

# **Consistent analysis of NCE and CCQE (anti)neutrino scattering off carbon**

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# Outline

## ① Introduction

- Motivation: the NOMAD-MiniBooNE difference
- Description of the approach

## ② NCE and CCQE (anti)neutrino scattering

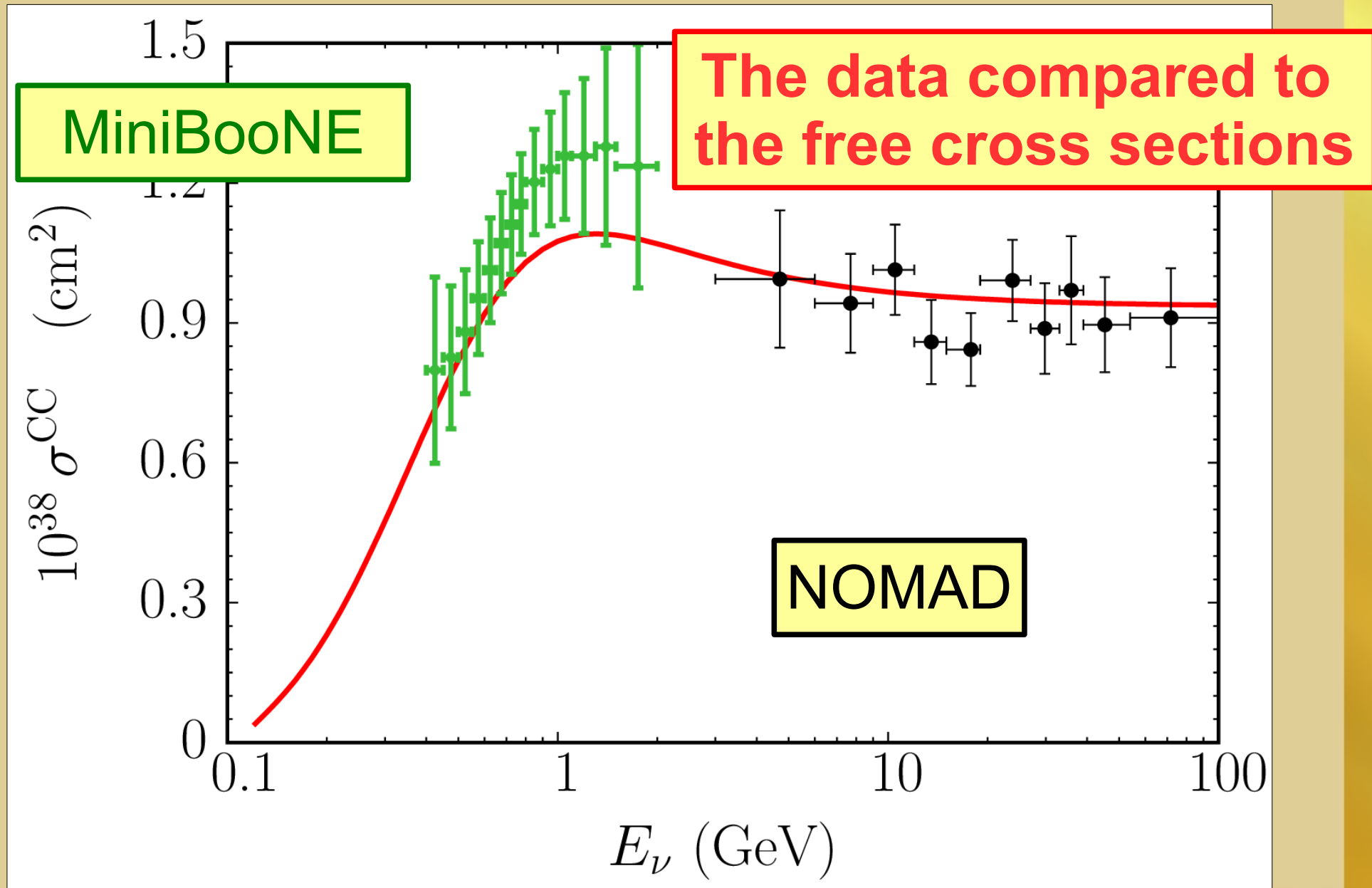
- NOMAD, Lyubushkin *et al.*, EPJ C **63**, 355 (2009)
- MINER $\nu$ A, Fields *et al.*, arXiv:1305.2234, Fiorentini *et al.*, arXiv:1305.2243
- BNL E734, Ahrens *et al.*, PRD **35**, 785 (1987)
- MiniBooNE, Aguilar-Arevalo *et al.*, PRD **81**, 092005 (2010), PRD **82**, 092005 (2010), arXiv:1301.7067

## ③ What are the features of the MiniBooNE-NOMAD difference?

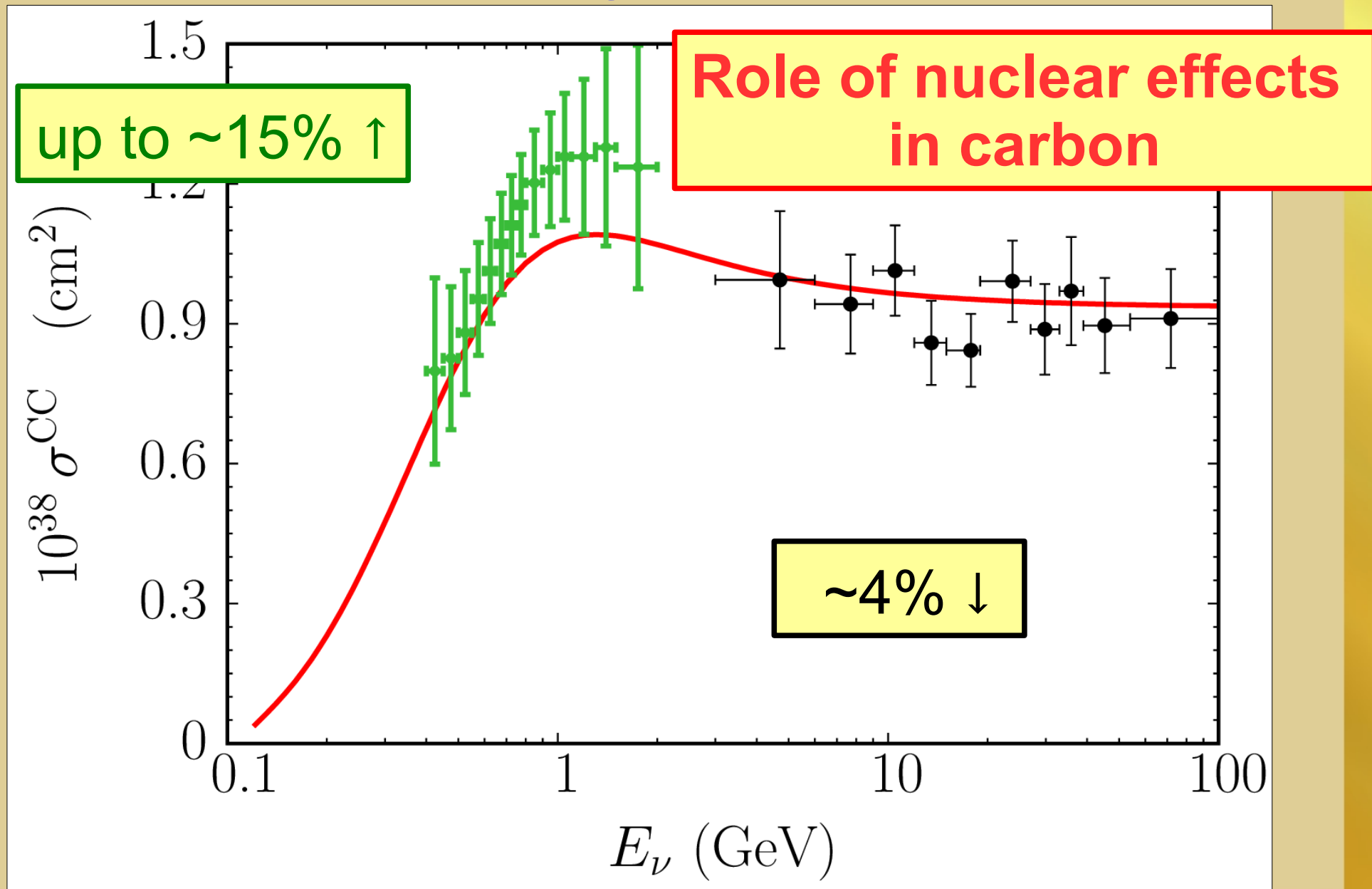
## ④ Summary

**Motivation**

# Available CCQE neutrino data



# Available CCQE neutrino data



# Available CCQE neutrino data

## MiniBooNE

- Cherenkov detector
- CCQE = no pions observed
- 146 070 events (193 709 events) in neutrino mode
- flux from MC simulation, involving extrapolation to the target 35 times thicker
- average energy of **788 MeV**

## NOMAD

- drift-chamber detector
- CCQE = muon only or muon + proton of kin. energy  $> 47$  MeV
- 14 021 events in neutrino mode
- normalization from the total inclusive CC cross section and from inverse muon decay
- average energy of **25.9 GeV** (CCQE events only)

# Do the two kinematics differ significantly?

For a neutrino energy of **100 GeV**, **89.8 (97.5)%** of the CCQE cross section comes from the momentum transfer range allowed for neutrino of  **$E = 1 (2)$  GeV**.

