contributions.<sup>20</sup> For Fe metal,  $H_i$  is predominantly produced by core polarization.<sup>21</sup> From the spectra in Fig. 2  $H_i$  was determined from the splitting of the two outermost lines of the spectrum.<sup>19</sup> For concentrations above approximately 14 at.% Fe, the IS and  $H_i$  were independent of concentration, within the experimental uncertainty, and equal to that of bulk Fe metal at 4 K (IS equals  $0.116 \pm 0.003$  mm/sec with respect to Fe metal at 300 K, and  $H_i = 338 \pm 3$  kOe).<sup>22</sup> Therefore, any change in electronic structure with concentration was undetectable using the Mössbauer effect. This was also true of the optical measurements of Phelps, Avei, and Flynn.<sup>6</sup>

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## Solvable Model of a Spin-Glass

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We consider an Ising model in which the spins are coupled by infinite-ranged random interactions independently distributed with a Gaussian probability density. Both "spin-glass" and ferromagnetic phases occur. The competition between the phases and the type of order present in each are studied.

Compelling experimental<sup>1,2</sup> and theoretical<sup>3-5</sup> evidence has accumulated in recent years suggesting that a new magnetic phase may occur in spatially random systems with competing exchange interactions. In this "spin-glass" phase, moments are frozen into equilibrium orientations, but there is no long-range order. Edwards and Anderson (EA) have demonstrated<sup>3</sup> that such a phase occurs within a novel form of molecular-field theory, and they propose that spin correla-

tions between Gibbs-like replicas of the random system play the role of a spin-glass order parameter.

A closely related replica formalism has been employed in several recent papers<sup>6,7</sup> applying renormalization-group methods to random magnetic systems. The possibility of an EA-type<sup>4</sup> order parameter was not considered in that work, although some of the models studied<sup>7</sup> appear likely to exhibit spin-glass phases.

It is well known that molecular-field theory for a pure ferromagnet becomes exact in the thermodynamic limit for a constant infinite-ranged exchange interaction provided that the interaction is appropriately scaled with the number of spins in the system. In this Letter we define and solve the analogous infinite-ranged problem for a disordered system. We obtain a spin-glass solution characterized by the EA order parameter in the appropriate regime of temperature and the strength of the exchange fluctuations. A simple interpretation of this order parameter is given. The various thermodynamic quantities and the competition with ferromagnetic long-range order are explored in some detail.

We consider *N* Ising spins interacting through infinite-ranged exchange interactions which are independently distributed with a Gaussian proba-

bility density. The Hamiltonian is

$$\mathcal{GC} = -\frac{1}{2} \sum_{i \neq i} J_{ij} S_i S_j, \quad S_i = \pm 1, \tag{1}$$

with the  $J_{ij}$  distributed according to

$$p(J_{ij}) = [(2\pi)^{1/2}J]^{-1} \exp[-(J_{ij} - J_0)^2/2J^2], \qquad (2)$$

and  $J_0$  and J scaled by

$$J_0 = \tilde{J}_0/N, \quad J = \tilde{J}/N^{1/2},$$
 (3)

so that  $\tilde{J}_0$  and  $\tilde{J}$  are both intensive. Following the usual procedure, we calculate the averaged free energy. (Averaging the free energy and not the partition function corresponds to treating a "quenched" rather than an "annealed" system.) With use of the identity

$$\ln x = \lim_{n \to 0} (x^n - 1)/n, \tag{4}$$

the averaged free energy F may be expressed as

$$F = -kT \lim_{n \to 0} n^{-1} \left\{ \int \prod_{(ij)} \left[ p(J_{ij}) dJ_{ij} \right] \operatorname{Tr}_n \exp\left( \sum_{\alpha = 1, \dots, n} \sum_{i \neq j} J_{ij} S_i^{\alpha} S_j^{\alpha} / 2kT \right) - 1 \right\}$$

$$= -kT \lim_{n \to 0} n^{-1} \left\{ \operatorname{Tr}_n \exp\left( \sum_{i \neq j} \left[ \sum_{\alpha} S_i^{\alpha} S_j^{\alpha} J_0 / 2kT + \sum_{\alpha, \beta} S_i^{\alpha} S_j^{\alpha} S_i^{\beta} S_j^{\beta} J^2 / 4(kT)^2 \right] \right) - 1 \right\}, \tag{5}$$

