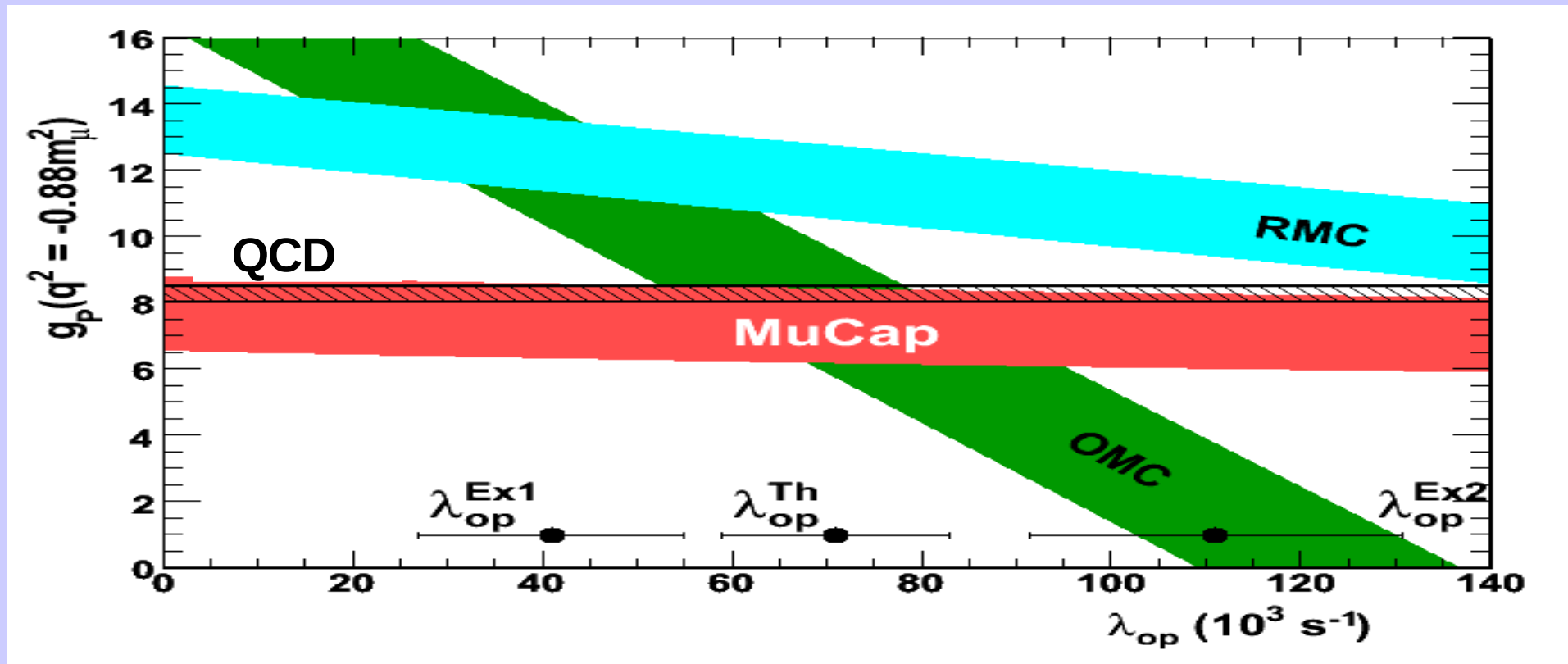
Rare  $\mu$  transfer




# MuCap Results

$$2005: \Lambda_s = 725.0 \pm 13.7(\text{stat}) \pm 10.7(\text{syst}) \text{ s}^{-1}$$