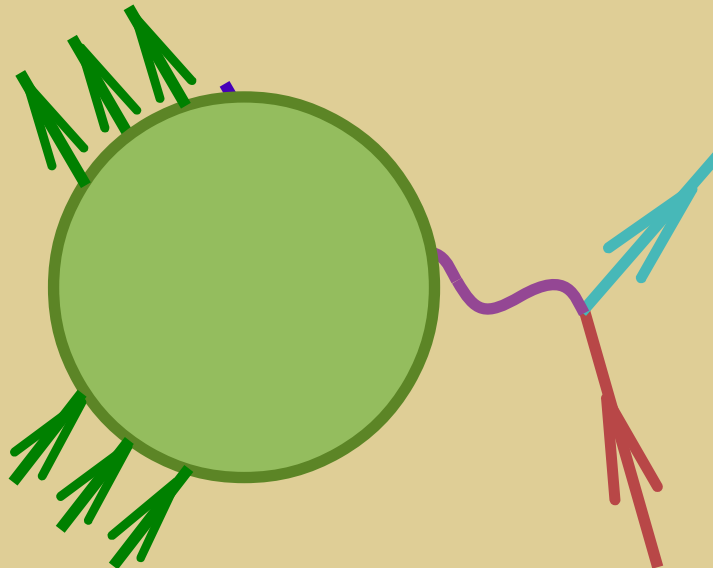
Therefore, in the context of CCQE interactions, the NOMAD and MiniBooNE experiments probe a **similar region of the  $(\omega, |\mathbf{q}|)$  plane**.

**Approach**



# Impulse approximation (IA)

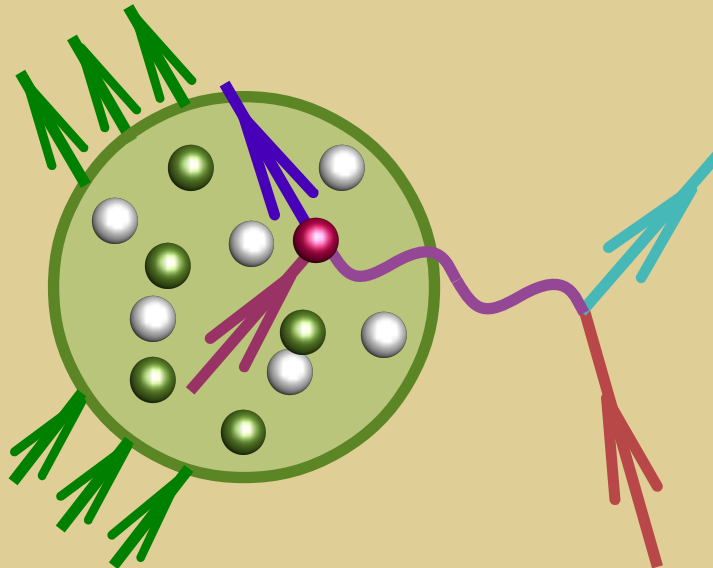
Assumption: the dominant process of neutrino-nucleus interaction is **scattering off a single nucleon**, the remaining nucleons act as a spectator system.



# Impulse approximation (IA)

Assumption: the dominant process of neutrino-nucleus interaction is **scattering off a single nucleon**, the remaining nucleons act as a spectator system.

It is valid when the momentum transfer  $|\mathbf{q}|$  is high enough, as the probe's spatial resolution is  $\sim 1/|\mathbf{q}|$ .



# Impulse approximation (IA)

In the IA regime, the neutrino-nucleus cross section is equal to the **elementary off-shell cross section** for neutrino scattering off a moving nucleon **averaged over the momentum and energy distribution of nucleons**.

This distribution is called **the spectral function (SF)**.

For neutral current elastic (NCE) interaction,

$$\frac{d\sigma_{\nu A}^{\text{NC}}}{dQ^2} = \sum_{N=p, n} \int d^3p dE P_{\text{hole}}^N(\mathbf{p}, E) \frac{d\sigma_{\nu N}^{\text{NC}}}{dQ^2}$$

# Spectral function (SF)

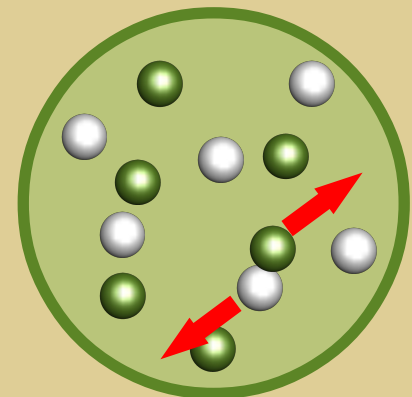
The realistic SFs of various nuclei have been obtained by Benhar *et al.* [NPA 579, 493 (1994)] in the **local-density approximation**, combining

- the shell structure from the Saclay  $(e,e'p)$  data
- the correlation contribution from theoretical calculations for uniform nuclear matter at different densities

# Spectral function (SF)

In short, in the carbon nucleus

- ~80% of nucleons occupy the **s and p shells**
- ~20% of nucleons are **deeply bound** due to strong short-range correlations creating **NN pairs of high relative momentum**  
(2-nucleon final states in the absence of reinteractions)



# Effects beyond the IA

In scattering off bound nucleons, the **effective  $M_A=1.23$  GeV** is applied to account for **multinucleon reaction mechanisms** (e.g. involving MEC).

This method seems to be justified in the kinematical setup of MiniBooNE by the results of Nieves *et al.* [PLB **707**, 72 (2012)] for the double diff. cross section.

The value of  $M_A$  is motivated by the result of the MiniBooNE Collaboration, obtained from the first shape analysis of the  $Q^2$  distribution of the **largest statistics of CCQE events collected to date** [PRL 100, 032301 (2008)].

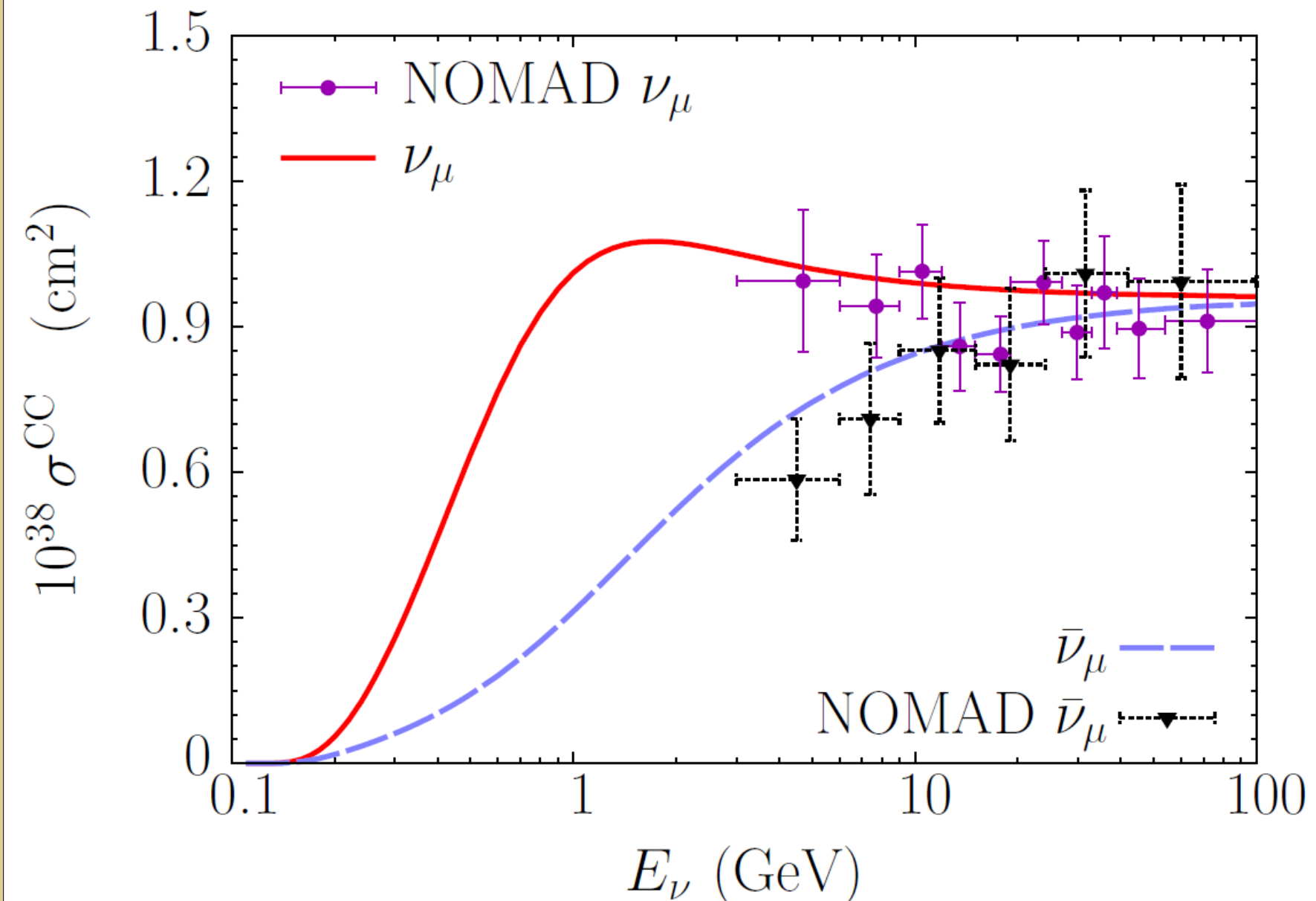
# NCE vs. CCQE

NCE	CCQE
both $n$ 's and $p$ 's contribute	only $\nu n$ and $\bar{\nu} p$
$G_F$	$G_F \cos \theta_C$
$E_{k'} =  \mathbf{k}' $	$E_{k'} = \sqrt{m'^2 + \mathbf{k}'^2}$
$\mathcal{F}_i^N = \pm \frac{1}{2}(F_i^p - F_i^n) - 2 \sin^2 \theta_W F_i^N$	$F_i = F_i^p - F_i^n$
$\mathcal{F}_A^N = \frac{1}{2}(F_A^s \pm F_A) = \frac{1}{2} \frac{\Delta s \pm g_A}{(1 - q^2/M_A^2)^2}$	$F_A = \frac{g_A}{(1 - q^2/M_A^2)^2}$