where  $\alpha$  and  $\beta$  label n dummy replicas. Reordering and dropping terms which vanish in the thermodynamic limit yields

$$F = -kT \lim_{n \to 0} n^{-1} \left\{ \exp\left[J^2 N^2 n / 4(kT)^2\right] \operatorname{Tr}_n \exp\left[\sum_{(\alpha\beta)} \left(\sum_i S_i^{\alpha} S_i^{\beta}\right)^2 J^2 / 2(kT)^2 + \sum_{\alpha} \left(\sum_i S_i^{\alpha}\right)^2 J_0 / 2kT\right] - 1 \right\}, \tag{6}$$

where  $(\alpha\beta)$  refers to combinations of  $\alpha$  and  $\beta$  with  $\alpha \neq \beta$ . Using the identity

$$\exp(\lambda a^2) = (2\pi)^{-1/2} \int dx \exp\left[-x^2/2 + (2\lambda)^{1/2} ax\right],\tag{7}$$

we rewrite (6) as

$$F = -kT \lim_{n \to 0} n^{-1} \left\{ \exp\left[\tilde{J}^{2}Nn/4(kT)^{2}\right] \int \left[\prod_{(\alpha\beta)} (N/2\pi)^{1/2} dy^{(\alpha\beta)}\right] \left[\prod_{\alpha} (N/2\pi)^{1/2} dx^{\alpha}\right] \right.$$

$$\times \exp\left[-N \sum_{(\alpha\beta)} (y^{(\alpha\beta)})^{2}/2 - N \sum_{\alpha} (x^{\alpha})^{2}/2 + N \ln \operatorname{Tr} \exp\left((\tilde{J}/kT) \sum_{(\alpha\beta)} y^{(\alpha\beta)} S^{\alpha} S^{\beta} + (\tilde{J}_{0}/kT)^{1/2} \sum_{\alpha} x^{\alpha} S^{\alpha}\right)\right] - 1\right\},$$

$$(8)$$

where the trace is now over n replicas at a single spin site.

It is assumed that the limit  $n \to 0$  and the thermodynamic limit  $N \to \infty$  can be interchanged. For integral  $n \ge 2$ , the integrals may be done by steepest descents. Since the replicas are indistinguishable, we consider only the extremum of the exponential for which all the  $y^{(\alpha\beta)}$  are equal, as are all the  $x^{\alpha}$ . We denote their values by y and x. This permits the replacement  $\sum y^{(\alpha\beta)}S^{\alpha}S^{\beta} \to y[(\sum_{\alpha}S^{\alpha})^2 - n]$ , and  $(\sum_{\alpha}S^{\alpha})^2$  may be absorbed by the introduction of a random field. Continuation to arbitrary n, extraction of the terms linear in n as  $n \to 0$ , and the substitutions  $y \to q(\tilde{J}/kT)$  and  $x \to m(\tilde{J}_0/kT)^{1/2}$  then yield

$$F = NkT \left\{ -\tilde{J}^2 (1-q)^2 / (2kT)^2 + \tilde{J}_0 m^2 / 2kT - (2\pi)^{-1/2} \int dz \exp(-z^2/2) \ln[2 \cosh(\tilde{J}q^{1/2}z/kT + \tilde{J}_0 m/kT)] \right\}, \tag{9}$$

where q and m satisfy the simultaneous equations

$$q = 1 - (2\pi)^{-1/2} \int dz \exp(-z^2/2) \operatorname{sech}^2[\tilde{J}q^{1/2}/kT]z + \tilde{J}_0 m/kT], \tag{10a}$$

$$m = (2\pi)^{-1/2} \int dz \exp(-z^2/2) \tanh[(\tilde{J}q^{1/2}/kT)z + \tilde{J}_0 m/kT].$$
 (10b)