$$g_p(q^2 = -0.88 \text{ m}_\mu^2) = 7.3 \pm 1.1$$



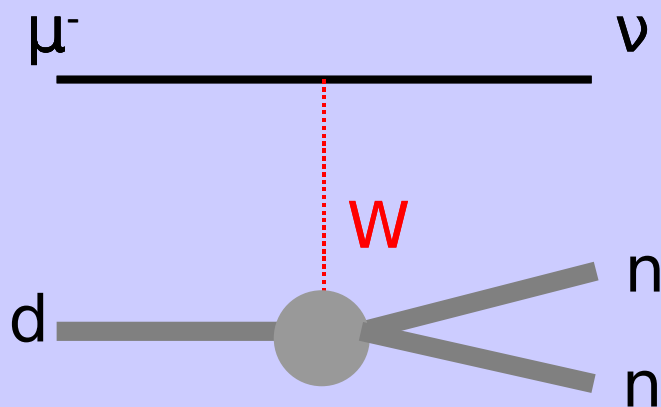
goal for 2006/2007 dataset is  $\Lambda_s$  to  $\pm 5 \text{ s}^{-1}$



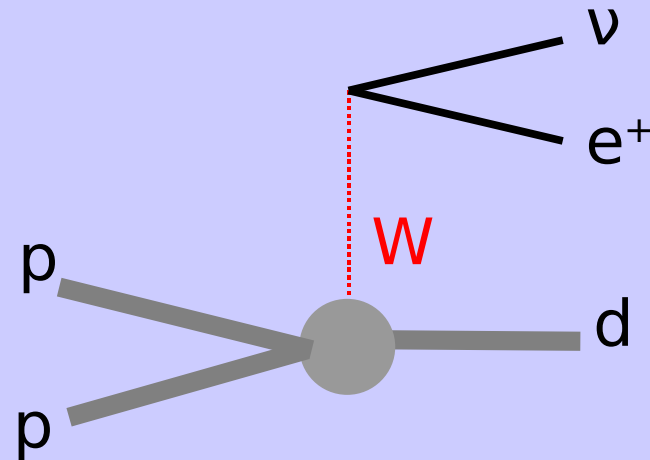
MuSun - the  $\mu$ -d lifetime,  
elementary weak nuclear interaction,  
and solar hydrogen burning.

# Why we measure $\tau_{\mu d}$ ?

muon capture,  
 $\mu^- d \rightarrow \nu n n$



pp fusion,  
 $pp \rightarrow d e^+ \nu$



knowing  $g_v$ ,  $g_a$ ,  $g_m$  and  $g_p$ ,  
the **deuteron wavefunction** and **NN interaction**,  
measure the poorly known  $\mu^- d$  capture rate and  
determine the poorly known **two-nucleon weak axial current**.



