

Chiral EFT Expansion in Light Nuclei

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ECT* 2017



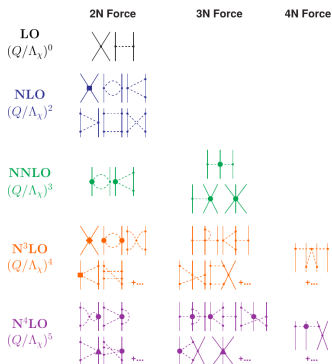
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Outline

- 1 Motivation
- 2 No-Core Shell Model
- 3 Similarity Renormalization Group
- 4 Chiral Interactions
- 5 Summary and Outlook

Motivation

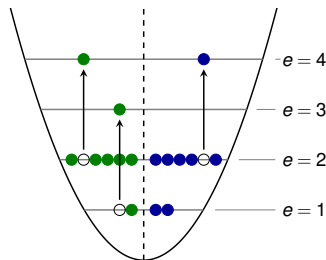
- ab initio nuclear structure
 - solving the nuclear many-body problem with realistic interactions
 - use controlled and improvable truncations
 - quantification of theoretical uncertainties
 - convergence with respect to truncations
- chiral effective field theory (EFT)
 - systematic and improvable
 - full quantification of theory uncertainties



arXiv:1703.05454[nucl-th](2017)

No-Core Shell Model

- model space constructed out of antisymmetric harmonic-oscillator states
- total excitation energy is truncated by $N_{\max} \hbar\omega$
- solve eigenvalue problem
- exact solution for $N_{\max} \rightarrow \infty$



example basis configuration for ^{16}O with $N_{\max} \geq 6$

Similarity Renormalization Group

- SRG aims to decouple low- and high-momentum states
- accelerate the convergence of many-body calculations with model-space size
- continuous unitary transformation via flow equation approach

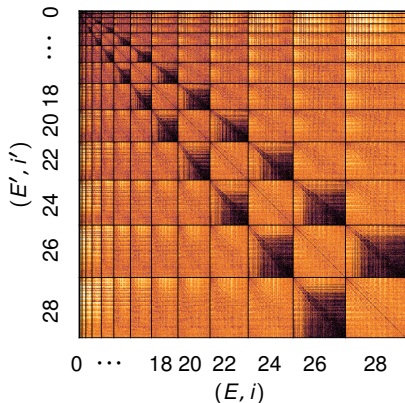
$$\mathbf{H}_\alpha = \mathbf{U}_\alpha^\dagger \mathbf{H}_0 \mathbf{U}_\alpha \quad \Rightarrow \quad \frac{d\mathbf{H}_\alpha}{d\alpha} = [\boldsymbol{\eta}_\alpha, \mathbf{H}_\alpha]$$

- antihermitian dynamic generator

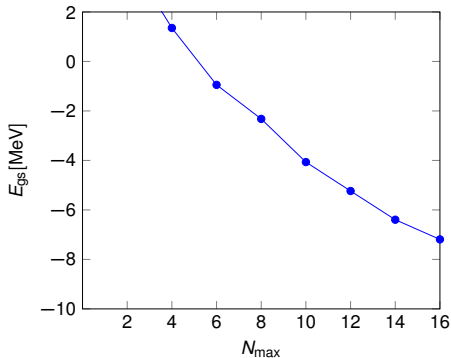
$$\boldsymbol{\eta}_\alpha = (2\mu)^2 [\mathbf{T}_{\text{int}}, \mathbf{H}_\alpha]$$

- SRG induces forces with higher particle rank
- solve flow equations in two- and three-body space

