The Impact of nuclear effects on accelerator-based neutrino-oscillation physics

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[Repetition helps]





[But it's boring]

Neutrinos Everywhere!



Accelerator-based neutrino-oscillation experiments

		$ heta_{12}$	$ heta_{13}$	$ heta_{23}$	$\Delta m^2_{21}/10^{-5}$	$\Delta m_{3j}^2/10^{-3}$	δ_{CP}			
Current knowledge:	Normal Ordering	$33.56\substack{+0.77 \\ -0.75}$	$8.46\substack{+0.15 \\ -0.15}$	$41.6^{+1.5}_{-1.2}$	$7.50\substack{+0.19 \\ -0.17}$	$2.524\substack{+0.039\\-0.040}$	261^{+51}_{-59}			
V	Inverted Ordering	$33.56\substack{+0.77 \\ -0.75}$	$8.49\substack{+0.15 \\ -0.15}$	$50.0^{+1.1}_{-1.4}$	$7.50\substack{+0.19 \\ -0.17}$	$-2.514_{-0.041}^{+0.038}$	277^{+40}_{-46}			
Current and future goals:										
Establish whether there is CP violation in the leptonic sector and, if so, measure δ_{CP}										
Improve the accuracy on	θ ₂₃									

Determine the neutrino mass ordering: $m_1 < m_2 < m_3$ or $m_3 < m_1 < m_2$

Many experiments:

- MiniBooNE (concluded), NOvA (running), etc.
- SBN Program: MicroBooNE (running), ICARUS (under construction), SBND (under construction); DUNE (under construction)
- T2K (running), T2HK (under construction)

Accelerator-based neutrino-oscillation experiments



Oscillation Probability: $P(\nu_i \rightarrow \nu_j) = \sin^2 2\theta \sin^2 \left(\frac{\Delta m^2 L}{4E_{\nu}}\right)$

- (i) Detector is too close to the source, no oscillation happened.
- (ii) Necessary but most sensitive region to detect oscillations.
- (iii) Several oscillations happened, only average oscillation probability can be measured.



Accelerator-based neutrino-oscillation experiments



Oscillation Probability: $P(\nu_i \rightarrow \nu_j) = \sin^2 2\theta \sin^2 \left(\frac{\Delta m^2 L}{4E_{\nu}}\right)$

Maximal sensitivity to oscillation probability:

• Maximize the baseline L

Neutrino beam diverges

Minimize the beam energy E_v

Cross section decreases

Optimal combination:

 $L \sim$ few 100s of km $E_v \sim$ Intermediate energies

Event Rates:

$$N_{\rm FD}^{\alpha \to \beta}(\boldsymbol{p}_{\rm reco}) = \sum_{i} \phi_{\alpha}(E_{\rm true}) \times P_{\alpha\beta}(E_{\rm true}) \times \sigma_{\beta}^{i}(\boldsymbol{p}_{\rm true}) \times \epsilon_{\beta}(\boldsymbol{p}_{\rm true}) \times R_{i}(\boldsymbol{p}_{\rm true}; \boldsymbol{p}_{\rm reco})$$

Event Rates:

es:

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$$P(\nu_{i} \to \nu_{j}) = \sin^{2} 2\theta \sin^{2} \left(\frac{\Delta m^{2}L}{4E_{\nu}}\right)$$

Energy reconstruction:



- Neutrino beams are part of tertiary beam neutrino energy is not know.
- The neutrino energy is reconstructed based on the kinematics of the final state particles.
- Using the nuclear model implemented in the Monte Carlo generator.



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Cross section is calculated using the nuclear model implemented in the Monte Carlo generator.

 Monte Carlo generators should consists of a realistic nuclear model that can describe accurately the neutrinonucleus scatterings at the kinematics relevant for these experiments.

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Example from ¹²C (e,e')



VP, PhD thesis (2016)

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Example from ¹²C (e,e')

 The uncertainties in the measurements, mainly owing to inadequate nuclear models in generators, is ~ 10-15 % - No Surprize!



VP, PhD thesis (2016)



Nuclear Theorist's Desk



 In an ideal world: with strong collaboration between neutrino experimentalists and nuclear theorists - we all understand neutrino cross section with high accuracy and make precise oscillations measurements.