# Why we determine $\Lambda_d$ ?

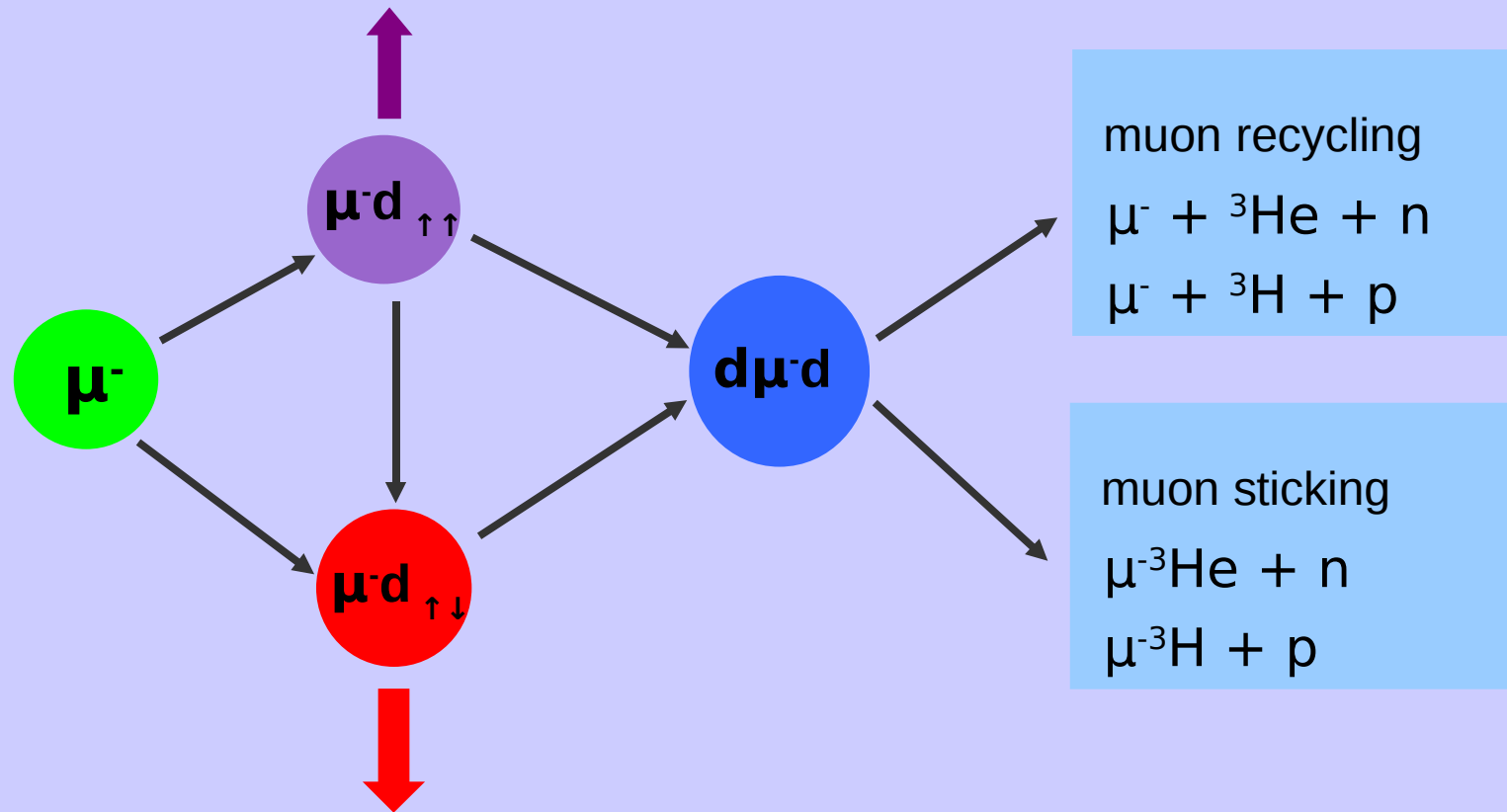
two-nucleon weak nuclear interaction where precision measurement and precision calculation are both possible.

determine the contribution of two-nucleon axial current.

relation of  $\mu^-d$  capture to other weak processes of intense interest in solar physics (pp fusion) and neutrino physics ( $\nu d$  interactions).