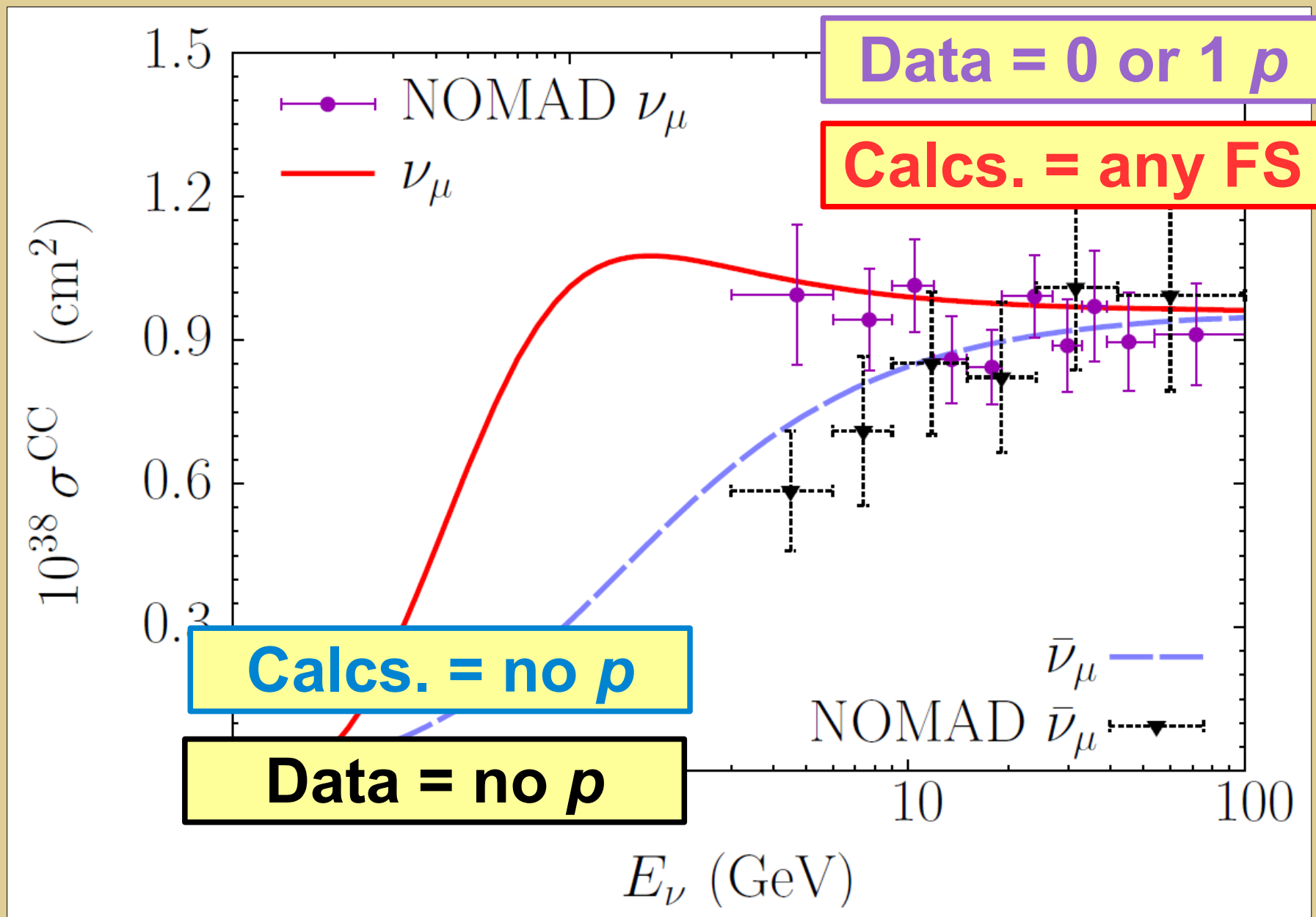
**NOMAD**



# Comparison to the NOMAD data



# Comparison to the NOMAD data

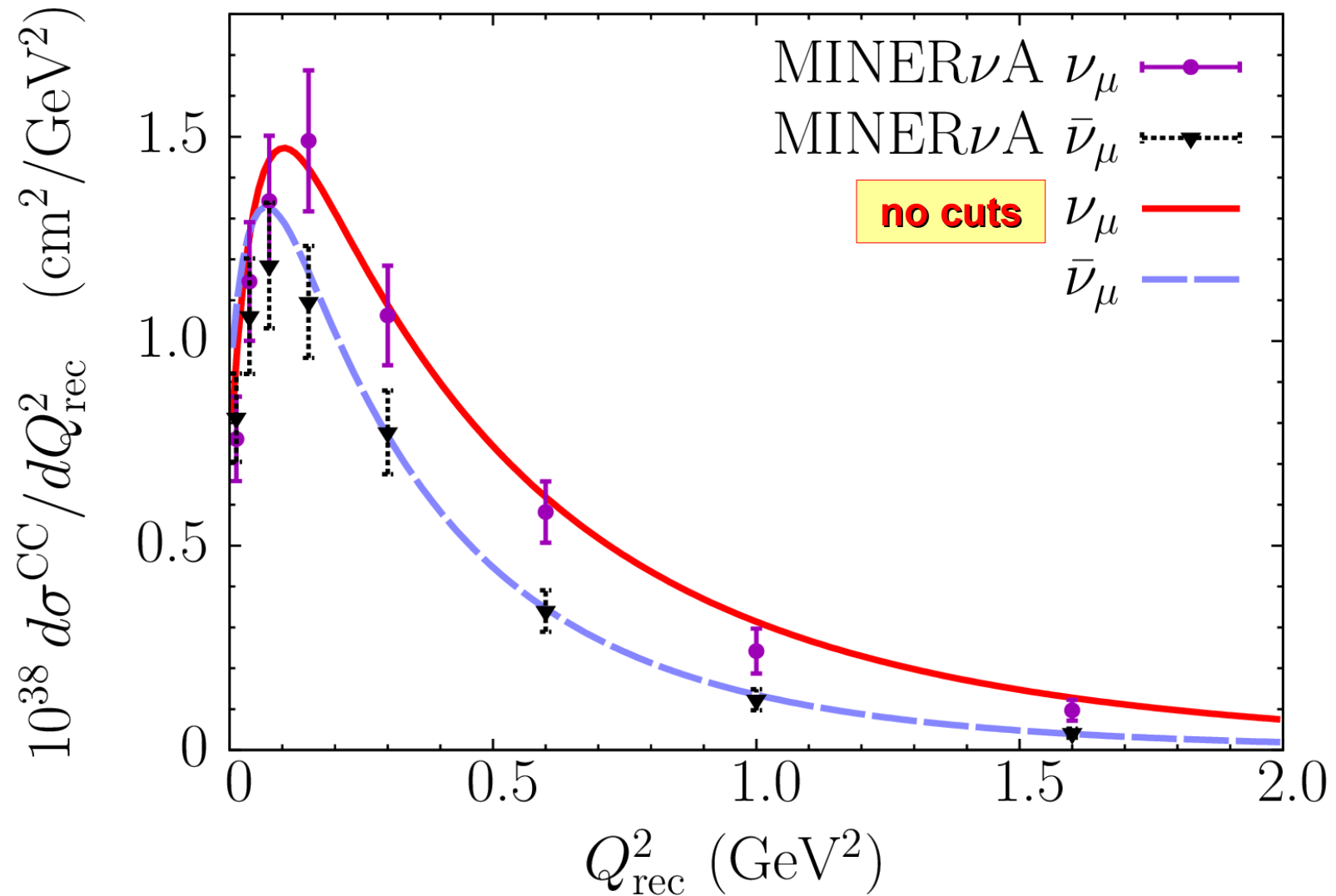


# Comparison to the NOMAD data

- **Good agreement** between the results and the data
- The SF results higher by  $\sim 6\%$  than the NOMAD best fit, to be compared to the  $\sim 8\%$  ( $\sim 11\%$ ) syst. uncertainty of the  $\nu$  ( $\bar{\nu}$ ) data
- The correlated contribution ( $6\%$  for  $|p| > 300$  MeV) would explain the difference for  $\nu$ 's but **not** for  $\bar{\nu}$ 's
- The difference may be related to the overestimated cross section in the low- $Q^2$  region