${}^3\text{H}$ SRG Evolution with $\alpha = 0.0 \text{ fm}^4$

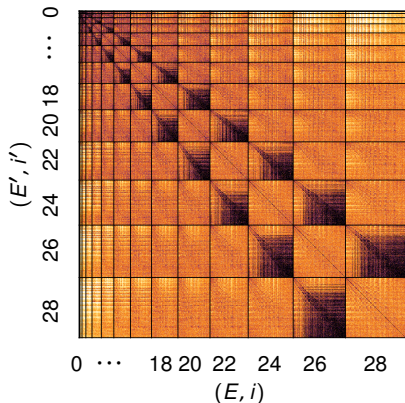


${}^3\text{H}$ channel ($T=1$ $J=1$ $P=1$) in antisymmetrized Jacobi HO basis

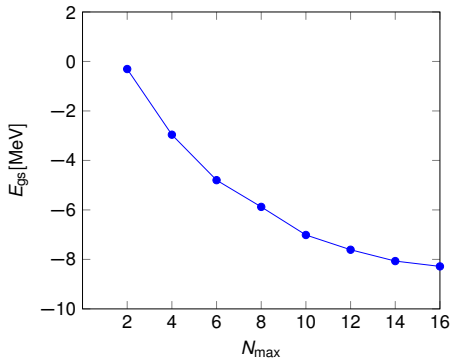


${}^3\text{H}$ NCSM calculation
 $\hbar\omega = 20 \text{ MeV}$

^3H SRG Evolution with $\alpha = 0.01 \text{ fm}^4$

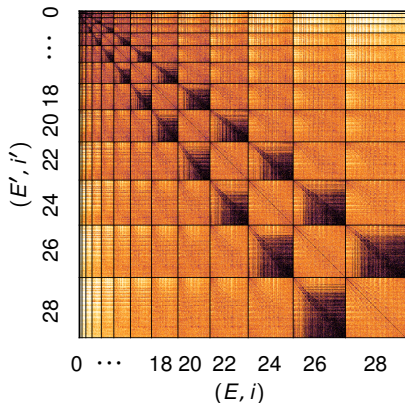


^3H channel ($T=1$ $J=1$ $P=1$) in antisymmetrized Jacobi HO basis

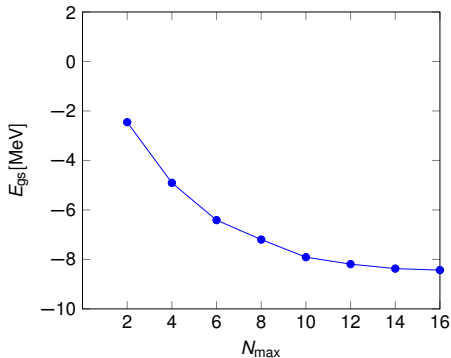


^3H NCSM calculation
 $\hbar\omega = 20 \text{ MeV}$

${}^3\text{H}$ SRG Evolution with $\alpha = 0.02 \text{ fm}^4$

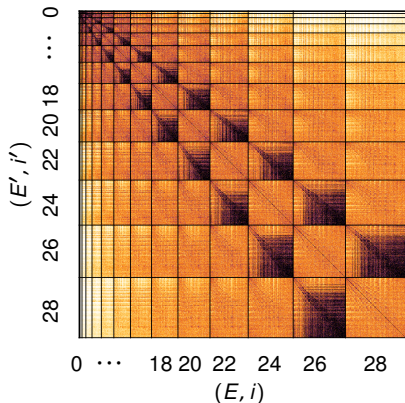


${}^3\text{H}$ channel ($T=1$ $J=1$ $P=1$) in antisymmetrized Jacobi HO basis

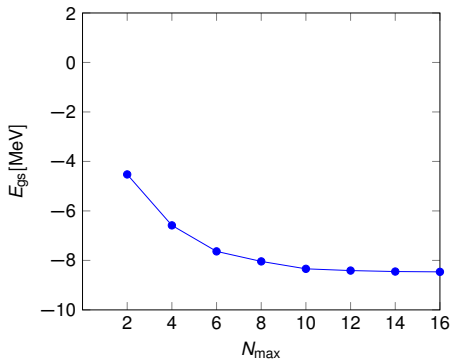


${}^3\text{H}$ NCSM calculation
 $\hbar\omega = 20 \text{ MeV}$

${}^3\text{H}$ SRG Evolution with $\alpha = 0.04 \text{ fm}^4$