And they lived happily ever after...

When nuclear theorists talk to neutrino experimentalists



When neutrino experimentalists talk to nuclear theorists



State of art, unfortunately :-/

My Neutrino Experimentalist's Desk



My Nuclear Theorist's Desk



There's no such thing as multi-tasking – just doing lots of things badly. The correct term is multi-failing.

General cross section formalism:

Leptonic current

$$J_{\mu} = \bar{\nu}_{l} \gamma_{\mu} (1 - \gamma_{5}) l$$

= $\bar{\nu}_{l} \gamma_{\mu} l - \bar{\nu}_{l} \gamma_{\mu} \gamma_{5} l$

Hadronic current

$$J^{\mu} = \bar{u}_{N} \left[\gamma^{\mu} F_{1}(Q^{2}) + \frac{i}{2M_{N}} \sigma^{\mu\nu} q_{\nu} F_{2}(Q^{2}) \right] + \gamma^{\mu} \gamma_{5} F_{A}(Q^{2}) + \frac{1}{2M_{N}} q^{\mu} \gamma_{5} F_{P}(Q^{2}) \right] u_{N}$$



Propagator
$$\approx \frac{1}{Q^2 - M_W^2} \ , \quad Q^2 \ll M_W^2$$

$$\left(\frac{d^2\sigma}{d\omega d\Omega}\right)_{\nu} = \frac{G_F^2 \cos^2\theta_c}{(4\pi)^2} \left(\frac{2}{2J_i+1}\right) \varepsilon_f \kappa_f \quad \zeta^2 \left(Z', \varepsilon_f, |q|\right) \quad \left[\sum_{J=0}^{\infty} \sigma_{CL,\nu}^J + \sum_{J=1}^{\infty} \sigma_{T,\nu}^J\right]$$

$$\sigma_{CL,\nu}^J = \left[v_{\nu}^{\mathcal{M}} R_{\nu}^{\mathcal{M}} + v_{\nu}^{\mathcal{L}} R_{\nu}^{\mathcal{L}} + 2 v_{\nu}^{\mathcal{M}\mathcal{L}} R_{\nu}^{\mathcal{M}\mathcal{L}}\right] \quad \sigma_{T,\nu}^J = \left[v_{\nu}^T R_{\nu}^T \pm 2 v_{\nu}^{TT} R_{\nu}^{TT}\right]$$

$$+/- \text{ sign is the only difference between v and anti-v}$$

General cross section formalism:



v's \rightarrow Leptonic coefficients \rightarrow Purely kinematical \rightarrow Easy to calculate

R's \rightarrow Response functions \rightarrow Nuclear dynamics \rightarrow Need nuclear models to calculate!

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e-A to v-A cross section



CAUTION: CHALLENGES AHEAD

- Monoenergetic beams (E_e known precisely; ω, q can be calculated)
- Hence, different reaction channels can be separated



- E_v has to be reconstructed \rightarrow wide flux
- Hence, difficult to distinguish different reactions channels.
- What experimentalist's measure:

$$\frac{d^2\sigma}{dT_l\cos\theta} = \frac{\sum_j U_{ij}(d_j - b_j)}{\Phi \cdot T \cdot \varepsilon_i \cdot (\Delta T_l, \Delta \cos\theta)_i}$$

• What theorist's calculate:

$$\frac{d^2\sigma}{dT_l \ d \cos\theta} = \frac{1}{\int \Phi(E_v) \ dE_v} \int dE_v \left[\frac{d^2\sigma}{d\omega \ d\cos\theta}\right]_{\omega=E_v-E_l} \Phi(E_v)$$



*There is plenty of data available for e-A scattering over wide range of kinematics and for several nuclei.

Few (many) models:

- RFG+RPA (Martini, Ericson, *et al*)
- RFG+RPA (Nieves, *et al*)
- HF+CRPA (Pandey, Jachowicz *et al*)
- Spectral Function Formalism (Benhar, Rocco, Ankowski, et al.)
- Super-Scaling approach (Amaro, Barbaro, Caballero, Donnelly, Megias, et al.)
- Relativistic Green's Function Model (Meucci, Giusti *et al.*)
- Green's Function Monte Carlo Approach (Lovato, Gandolfi, Carlson, et al.)
- ..., *etc*.