**MINER<sub>v</sub>A**

# CCQE x-sections from MINER $\nu$ A

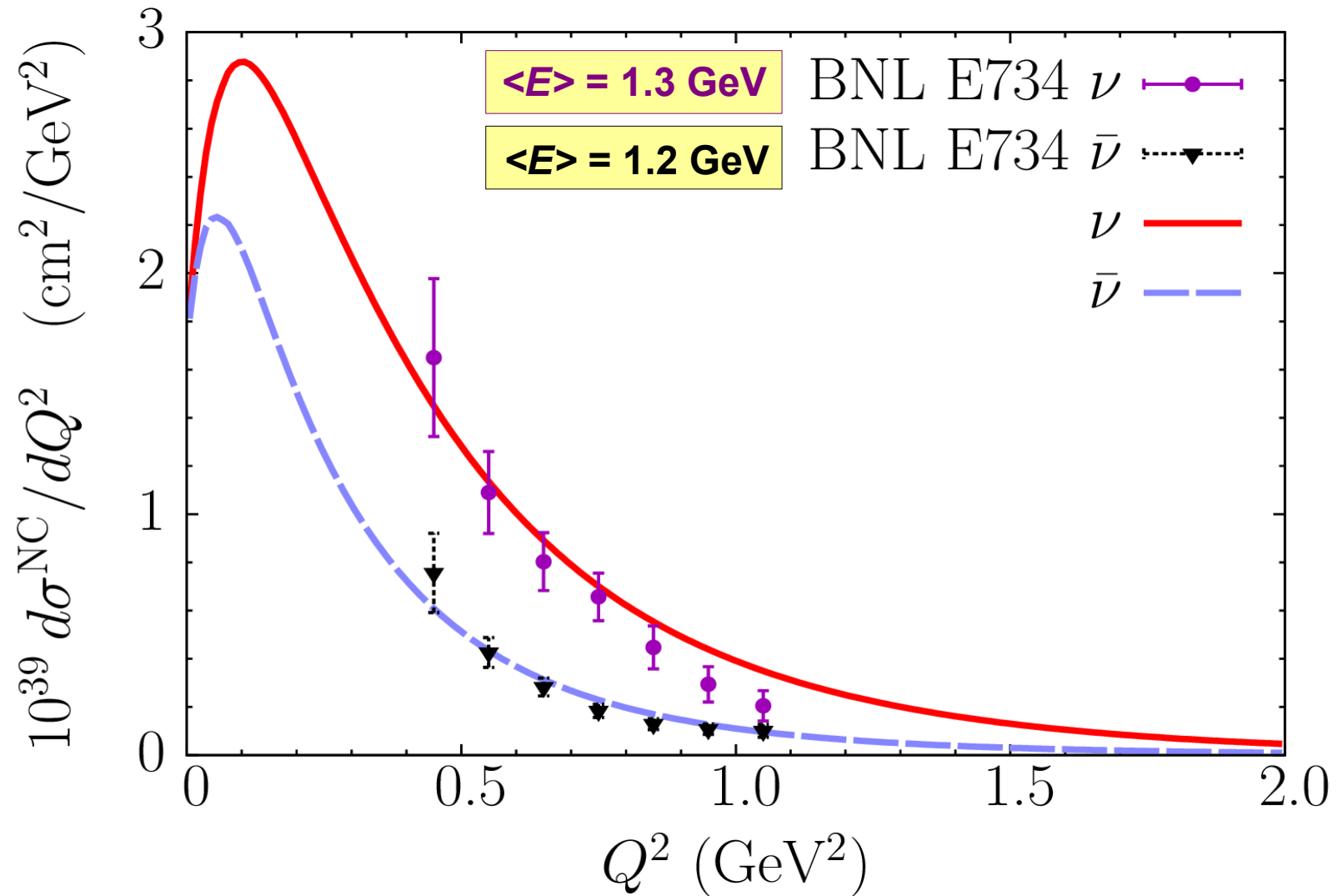


# CCQE x-sections from MINERvA

- Both the shape and the normalization of the data are **well reproduced**
- Better agreement with the  $\bar{\nu}$  data. For neutrinos, the correlated NN contribution ( $\nu_{\mu} + np \rightarrow \mu + pp$ ) **needs to be subtracted** from the calculations.
- In the low- $Q^2$  region, the data are **overestimated**, likely due to the IA breakdown