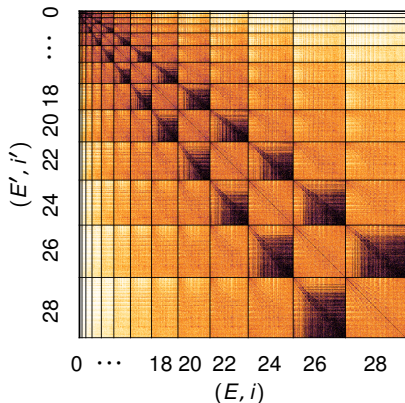


${}^3\text{H}$ channel ($T=1$ $J=1$ $P=1$) in antisymmetrized Jacobi HO basis

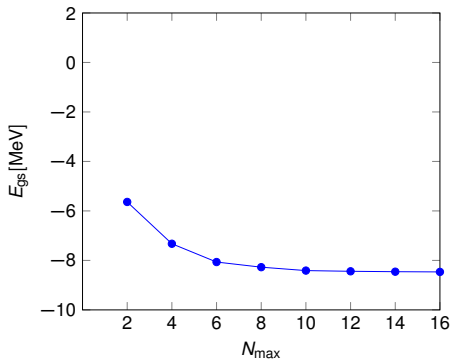


${}^3\text{H}$ NCSM calculation
 $\hbar\omega = 20 \text{ MeV}$

${}^3\text{H}$ SRG Evolution with $\alpha = 0.0625 \text{ fm}^4$

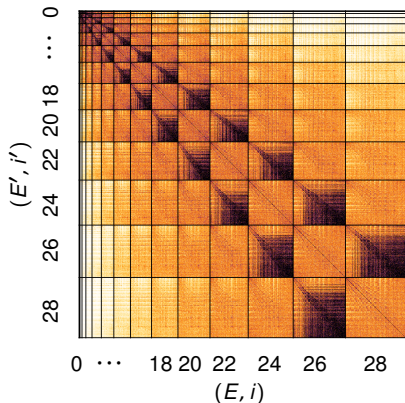


${}^3\text{H}$ channel ($T=1$ $J=1$ $P=1$) in antisymmetrized Jacobi HO basis

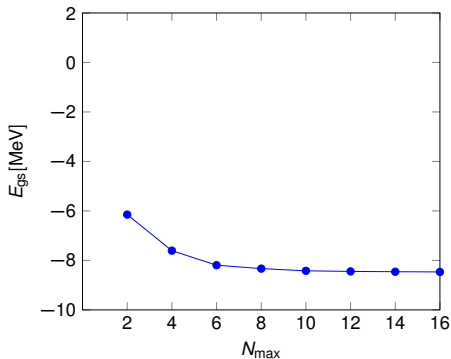


${}^3\text{H}$ NCSM calculation
 $\hbar\omega = 20 \text{ MeV}$

^3H SRG Evolution with $\alpha = 0.08 \text{ fm}^4$

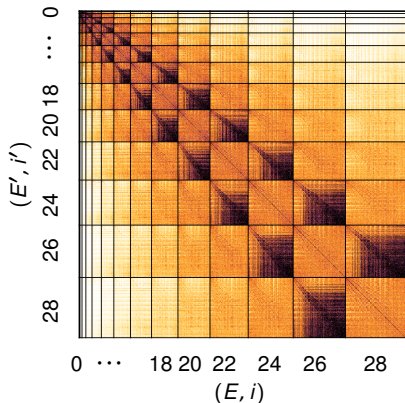


^3H channel ($T=1$ $J=1$ $P=1$) in antisymmetrized Jacobi HO basis

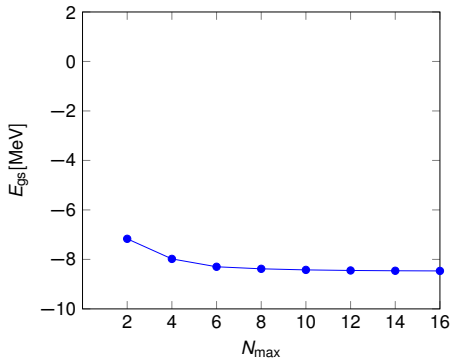


^3H NCSM calculation
 $\hbar\omega = 20 \text{ MeV}$

^3H SRG Evolution with $\alpha = 0.16 \text{ fm}^4$

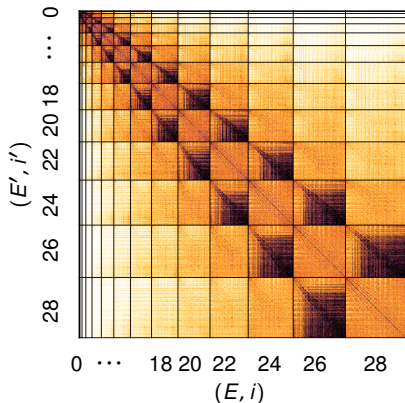


^3H channel ($T=1$ $J=1$ $P=1$) in antisymmetrized Jacobi HO basis