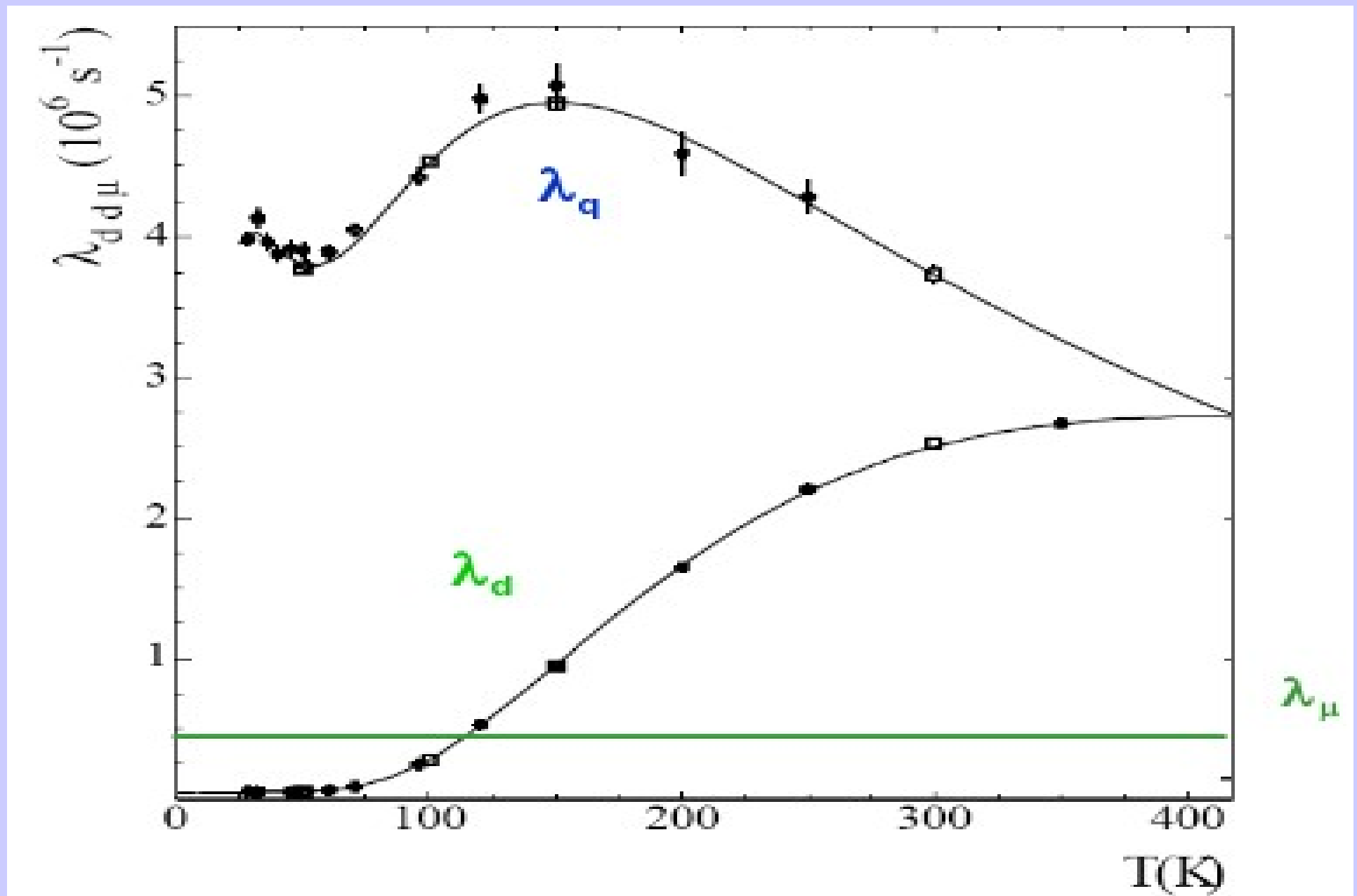
goal of  $\pm 1.5\%$  measurement of capture rate  $\Lambda_d$  is five-fold improvement over existing measurements of  $470 \pm 29 \text{ s}^{-1}$  (Bardin et al.) and  $409 \pm 40 \text{ s}^{-1}$  (Cargnelli et al.).