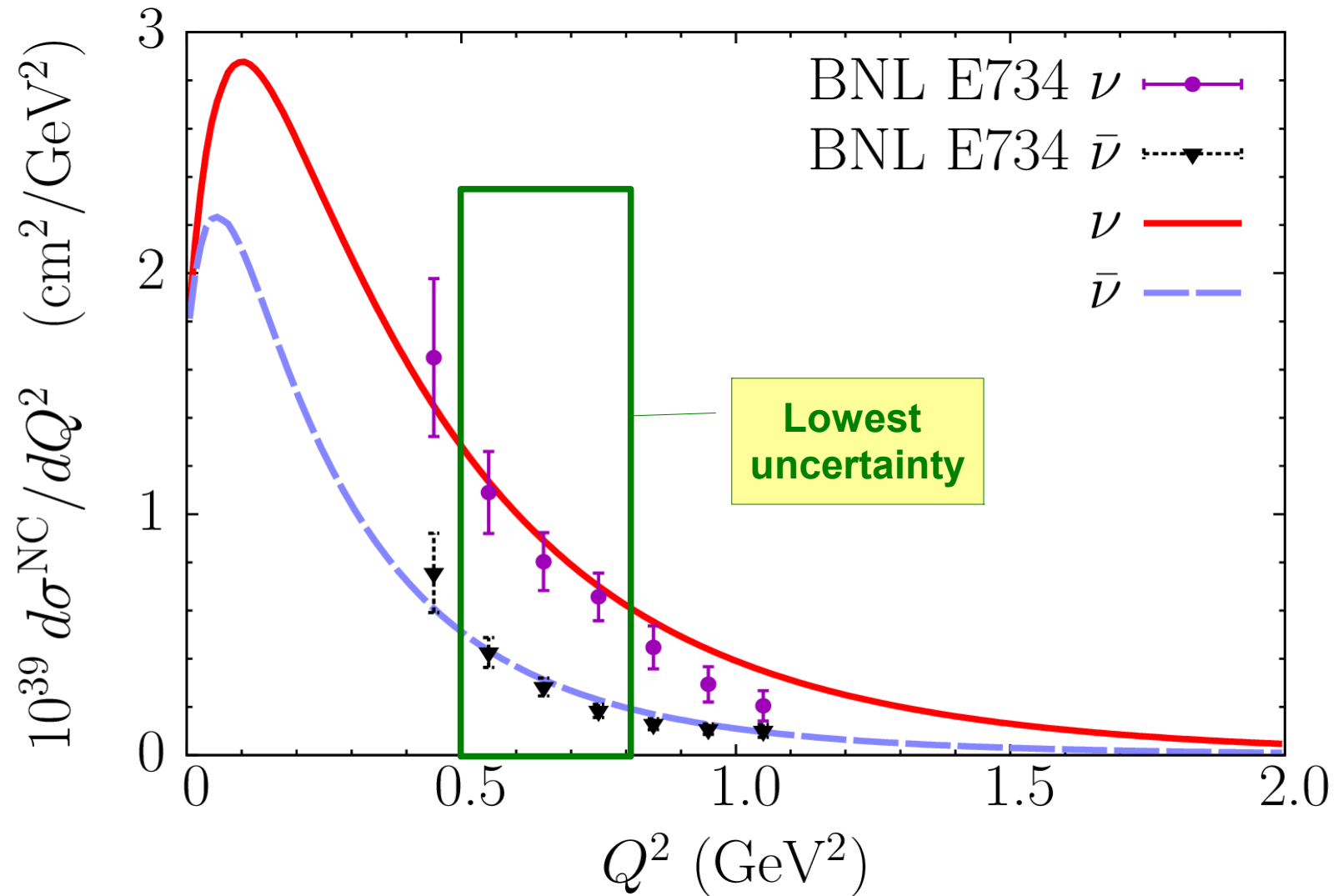
**BNL E734**

# NCE cross sections from BNL E734





# NCE cross sections from BNL E734

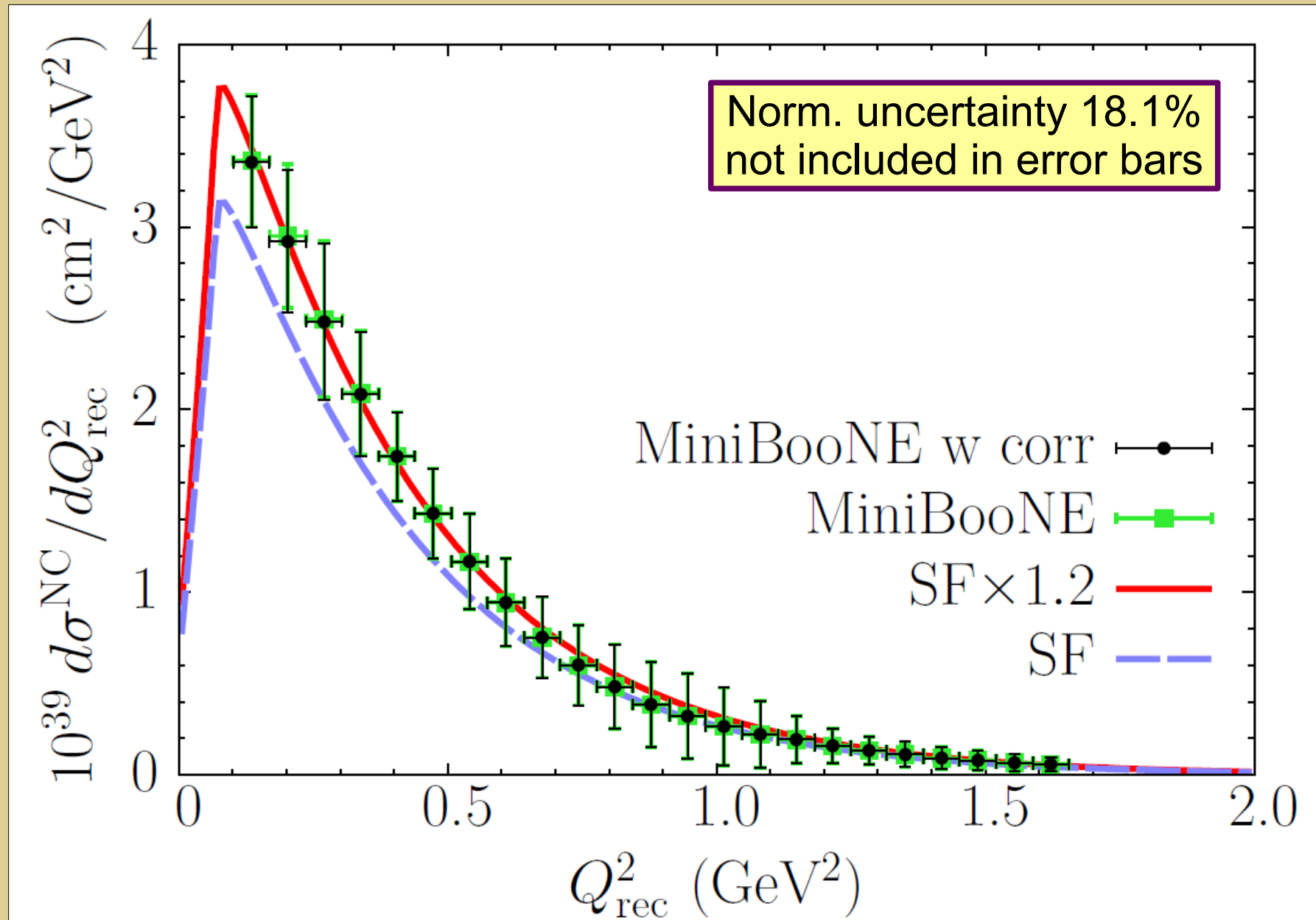


# NCE cross sections from BNL E734

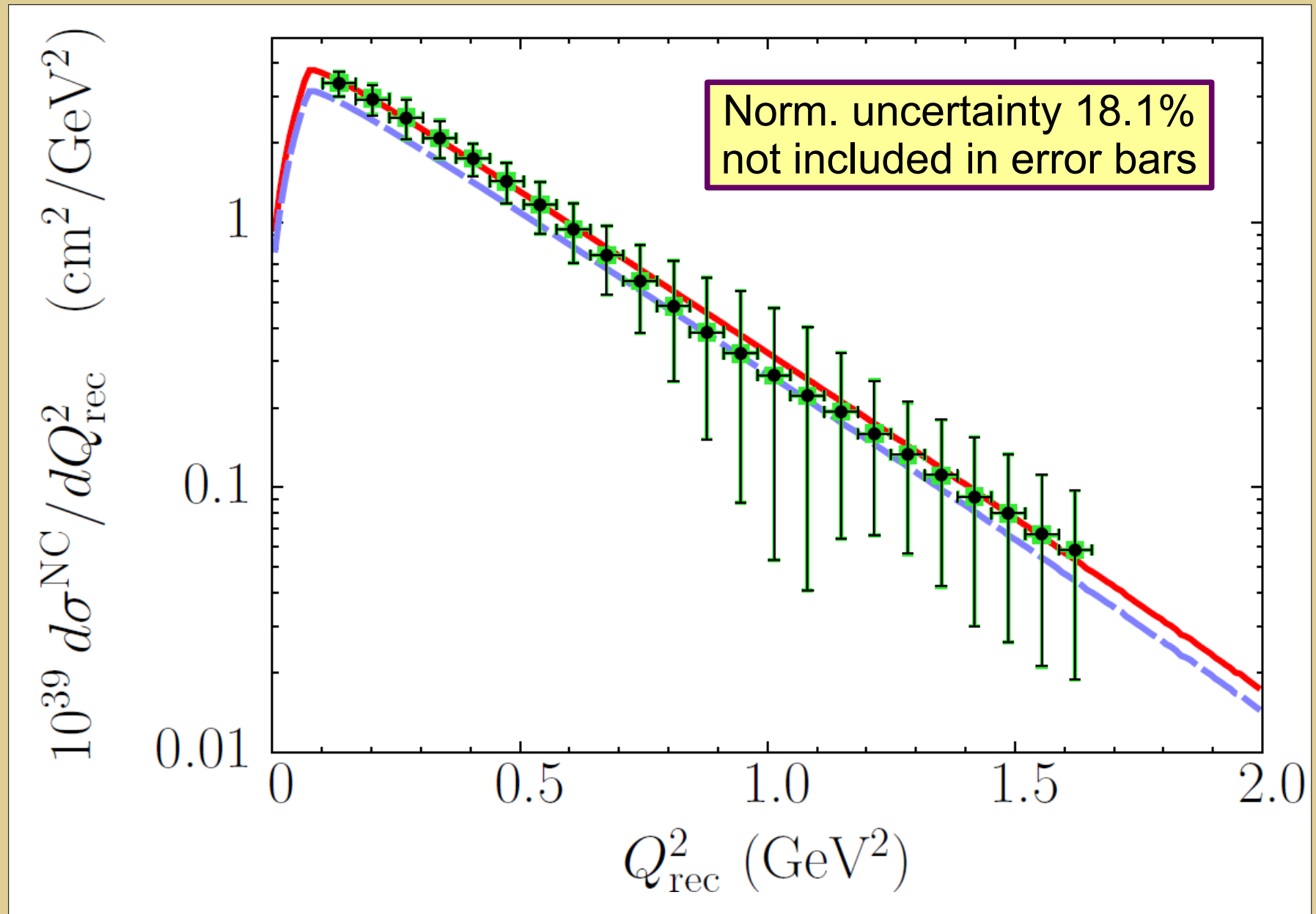
- Overall agreement with the data is **fairly good**
- **Better description** of the lower-uncertainty antineutrino data
- For the neutrino case, the agreement **improves** in the lowest uncertainty region,  $0.5 \leq Q^2 \leq 0.8 \text{ GeV}^2$