To show the physical significance of m and q we note that the thermal average of the spin at site i,  $\langle S_i \rangle$ , and its square may be written

$$\langle S_i \rangle = (\partial/\partial h) \ln \operatorname{Tr} \exp(\sum_{i \neq j} J_{ij} S_i^{\alpha} S_j^{\alpha} / 2k T + h S_i^{\alpha})_{h=0},$$
 (11a)

$$\langle S_{i} \rangle = (\partial/\partial h) \ln \operatorname{Tr} \exp\left(\sum_{i \neq j} J_{ij} S_{i}^{\alpha} S_{j}^{\alpha} / 2k \, T + h S_{i}^{\alpha}\right)_{h=0}, \tag{11a}$$

$$\langle S_{i} \rangle^{2} = (\partial/\partial h') \ln \operatorname{Tr} \exp\left[\sum_{i \neq j} J_{ij} \left(S_{i}^{\alpha} S_{j}^{\alpha} + S_{i}^{\beta} S_{j}^{\beta}\right) / 2k \, T + h' S_{i}^{\alpha} S_{i}^{\beta}\right]_{h'=0}, \tag{11b}$$

where  $\alpha \neq \beta$  are dummy labels. Averaging over the  $J_{ij}$  distribution, which we denote by  $\langle \rangle_J$ , we see that  $\langle\langle S_i \rangle\rangle_J$  and  $\langle\langle S_i \rangle^2\rangle_J$  are given by taking the  $n \to 0$  limits respectively of  $\langle S_i^{\alpha} \rangle$  and  $\langle S_i^{\alpha} \rangle$  $\times S_{i}^{\beta}\rangle_{\alpha\neq\beta}$  evaluated for a system characterized by the J-averaged n-ensemble partition function. This result is valid for finite-ranged interactions as well as infinite-ranged ones. Thus9

$$m \equiv \langle \langle S_i \rangle \rangle_J, \tag{12a}$$

$$q \equiv \langle \langle S_i \rangle^2 \rangle_I, \tag{12b}$$

independent of i. A nonzero q indicates magnetic order, while nonzero m (in addition to q) indicates that that order is ferromagnetic. When m= 0 but q is nonzero, we shall call the state a "spin-glass."

Equations (10) indicate that magnetic order sets in as kT is reduced below the greater of  $\tilde{J_0}$  or  $\tilde{J}$ . If  $\tilde{J}_0 > \tilde{J}$ , the phase that is reached is ferromagnetic, but when the converse is true, spin-glass order ensues, and m remains zero for  $kT < \tilde{J}$ . The full phase diagram is plotted in Fig. 1, in terms of the dimensionless combinations  $\tilde{J}_0/\tilde{J}$  and  $kT/\tilde{J}$ . and may easily be rescaled to describe models in which  $\tilde{J_0}$  and  $\tilde{J}$  are known functions of external parameters (see, e.g., Ref. 4).

For  $\tilde{J}_0/\tilde{J}\gg 1$  the effects of fluctuations are weak, and one can show from (10a) and (10b) that  $q \sim m^2$ , in accord with the physical interpretation (12b) of q as the square of the modulus of the frozen mo-

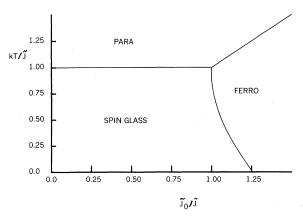


FIG. 1. Phase diagram of spin-glass ferromagnet.

ment per site. The zero-temperature magnetization is diminished by weak fluctuations as

$$m \sim 1 - (2/\pi)^{1/2} (\tilde{J}/\tilde{J}_0) \exp(-\tilde{J}_0^2/2\tilde{J}^2),$$
 (13a)

and vanishes continuously at the spin-glass phase boundary as

$$m \sim (18\pi)^{1/4} (\tilde{J}_0/\tilde{J})^2 [(2/\pi)^{1/2} - \tilde{J}/\tilde{J}_0]^{1/2}.$$
 (13b)

Values of m(T) and  $q^{1/2}$  obtained by numerical solution of (10a) and (10b) are plotted in Fig. 2 for various values of  $\tilde{J}_0/\tilde{J}$ . We note that the effect of fluctuations is strongest at low temperatures, causing the decrease in the magnetization as  $T \rightarrow 0$  in Fig. 2, and a line of second-order transitions from ferromagnet to spin-glass in the phase diagram of Fig. 1.