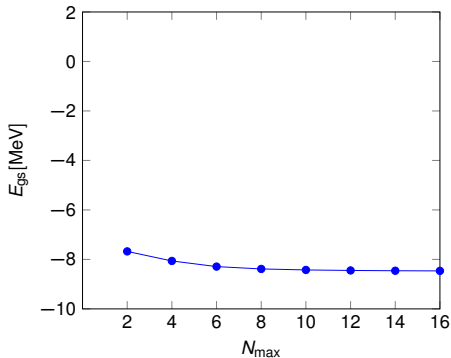


^3H NCSM calculation
 $\hbar\omega = 20 \text{ MeV}$

${}^3\text{H}$ SRG Evolution with $\alpha = 0.32 \text{ fm}^4$

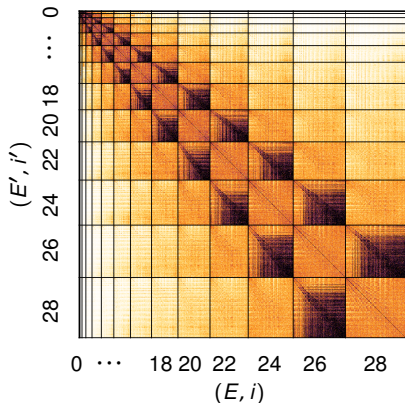


${}^3\text{H}$ channel ($T=1$ $J=1$ $P=1$) in antisymmetrized Jacobi HO basis

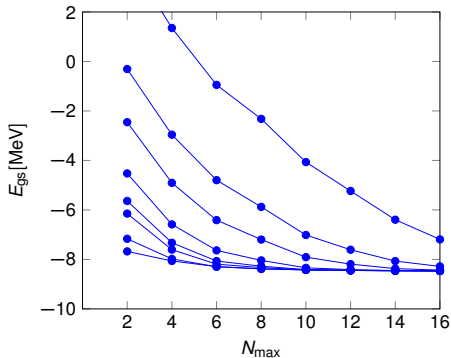


${}^3\text{H}$ NCSM calculation
 $\hbar\omega = 20 \text{ MeV}$

${}^3\text{H}$ SRG Evolution with $\alpha = 0.32 \text{ fm}^4$



${}^3\text{H}$ channel ($T=1$ $J=1$ $P=1$) in antisymmetrized Jacobi HO basis



${}^3\text{H}$ NCSM calculation
 $\hbar\omega = 20 \text{ MeV}$

Improved Epelbaum
/LENPIC

Entem and
Machleidt (EM)

Improved Epelbaum
/LENPIC

- semi-local regularization
- five cutoffs $R = 0.8, 0.9, 1.0, 1.1$ and 1.2 fm
- NN force up to N4LO
- consistent 3N force at N2LO and N3LO in construction

[Eur.Phys.J.A\(2015\)51:53](#), [PRL115.122301\(2015\)](#)

Entem and
Machleidt (EM)