# $\mu$ chemistry, a complication

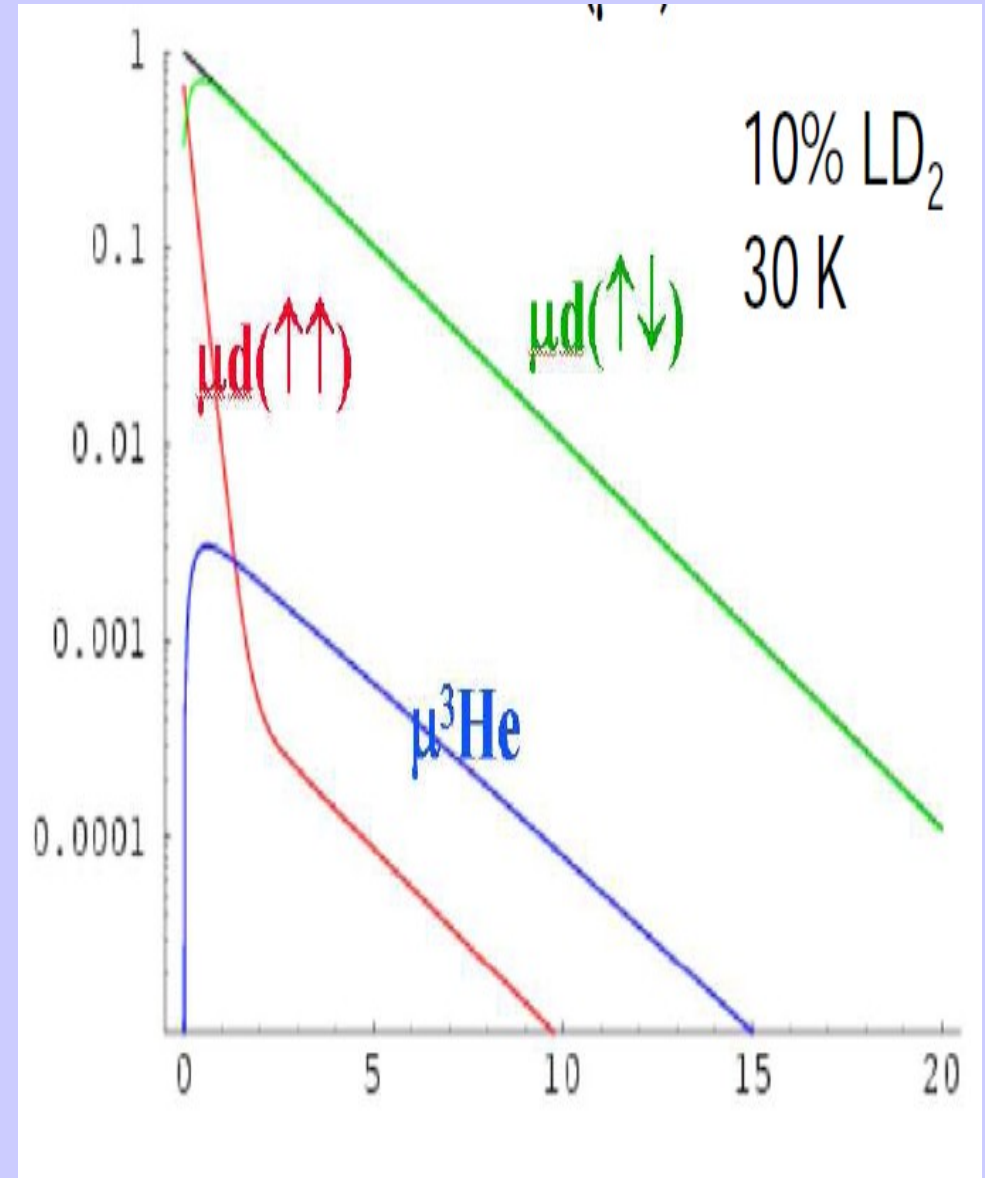