**MiniBooNE**

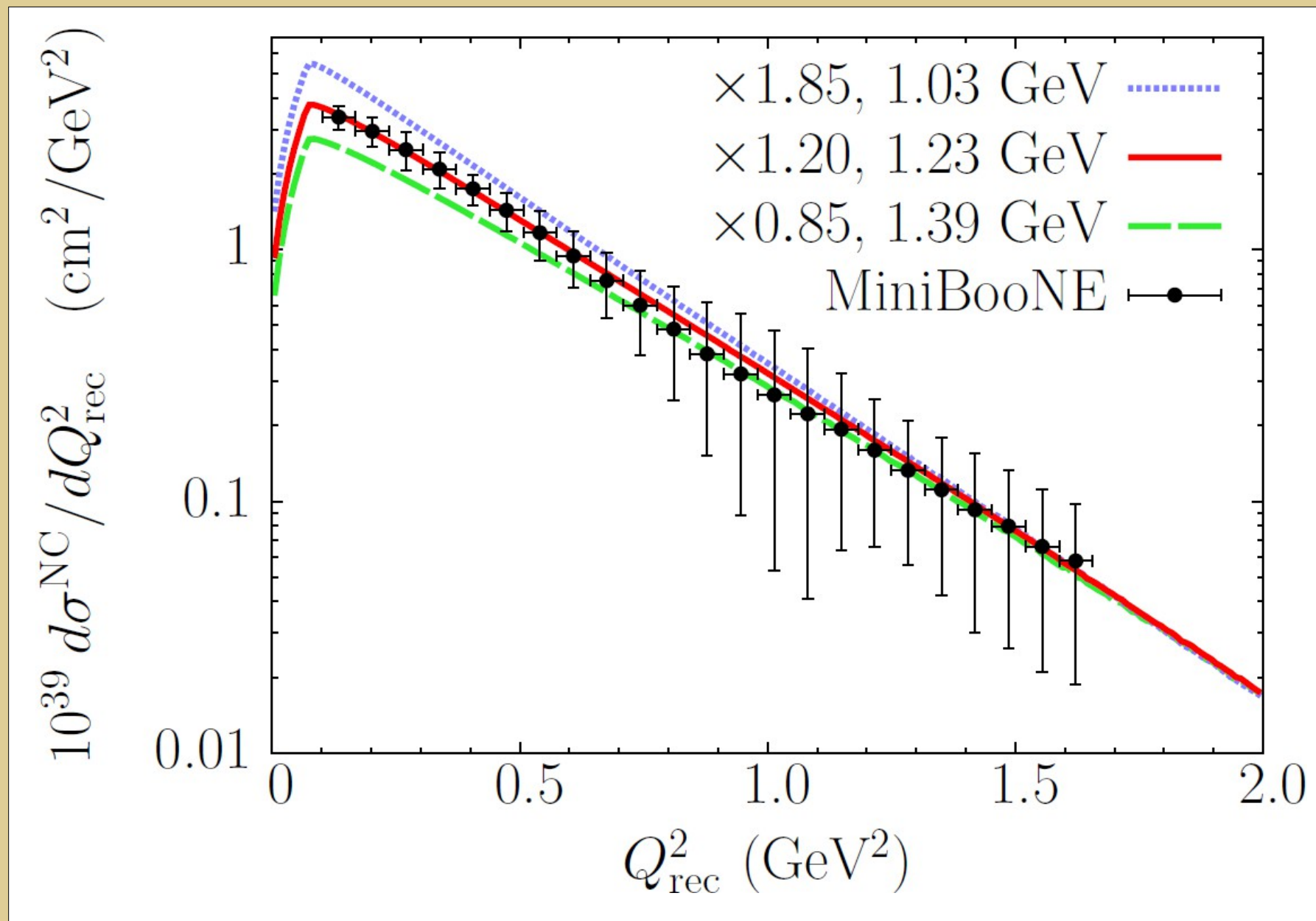
# NCE cross section from MiniBooNE



# NCE cross section from MiniBooNE



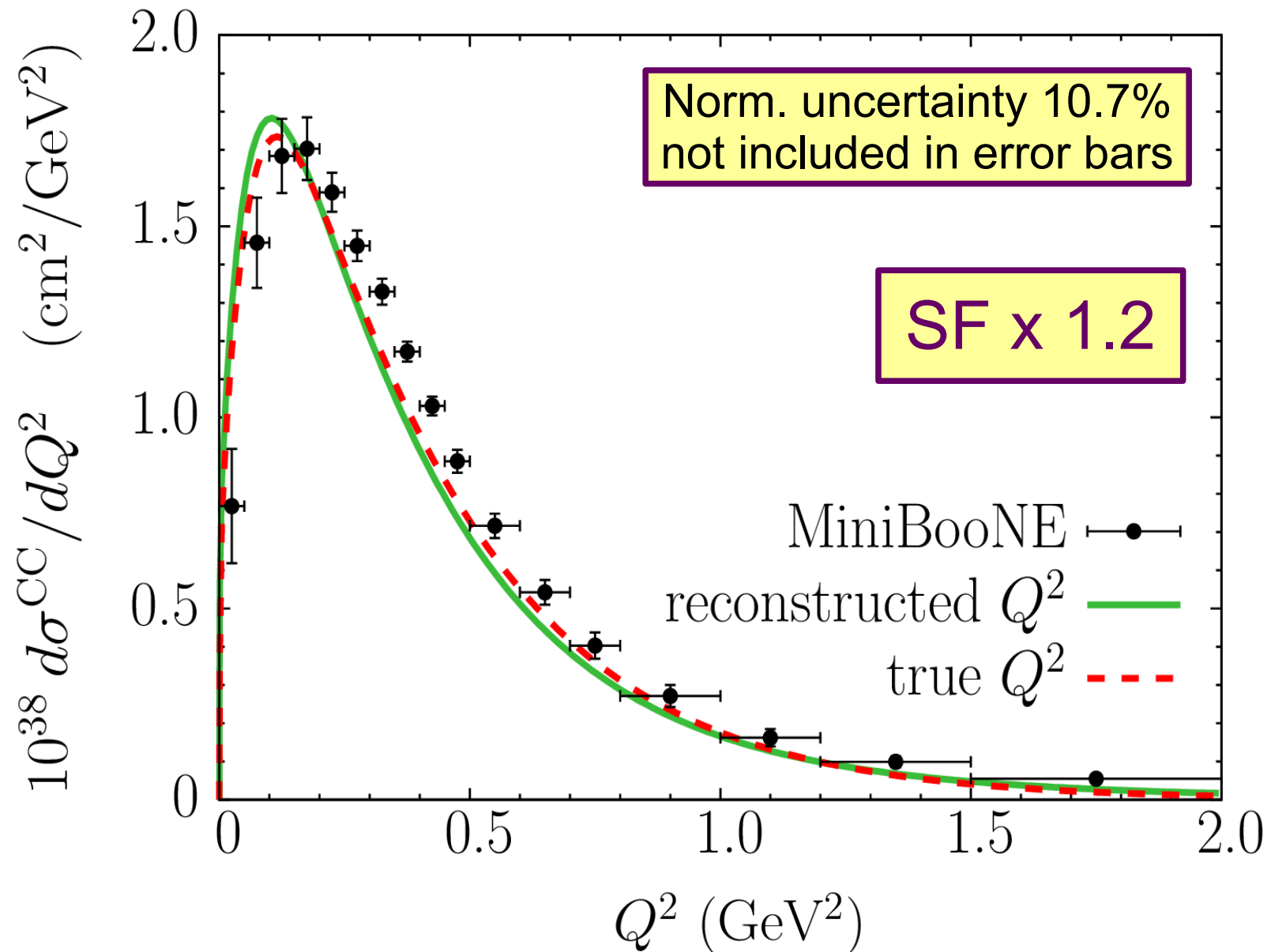
# NCE cross section from MiniBooNE



# NCE cross section from MiniBooNE

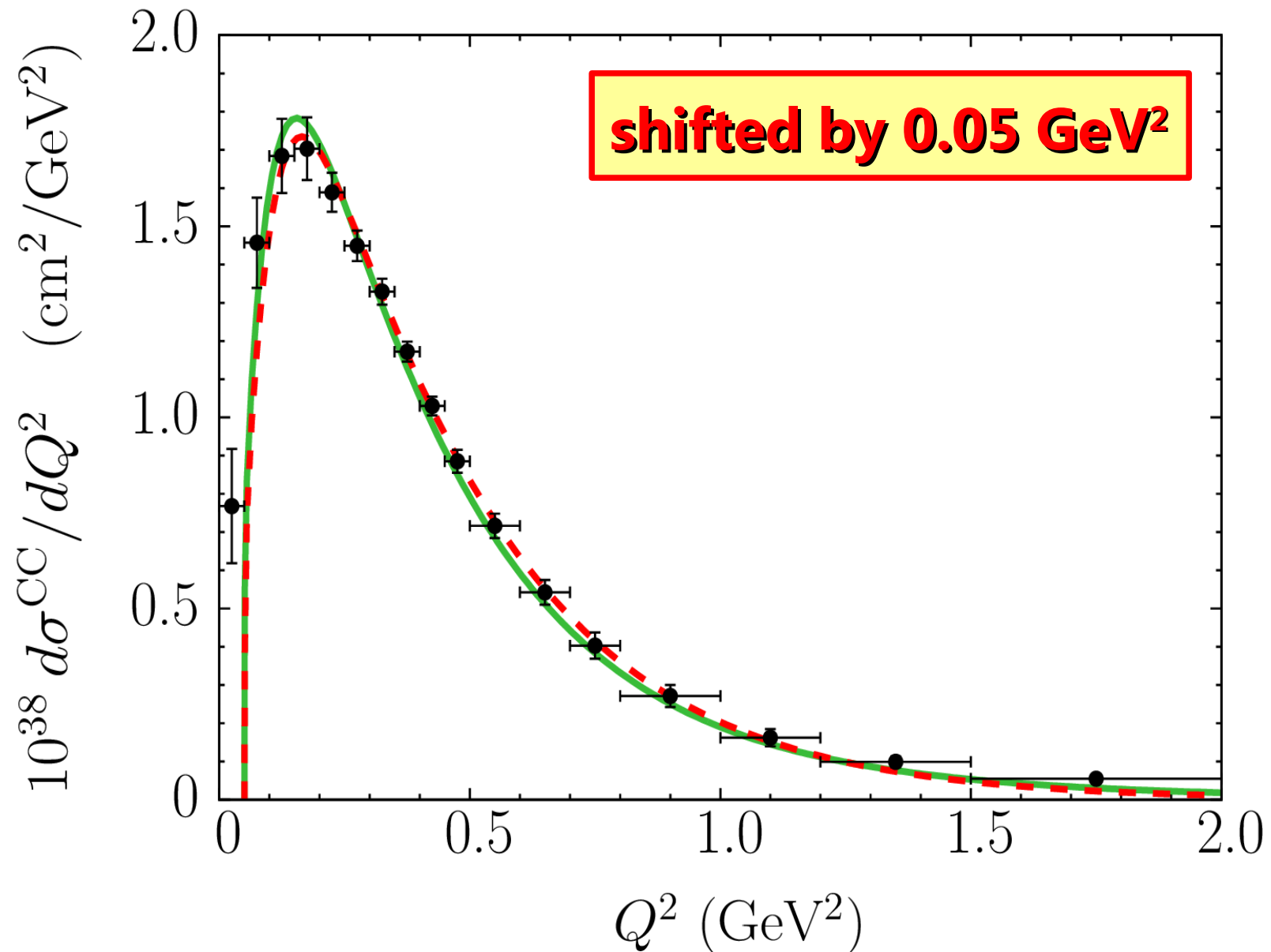
- The calculations fail to reproduce the normalization by **20%** (norm. uncertainty 18.1%  $\rightarrow$  0.84-1.22), consistent with the 1<sup>st</sup> shape analysis of CCQE events (data/MC =  $1.21 \pm 0.24$ ) .
- The shape reproduced **very well**. For  $Q^2 \leq 0.64 \text{ GeV}^2$ , the differences are on average 1.6%. The largest deviations for  $0.8 \leq Q^2 \leq 1.1 \text{ GeV}^2$  remain well within the error bars.
- The slope of the cross section is not consistent with the axial mass **very different** from 1.23 GeV