Formalism: HF-CRPA Approach

<u>References</u>: PRC 89, 024601 (2014); PRC 92, 024606 (2015); PRC 94, 015501 (2016); PRC 94, 024611 (2016); PRC 94, 054609 (2016); arXiv:1612.05511 [nucl-th] (accepted in PRD); arXiv:1704.07817 [nucl-th]

- We start by describing the nucleus with a Hartree-Fock (HF) approximation. The mean-field (MF) potential is obtained by solving the HF equations and using a Skyrme (SkE2) two-body interaction.
- Once we have bound and continuum single-nucleon wave functions, we introduce long-range correlations between the nucleons through a continuum Random Phase Approximation (CRPA).
- The propagation of particle-hole pairs in the nuclear medium is described by the polarization propagator. In the Lehmann representation, this particle-hole Green's function is given by

$$\Pi(x_{1}, x_{2}, x_{3}, x_{4}; E_{x}) = \hbar \sum_{n} \left[\frac{\langle \Psi_{0} | \hat{\psi}^{\dagger}(x_{2}) \hat{\psi}(x_{1}) | \Psi_{n} \rangle \langle \Psi_{n} | \hat{\psi}^{\dagger}(x_{3}) \hat{\psi}(x_{4}) | \Psi_{0} \rangle}{E_{x} - (E_{n} - E_{o}) + i\eta} - \frac{\langle \Psi_{0} | \hat{\psi}^{\dagger}(x_{3}) \hat{\psi}(x_{4}) | \Psi_{n} \rangle \langle \Psi_{n} | \hat{\psi}^{\dagger}(x_{2}) \hat{\psi}(x_{1}) | \Psi_{0} \rangle}{E_{x} + (E_{n} - E_{o}) - i\eta} \right]$$

• RPA equations are solved using a Green's function approach.

• The RPA-polarization propagator

$$\Pi^{(RPA)}(x_1, x_2; E_x) = \Pi^{(0)}(x_1, x_2; E_x) + \frac{1}{\hbar} \int dx dx' \ \Pi^0(x_1, x; E_x) \\ \times \tilde{V}(x, x') \ \Pi^{(RPA)}(x', x_2; E_x)$$



• The Skyrme (SkE2) nucleon-nucleon interaction, which was used in the HF calculations, is also used to perform CRPA calculations. That makes this approach self-consistent.

Formalism: Folding procedure

A limitation of RPA formalism at lower energies:

- ightarrow energy position of the giant resonances is generally well predicted
- ightarrow width is underestimated
- \rightarrow height is overestimated





Formalism: Relativistic corrections

Non-relativistic model

'Semi-relativistic' modeling

(S. Jeschonnek and T. W. Donnelly, PRC57, 2438 (1998))

Kinematic effects:

 $\lambda \rightarrow \lambda (1+\lambda), \quad \lambda = \omega/2M_N$

QE peak: $\omega = q^2/2M_N => Q^2/2M_N$



Formalism: Regularization of the residual interaction

SkE2 interaction → optimized against ground-state and low-excitation energy properties → at higher Q², unrealistically strong!

$$V(Q^2) = V(Q^2 = 0) \frac{1}{(1 + \frac{Q^2}{\Lambda^2})^2}$$

With $\Lambda = 455$ MeV, optimized with a χ^2 fitting of theory-experiment comparison from low ω up to the QE peak, over broad set of available data on A(e,e') scattering.



Formalism: Coulomb correction

Effect of coulomb potential of the nucleus on the charged lepton:

 \rightarrow High energies:

Modified effective momentum approximation

(J. Engel, PRC57,2004 (1998))

$$q_{\rm eff} = q + 1.5 \left(\frac{Z' \alpha \hbar c}{R}\right)$$
$$\zeta(Z', E, q) = \sqrt{\frac{q_{\rm eff} E_{\rm eff}}{q E}}$$





Comparison with neutrino data





Comparing RPA-based models $\Pi = \Pi^0 + \Pi^0 V \Pi$

RPA polarization propagator:

Comparing RPA-based models



Comparing RPA-based models



- At low ω, RPA (long-range correlations) describes the collective behavior of the nucleus (low-energy excitations).
- At high ω, RPA effects are smaller.
- Approach compares well with the (e,e') cross section.