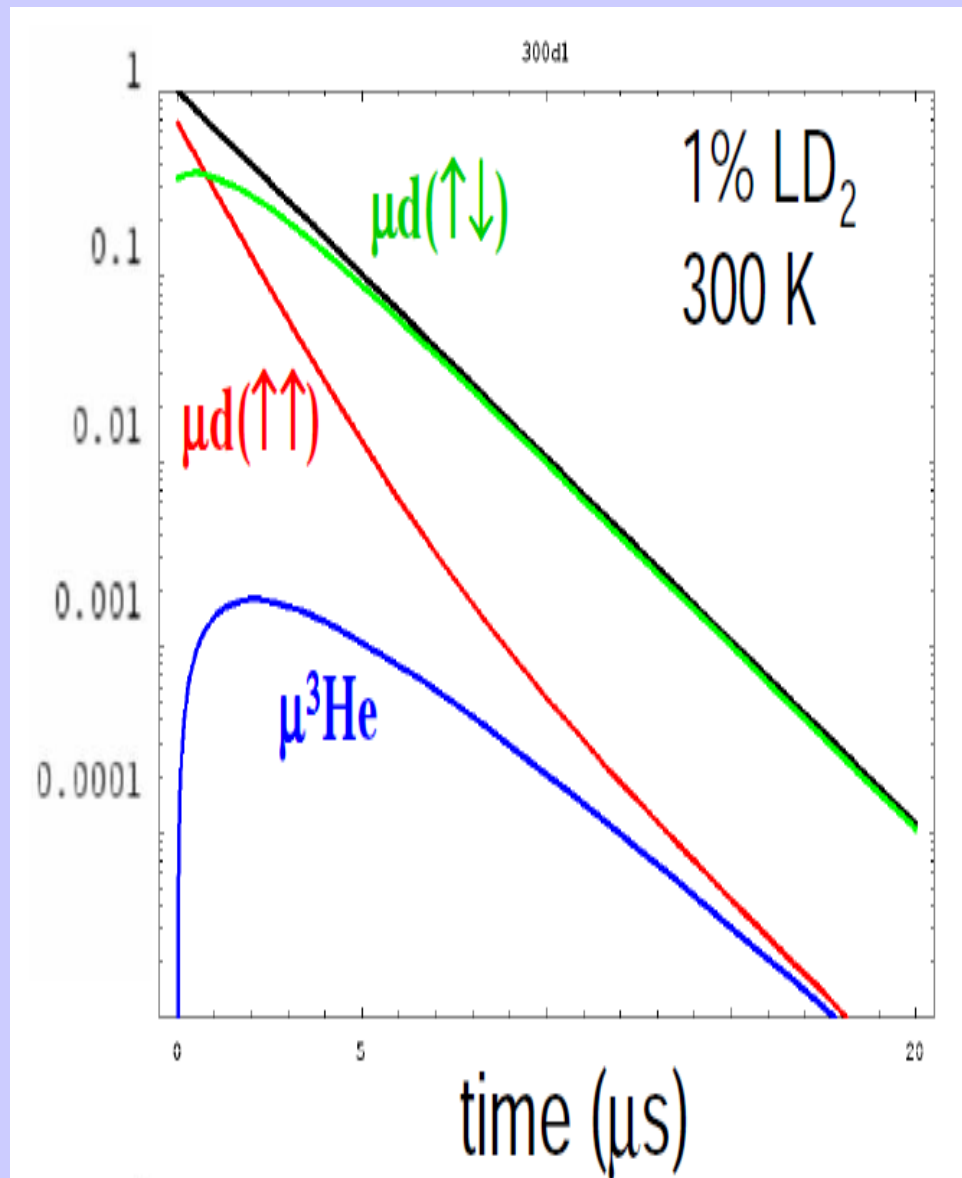