The frozen moment,  $q^{1/2}(T)$ , as is shown in Fig. 2 and as can be derived from (10a) and (10b), is proportional to  $(T_c - T)^{1/2}$  just below  $T_c$ , tends to unity as  $T \rightarrow 0$ , and is always greater than m(T)at the same temperature. The linear low-temperature dependence of q and  $q^{1/2}$ ,

$$1 - q(T) \sim (2/\pi)^{1/2} (kT/\tilde{J}) \exp(-\tilde{J}_0^2 m^2/2\tilde{J}^2),$$
 (14)

as  $T \rightarrow 0$ , contrasts with that of m(T) in a uniform Ising magnet, for which all temperature derivatives vanish at T = 0, since excitations from the ferromagnetic ground state require a

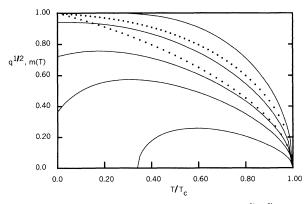


FIG. 2. Solid lines denote m(T) for ratios  $\tilde{J}_0/\tilde{J}$  of (top to bottom)  $\infty$ , 2.0, 1.5 1.3, and 1.1. Dotted lines show  $q^{1/2}(T)$  for  $\tilde{J}_0/\tilde{J}=2.0$  (upper line) and 0.0 (lower

finite energy.

The differential susceptibility,  $\chi$ , may be obtained by repeating the steps leading to (9) and (10) with an external field term,  $\sum_i HS_i$ , in the Hamiltonian (1). This simply adds an extra contribution, H/kT, to the arguments of sech and tanh in (10a) and (10b). Differentiating (10b) with respect to H, and taking the limit  $h \to 0$ , we then obtain

$$\chi(T) = [1 - q(T)] / \{kT - \tilde{J}_0[1 - q(T)]\}$$

$$= \chi^{(0)} / (1 - \tilde{J}_0\chi^{(0)}), \tag{15}$$

where  $\chi^{(0)}$  is the result for  $\tilde{J_0} = 0$ . Above the ordering temperature, where q = 0, this is just a Curie-Weiss law. In the spin-glass phase, the fluctuations decrease  $\chi$ , while  $\tilde{J_0}$  enhances it. Two examples are plotted in Fig. 3. The dotted lines in Fig. 3 show the effect of a finite field,  $H = 0.1\tilde{J}$ , on the differential susceptibility in each case.

From (9), we obtain the internal energy, U:

$$U = -N[m^2 \tilde{J}_0/2 + \tilde{J}^2(1 - q^2)/2kT]. \tag{16}$$

In the spin-glass phase the leading term in the specific heat at low temperatures is

$$C \sim Nk(kT/\tilde{J})(2/\pi)^{1/2}[(\pi^2/12) - 1/2\pi].$$
 (17)

At the spin-glass ordering temperature C has a cusp. For all  $\tilde{J}_0$ , C equals  $Nk\tilde{J}^2/2(kT)^2$  above the ordering temperature,  $^{10}$  in contrast to the corresponding pure systems for which it vanishes. The linear temperature dependences seen in C, m, and  $q^{1/2}$  suggest that the system possesses excitations from the ground state whose density remains finite down to zero energy. The entropy S equals  $Nk[\ln 2 - \tilde{J}^2/(2kT)^2]$  above the spin-glass ordering temperature, but goes to a negative limit,  $-Nk/2\pi$ , at T=0. We speculate that this unphysical behavior has its origin in the interchange of limits  $N+\infty$  and n+0, but that the consequences are confined to low temperatures.

When an Ising system described by (1) and (2) with nearest-neighbor interactions is treated with mean-field theory (of the EA type), equations identical to (10) are obtained, with  $zJ_0$  and  $z^{1/2}J$  replacing  $J_0$  and J, where z is the average number of neighbors. For interactions which are on the average antiferromagnetic or which include second-neighbor terms, analogous equations result in which m is replaced by the appropriate sublattice magnetization.

For the finite-ranged interactions occurring in real systems, the results presented here have at

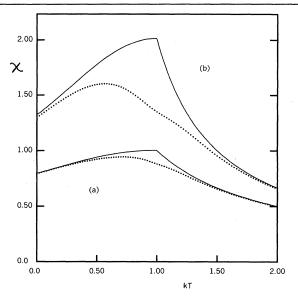


FIG. 3. Differential susceptibility without external field (solid lines) and with a field  $H=0.1\tilde{J}$  (dotted lines) for  $\tilde{J}_0/\tilde{J}=0$ , curves a, and  $\tilde{J}_0/\tilde{J}=0.5$ , curves b.

best mean-field significance, and thus cannot treat critical phenomena correctly. However, it is evident that any more sophisticated treatment of critical properties in the presence of random competing exchange interactions should allow for the possibility of order parameters  $\langle S_i \rangle^n \rangle_J$  with n>1, such as q discussed above.