Comparing RPA-based models

For more details: M. Martini, N. Jachowicz, M. Ericson, and VP et al., PRC 94, 015501 (2016)

LRFG, RPA: Martini, Ericson et al.

HF, CRPA: Pandey, Jachowicz et al.

- Important differences at both ends of the spectrum
 - \rightarrow Low-energy excitations at low ω
 - \rightarrow High ω tail



Comparing RPA-based models

Model	Starting point	N-N interaction	Shell effects	Low-energy excitations & Giant resonances	RPA effect
Martini, Ericson <i>et al</i> .	Local Fermi Gas	Meson -exhange (π,ρ,g')	No	No	Significant suppression (LLEE effect*)
Nieves <i>et al</i> .	Local Fermi Gas	Meson -exhange (π,ρ,g')	No	No	Significant suppression (LLEE effect*)
Pandey, Jachowicz <i>et al</i> .	Hartree-Fock	Skyrme	Yes	Yes	Describes low ω physics, not much effects at higher ω

- Significant differences between RPA and CRPA approach, at both ends of the (one-body) ω spectrum.

What neutrino brings: E_{ν}

Cross section (integrated over full phase-space) in terms of incoming neutrino energy E_{v} .





Response

 Q^2

Cross section (integrated over full phase-space) in terms of incoming neutrino energy E_{v} .

 $\omega = 50 \text{ MeV}$

QE

 N^{\star}

Nucleon

GR: Giant Resonance

ω

Elastic

GR

Elastic

300 MeV

W

 $\frac{Q^2}{2M_N}$



For a given E_v , it depends on other factors, such as on lepton scattering angle.

What is missed in the translation.



 Q^2

Low E_v : cross section is dominated by low-energy excitations.

 E_v at the peak of MicroBooNE/T2K, forward scattering receive contribution from low-energy excitations.

300 MeV



Low E_{v} : cross section is dominated by low-energy excitations.

 E_v at the peak of T2K flux, forward scattering receive contribution from low-energy excitations.

- The forward we go in scattering angle, longitudinal contribution starts competing with the transverse one (at intermediate energy).
- At low-energies and forward scattering, longitudinal response dominates over transverse one.



VP, N. Jachowicz et al, PRC 92, 024606 (2015)

Does it affect the flux-folded cross section? And how much?





How does RgFG model describes low-energy excitations – it does not!



Example from ${}^{12}C(e,e')$



The effect of low-energy nuclear excitations on $v_e vs v_{\mu}$ cross section

M. Martini, N. Jachowicz, M. Ericson, and VP et al., PRC 94, 015501 (2016)

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M. Martini, N. Jachowicz, M. Ericson, and VP et al., PRC 94, 015501 (2016)

The effect of low-energy nuclear excitations on $v_e vs v_{\mu}$ cross section



Low-energy nuclear excitations are vital

- At low E_v
- At intermediate E_{ν} and forward scattering
- Differentiating between v_e and v_{μ} cross section (at low E_v)





• Accelerator-based neutrino-oscillation program, for the precision measurement of neutrino oscillation parameters and hopefully establishing cp violation in leptonic sector, is moving with full steam.



• There are still major issues related to identification of basic processes contributing to the neutrino-nucleus signal in a detector and the reduction of systematic uncertainties.





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- A number of theoretical efforts to model neutrino-nucleus interactions at the kinematics relevant for the neutrinooscillation experiments.
- The Monte-Carlo generators are still based on inadequate models and implementing new models into current generators is complex and slow.





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 Next generation experiments (MicroBooNE, ICARUS, SBND, and DUNE) employ LArTPC technology but a little (almost nonthing) is known about Ar nucleus and its electroweak response.



 A new Ar(e,e'p) experiment at Jlab (was recently approved and now also already finished collecting data) will provide spectroscopic factors and cross sections on Ar.