Chiral Interactions

Improved Epelbaum /LENPIC

- semi-local regularization
- five cutoffs $R = 0.8, 0.9, 1.0, 1.1$ and 1.2 fm
- NN force up to N4LO
- consistent 3N force at N2LO and N3LO in construction

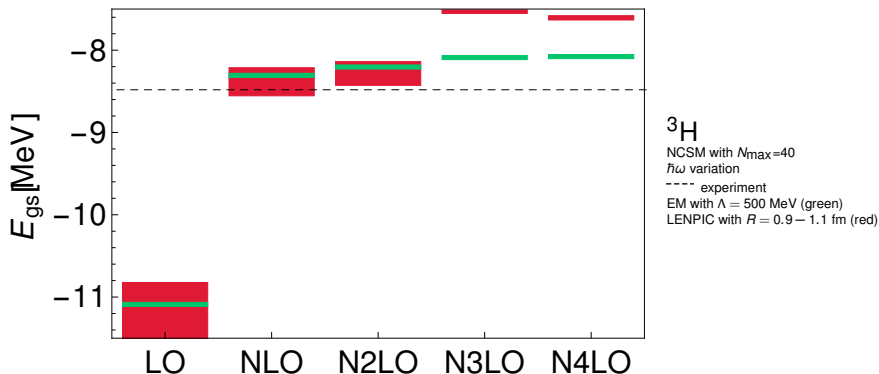
[Eur.Phys.J.A\(2015\)51:53](#), [PRL115.122301\(2015\)](#)

Entem and Machleidt (EM)

- non-local regularization
- three cutoffs $\Lambda = 450, 500$ and 550 MeV
- NN force up to N4LO
- added consistent regularized N2LO 3N force

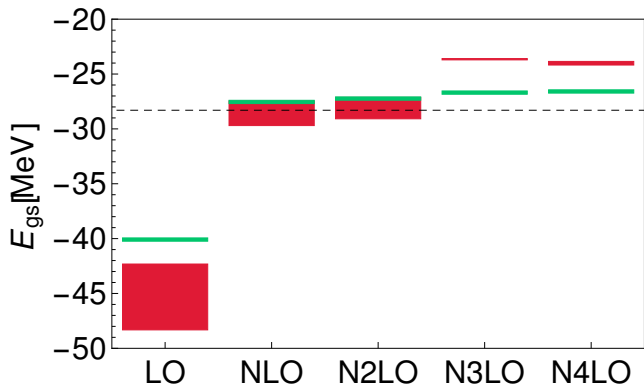
[arXiv:1703.05454\[nucl-th\]\(2017\)](#)

${}^3\text{H}$ with NN Interactions



- uncertainty due to cutoff variation decreases with increasing order
- 3N force necessary for reproducing ${}^3\text{H}$ ground-state energy

^4He with NN Interactions



^4He

NCSM with $M_{\text{max}}=20$

$\hbar\omega$ variation

---- experiment

EM with $\Lambda = 500$ MeV (green)

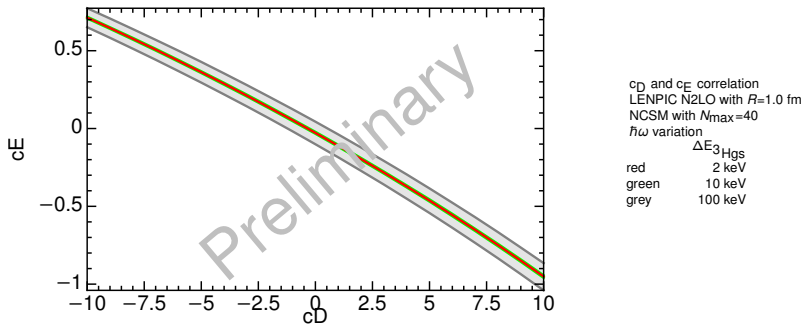
LENPIC with $R = 0.9 - 1.1$ fm (red)