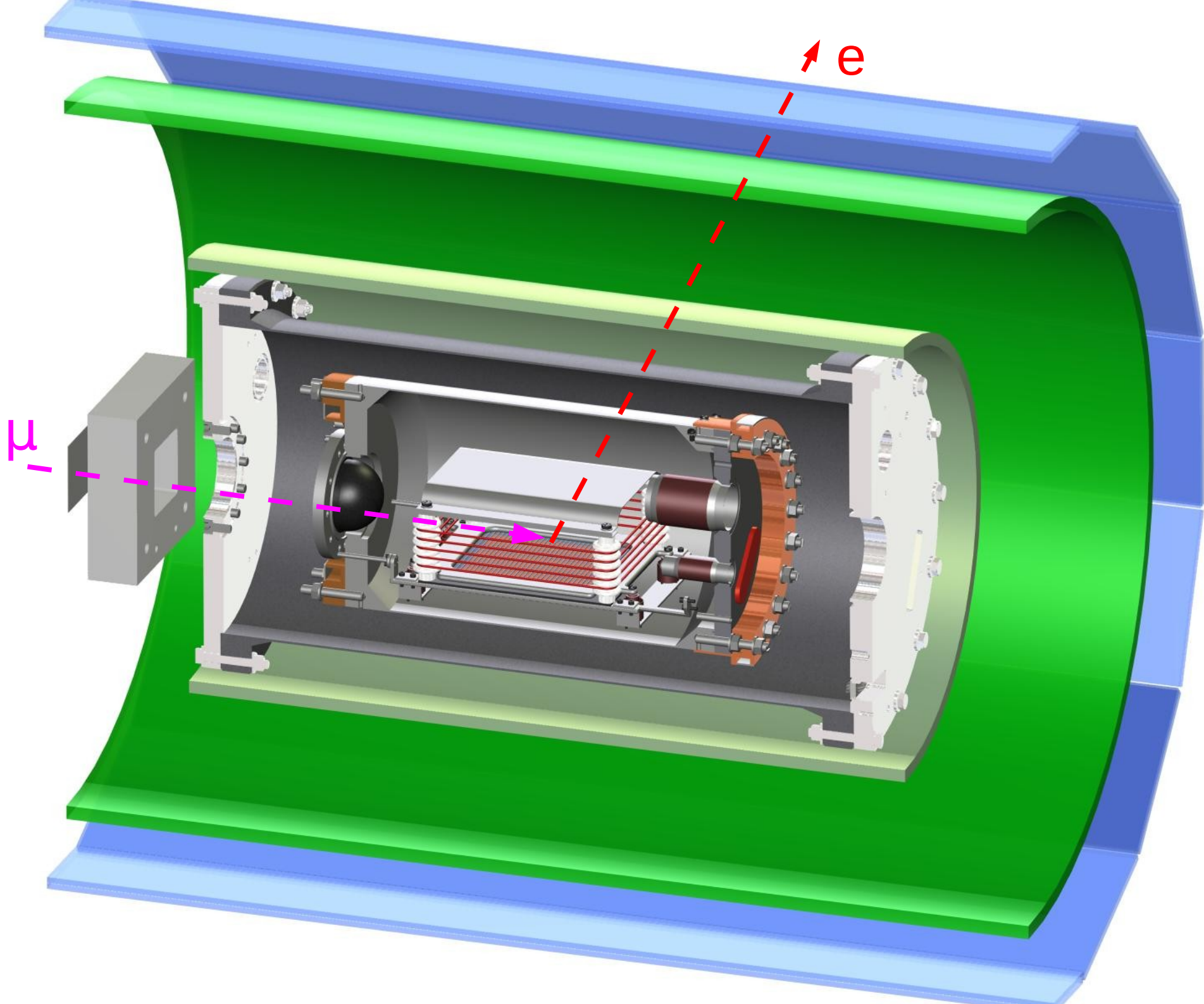
**use ultra-pure (chemically, isotopically)  
30 Kelvin, 5% liquid density  $D_2$  gas**