# CCQE $\nu_\mu$ x-section from MiniBooNE

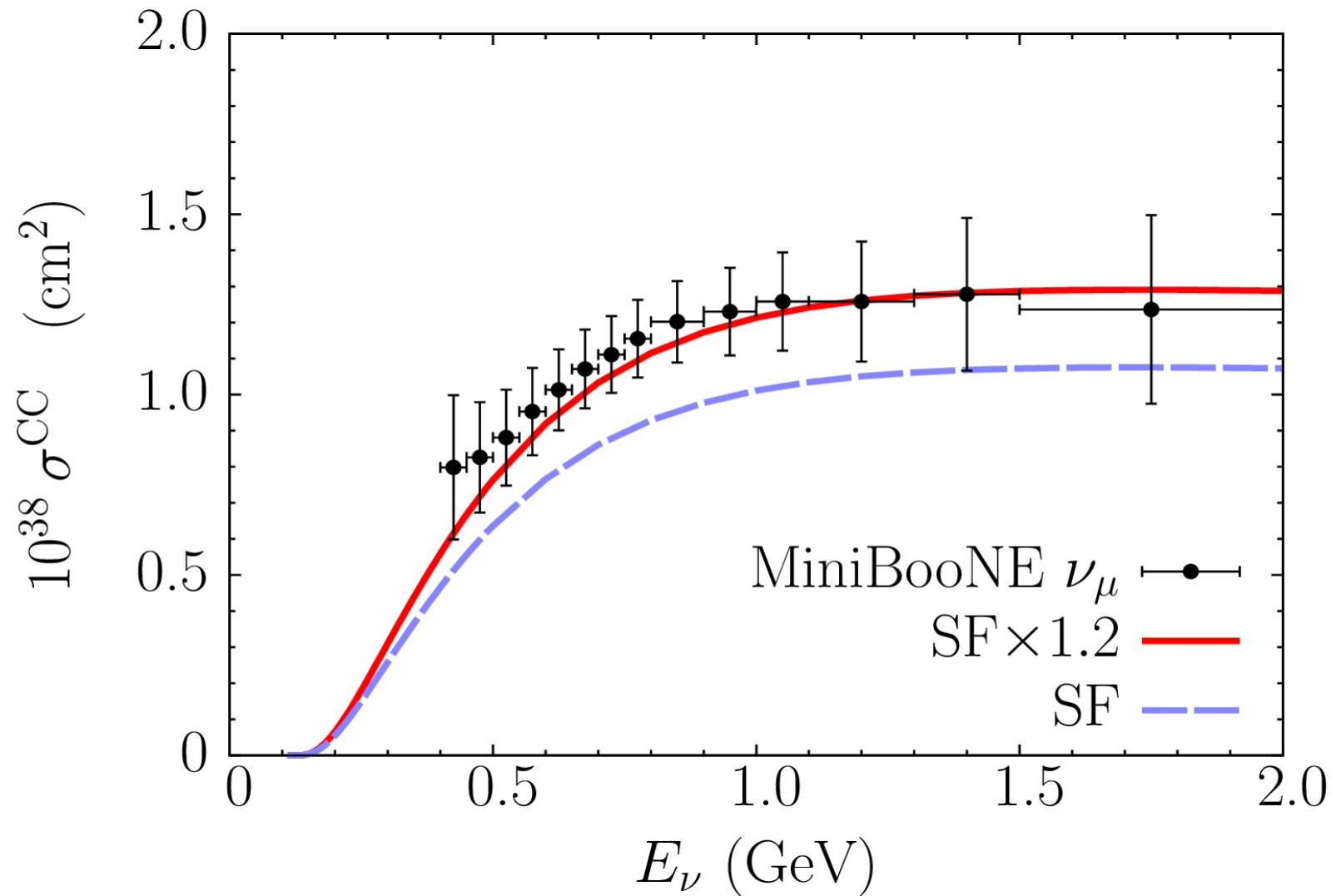




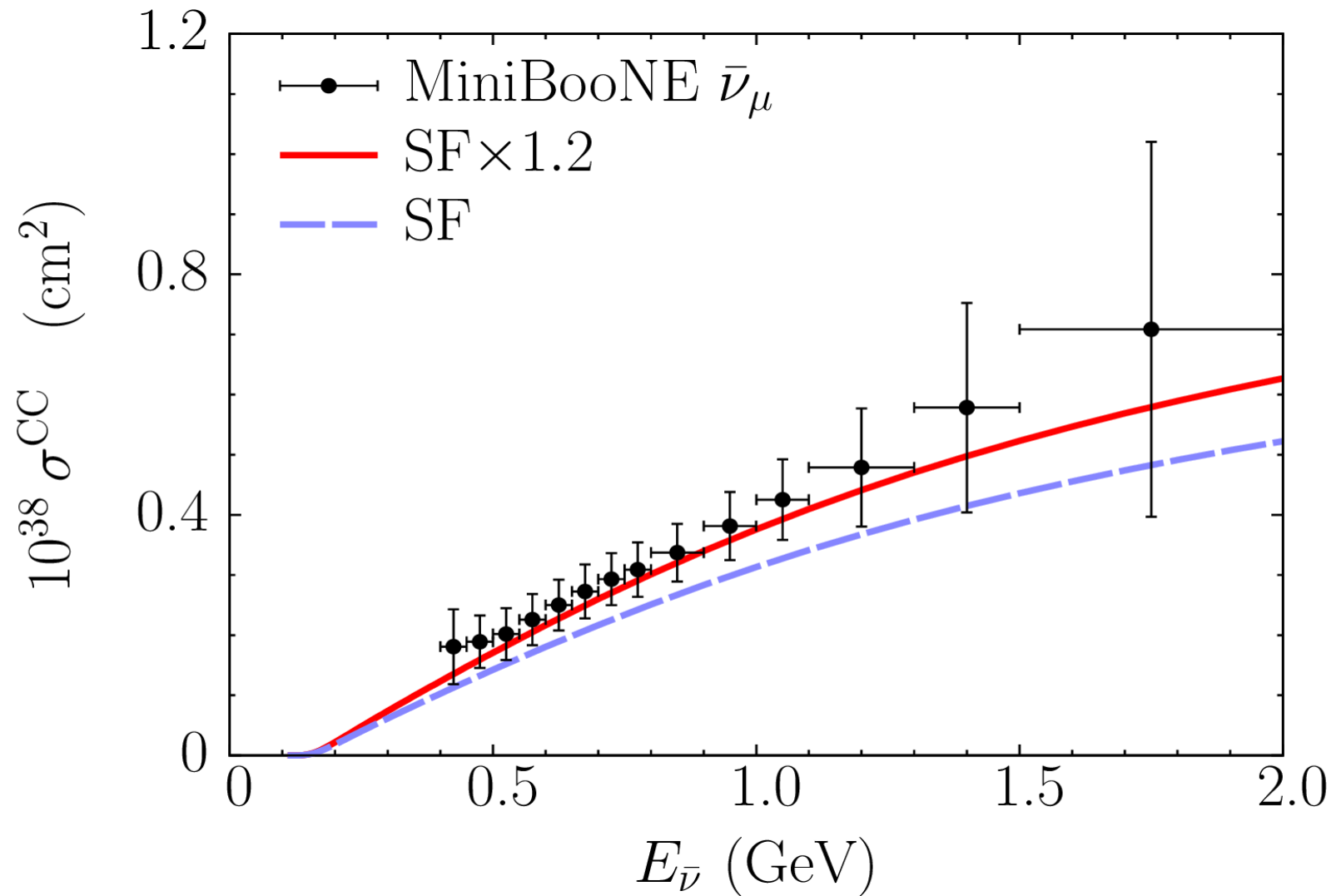
# CCQE $\nu_\mu$ x-section from MiniBooNE



# Total CCQE $\nu_\mu$ cross section



# Total CCQE $\bar{\nu}_\mu$ cross section



# CCQE x-sections from MiniBooNE

- The result for  $d\sigma^{\text{CC}}/dQ^2$  and the data seem to be shifted by  $+0.05 \text{ GeV}^2$  (the smallest bin size)
- The energy-dependence of the total cross sections in a **good agreement** with the data
- The normalization consistently different by **20%**.

**NOMAD-MiniBooNE difference**

# NOMAD-MiniBooNE difference

- CCQE are defined **differently** in both experiments
  - NOMAD: muon only or muon + proton ( $T > 47$  MeV)
  - MiniBooNE: no pions detected

# NOMAD-MiniBooNE difference

- In NOMAD, CCQE events may involve **any number of protons of  $T < 47$  MeV each** and **any number of neutrons**. Such multinucleon final states seem to contribute equally to the 1- and 2-track events (73.9 and 26.1% of the sample, respectively) and independently of energy for  $3 < E < 100$  GeV
- In MiniBooNE, a broader class of multinucleon final states may, in principle, contribute to the CCQE data, such as those involving **at least two protons of  $T > 2*47=94$  MeV in total**

## Does the $\sim 20\%$ difference result from the multiproton events subtracted in NOMAD?

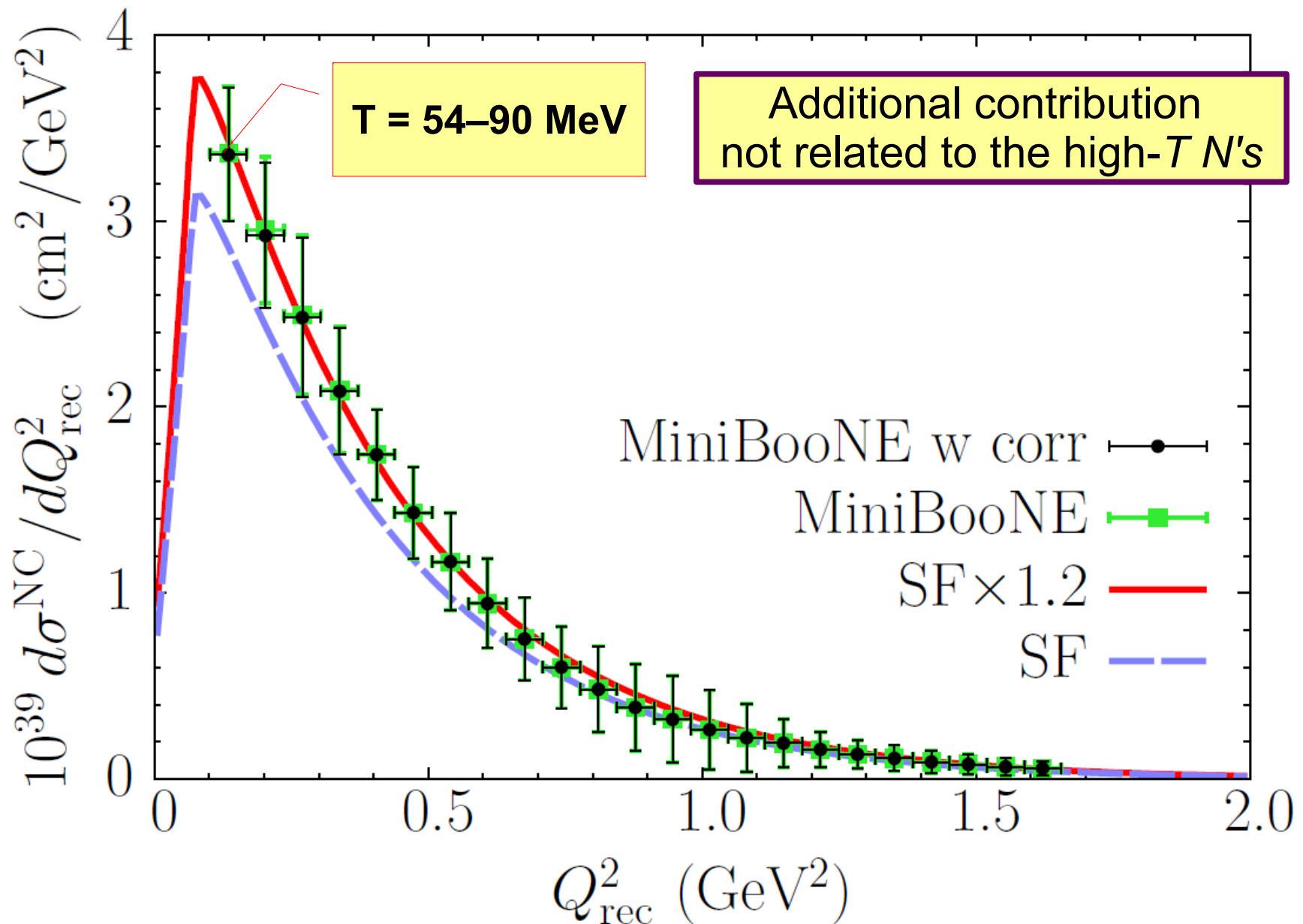
- The additional  $\sim 20\%$  contribution to the MiniBooNE CCQE data **lacks apparent dependence on energy** for  $0.4 < E < 2$  GeV, so it should be recorded also in the NOMAD detector.
- However, the NOMAD Collaboration has not reported a sizable contribution of multinucleon background events