SRG used for LENPIC at N3LO and N4LO

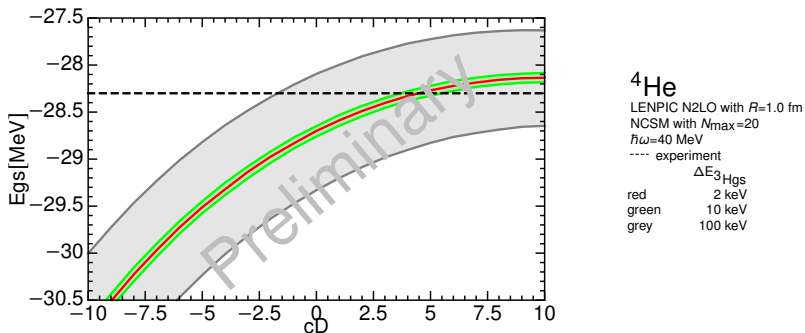
■ similar to ^3H ground-state results

Fitting additional 3N LECs

- adding 3N force at N2LO gives rise of 2 additional LECs
- correlation between c_D and c_E by fitting ${}^3\text{H}$ ground-state energy



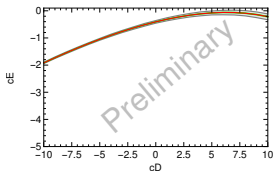
Sensitivity of c_D and c_E



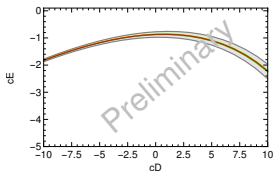
- ground-state energy of ^4He can be reproduced within uncertainty range
- fix c_D with scattering data

Fitting additional 3N LECs of EM Interactions

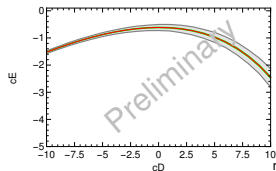
N2LO



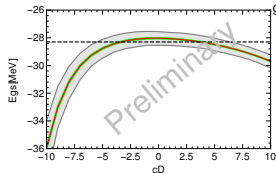
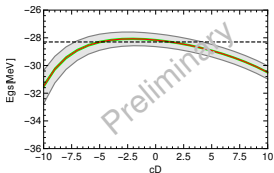
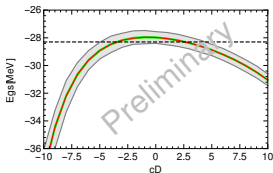
N3LO



N4LO

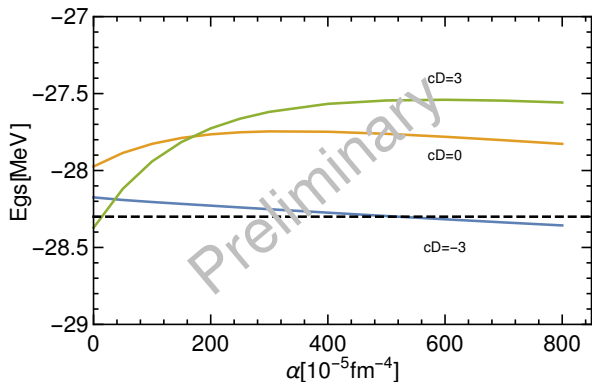


$\Lambda = 500$ MeV
--- experiment
 ΔE_3^{Hgs}
red 2 keV
green 10 keV
grey 100 keV



- broad range of cD and cE pairs reproduce ${}^4\text{He}$ ground-state energy

SRG evolved NN+3N Hamiltonian



${}^4\text{He}$

EM N²LO with $\Lambda = 500$ MeV

NCSM with $N_{\text{max}}=20$

$\hbar\omega=36$ MeV

---- experiment

- strong flow parameter α dependence \rightarrow induced four-body force
- how to resolve this problem?

Summary and Outlook

- LENPIC and EM interactions allow order-by-order analysis
- full quantification of theory uncertainties possible

- finalize cD and cE pairs
- add N3LO 3N interaction
- resolve problem with SRG
- have fun with chiral interactions

Thank You

Thank you for your attention!