temperature dependence of  $d\mu d$  formation.



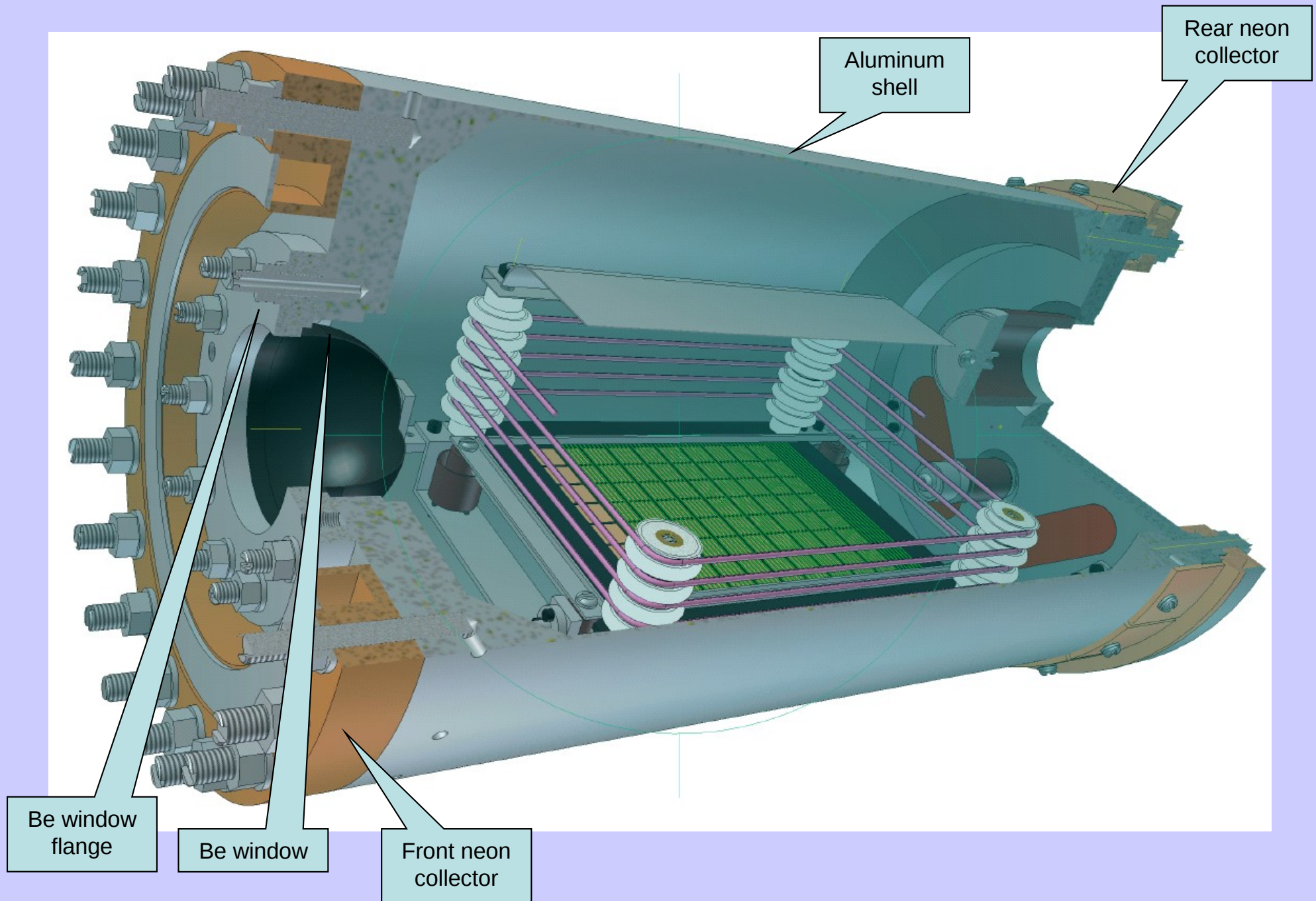
# Relative populations of doublet atoms, quadruplet atoms, $\mu^3\text{He}$ atoms in warm/cold gas







# Cryogenic TPC



# Conclusions

MuX experiments - precision measurements of positive muon, muonic hydrogen, muonic deuterium lifetimes addressing fundamental leptonic, nucleonic and nuclear weak interactions.

MuLan experiment -  $\tau_\mu = 2196980.1 \pm 2.5(\text{stat}) \pm 1.2(\text{syst}) \text{ ps}$  [2006],  $\tau_\mu = 2196980.7 \pm 3.7(\text{stat}) \pm 1.2(\text{syst}) \text{ ps}$  [2007],  $G_F = 1.166\,381\,8\,(7) \times 10^{-5} \text{ GeV}^{-2}$  - a twenty-fold improvement over earlier experiments.

MuCap experiment -  $\Lambda_s = 725.0 \pm 13.7(\text{stat}) \pm 10.7(\text{syst}) \text{ s}^{-1}$ ,  $g_p(q^2 = -0.88 \text{ m}_\mu^2) = 7.3 \pm 1.1$  - with goal of reaching  $\pm 5 \text{ s}^{-1}$ .

MuSun experiment - **goal of  $\Lambda_s$  to  $\pm 1.5\%$**  - recent milestone of operation of 3K, 5% LD<sub>2</sub> cryo-TPC



# Extras

# Relation to Standard Model

$$\sqrt{4\pi\alpha} = g g' / \sqrt{g^2 + g'^2}$$

$$G_F = \sqrt{2}/v^2$$

$$M_Z = \sqrt{g^2 + g'^2} v$$

→ exacting tests of standard model  
by precision measurements of  $\theta_w$ ,  $M_w$ , ...

# Detection of $\mu$ stops in $\text{H}_2$ gas