## Does the $\sim 20\%$ difference result from the multiproton events subtracted in NOMAD?

- The MiniBooNE data show no evidence for nuclear effects being different in NCE and CCQE scattering, so **nucleon kinematics in CCQE interaction may be deduced from the NCE result**
- In the MiniBooNE NCE data, the additional strength is **not** limited to the  $T > 94$  MeV ( $Q^2 > 0.177$  GeV<sup>2</sup>) region, but it yields  $\sim 20\%$  of the cross section over the whole considered range  $50 < T < 650$  MeV (no bumps = no new channels)

**Does the ~20% difference result from  
the multiproton events subtracted in NOMAD?**



## Does the $\sim 20\%$ difference result from the multiproton events subtracted in NOMAD?

The MiniBooNE NCE and CCQE data suggest that

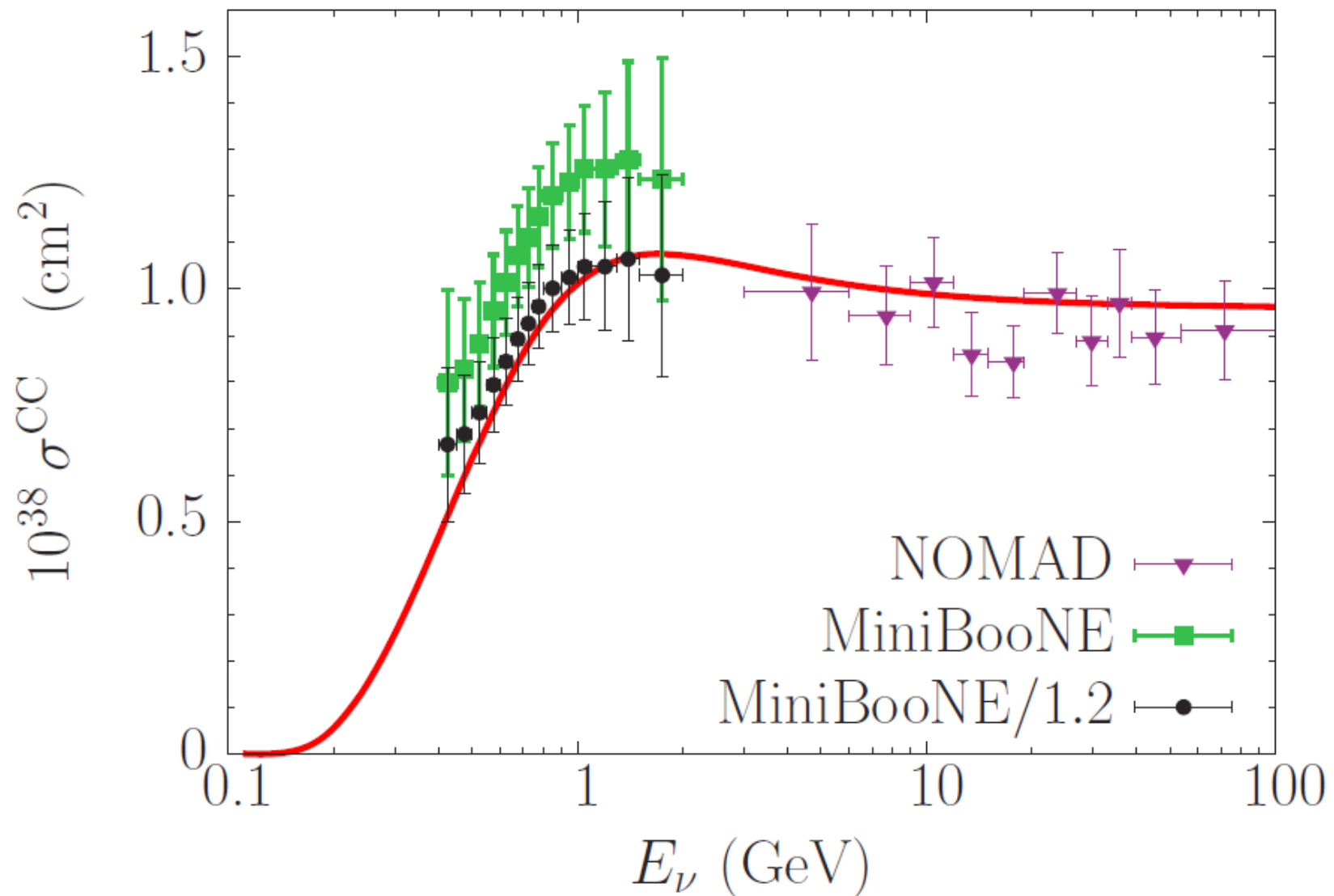
- all the multinucleon channels are open at  $T = 50$  MeV and do not show energy dependence for  $E > 0.4$  GeV, contributing also to the NOMAD data
- the NOMAD-MiniBooNE difference is not related to the multiproton events of  $T > 94$  MeV
- the **same nuclear effects** contribute to the MiniBooNE and NOMAD results

## Other channels

The ratio data/MC is ( $\kappa \sim 1.02$ ,  $M_A = 1.23$  GeV)

- $1.21 \pm 0.24$  for CCQE, MiniBooNE
- 1.23 for CC charged pion production, MiniBooNE
- $1.58 \pm 0.05(\text{stat}) \pm 0.26(\text{syst})$  for CC neutral pion production, MiniBooNE
- $1.29 \pm 0.02(\text{fit}) \pm 0.03(\text{efficiency\&purity})$  for the **inclusive** CC cross section, SciBooNE

**Does the  $\sim 20\%$  difference result from  
the multiproton events subtracted in NOMAD?**



## Summary

- ① Fairly good description of the BNL E734 data, good agreement with NOMAD and MINERvA
- ② The shape of the NCE MiniBooNE data described very accurately, similar results for CCQE. The normalization consistently off by 20%.
- ③ In the MiniBooNE NCE data, I find no evidence for multinucleon contributions different than those in the NOMAD data.
- ④ The NOMAD-MiniBooNE difference likely to be related to the flux uncertainty in MiniBooNE.

**Back-up slides**

# Axial mass from shape analysis

- $1.144 \pm 0.077$  GeV for  $^{12}\text{C}$ ,  
C. Mariani (K2K), AIP Conf. Proc. **981**, 247 (2008)
- $1.23 \pm 0.20$  GeV for  $^{12}\text{C}$ ,  $\langle E \rangle = 0.8$  GeV,  
Aguilar-Arevalo *et al.* (MiniBooNE), PRL **100**, 032301 (2008)
- $1.07 \pm 0.06(\text{stat}) \pm 0.07(\text{syst})$  GeV for  $^{12}\text{C}$ ,  $\langle E \rangle = 25.9$  GeV  
V. Lyubushkin *et al.* (NOMAD), EPJ C **63**, 355 (2009)
- $1.35 \pm 0.17$  GeV for  $^{12}\text{C}$ ,  $\langle E \rangle = 0.8$  GeV,  
Aguilar-Arevalo *et al.* (MiniBooNE), PRD **81**, 092005 (2010)
- $1.20 \pm 0.12$  GeV for  $^{16}\text{O}$ ,  $\langle E \rangle = 1.3$  GeV,  
R. Gran *et al.* (K2K), PRD **74**, 052002 (2006)
- $1.19^{+0.09}_{-0.10}(\text{fit})^{+0.12}_{-0.14}(\text{syst})$  GeV for  $^{56}\text{Fe}$ , all  $Q^2$ , peak at 3 GeV  
M. Dorman (MINOS), AIP Conf. Proc. **1189**, 133 (2009)



# NCE cross sections from BNL E734

- The fluxes determined from the CCQE cross sections (Llewellyn-Smith + corrections for Fermi motion and Pauli blocking)
- At  $0.15 \leq Q^2 \leq 1.15 \text{ GeV}^2$  the SF result (1.23 GeV) varies 9.1 times, differing by **less than 10%** from the free cross section (1.03 GeV); the corrections should diminish the difference
- Therefore, the agreement between the results and the data **does not seem to be accidental**

## II. MINIBOONE EXPERIMENT

### A. Neutrino beamline and flux

The Booster Neutrino Beamline (BNB) consists of three major components as shown in Fig. 1: a primary proton beam, a secondary meson beam, and a tertiary neutrino beam. Protons are accelerated to 8 GeV kinetic energy in the Fermilab Booster synchrotron and then fast-extracted in  $1.6 \mu\text{s}$  “spills” to the BNB. These primary protons impinge on a 1.75 interaction-length beryllium target centered in a magnetic focusing horn. The secondary mesons

HARP data. The HARP data used was that from a thin (5% interaction length) beryllium target run [20]. While that