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 $^9{\rm The}$  identification (12b) of q has also been pointed out by Fischer in Ref. 5.

<sup>10</sup>This result can also be obtained from high-temperature expansions.

<sup>11</sup>R. Harris and D. Zobin (private communication) have

investigated analogous mean-field equations for the Heisenberg spin-glass model of Ref. 4. They find a phase diagram similar to Fig. 1.

## Electronic Structure of Polymeric Sulfur Nitride, $(SN)_x$ , from X-Ray-Photoelectron Spectroscopy

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An overview of the valence-band region of  $(SN)_x$  by means of photoelectron spectroscopy is presented. The spectrum gives, in general, an excellent account of the density of occupied states compared with band-structure calculations. Deviations between theory and experiment in the region of the conduction band are taken as strong evidence for interchain coupling. The interchain matrix element is estimated to be 0.6 times the value of the intrachain matrix element. The consequences of this result are discussed.

Polysulfur nitride,  $(SN)_x$ , is a quasi one-dimensional inorganic polymer with a metallic ground state. It maintains in contrast to other one-dimensional systems such as  $K_2[Pt(CN)_4]Cl_{0.3}$ .  $3H_2O$  and tetrathiafulvalene-tetracyanoquinodimethane its metallic conductivity down to very low temperatures and becomes even superconducting at  $T_c \simeq 0.26^\circ K$ . Experimental information about the electronic structure of this important new material is as yet scarce and—with the exception of one optical absorption measurement —limited to effective masses of the conduction electrons and the density of states at the Fermi energy.  $^2$ 

I report in this Letter the first overall density of occupied states of  $(SN)_x$  as measured by x-ray-photoelectron spectroscopy (XPS). The result indicates appreciable interaction of electrons on neighboring chains.

Samples of  $(SN)_x$  were prepared following the method developed by Douillard<sup>5</sup> as films on glass and fused silica substrates.<sup>6</sup> The films have the characteristic brassy luster and showed good conductivity.

The XPS spectra with a resolution of 0.6 eV were taken in a Hewlett-Packard electron spectrometer utilizing monochromatized x rays (Al  $K\alpha$ , 1486 eV). Initial oxygen- and carbon-containing surface contaminations could almost completely be removed by wiping the film surface several times in a dry nitrogen atmosphere just prior to insertion of the sample into the spectrometer vacuum of  $1\times 10^{-9}$  Torr. No signal from any contamination apart from 3% carbon could be detected after this procedure.

In spite of an average film thickness of several thousand angstroms the films were not found to be completely opaque: The spectrum showed some emission from the substrate. This emission could easily be corrected for, by removing the  $(SN)_x$  film and running a spectrum of the glass substrate alone. Position and intensity of strong core levels common to both spectra allowed a very accurate correction of the original spectra.

The valence-band region of the photoelectron spectrum extending from the Fermi energy,  $E_{\rm F}$ , to 30 eV below  $E_{\rm F}$  is shown in the upper part of Fig. 1. The dots represent the raw data and the continuous line the spectrum corrected for the contribution of the substrate. It is apparent that the corrections are insignificant for most of the spectrum except for a region close to the bottom of the band. Corrected spectra, I(E), identical to the one shown in Fig. 1 were obtained for three different samples with varying substrate contributions. Energies are referred to the Fermi level  $(E_{\rm F})$  as determined from an Au mask in electrical contact with the film surface.

Five main pieces of structure can be distinguished within the total bandwidth of  $24.4\pm0.7$  eV: four peaks labeled 1 to 4 in Fig. 1 centered at 21.0, 15.2, 7.4, and 3.6 eV, respectively, and a shoulder ("5") at 0.7 eV below  $E_{\rm F}$ . The density of states at  $E_{\rm F}$  is small, but finite, thus reaffirming the metallic character of (SN)<sub>r</sub>.

These features are in excellent agreement with those in the density of states, N(E), calculated by Parry and Thomas(PT),<sup>9</sup> as shown in Fig. 1. The agreement is further emphasized if the observed lifetime broadening in N(E) is included