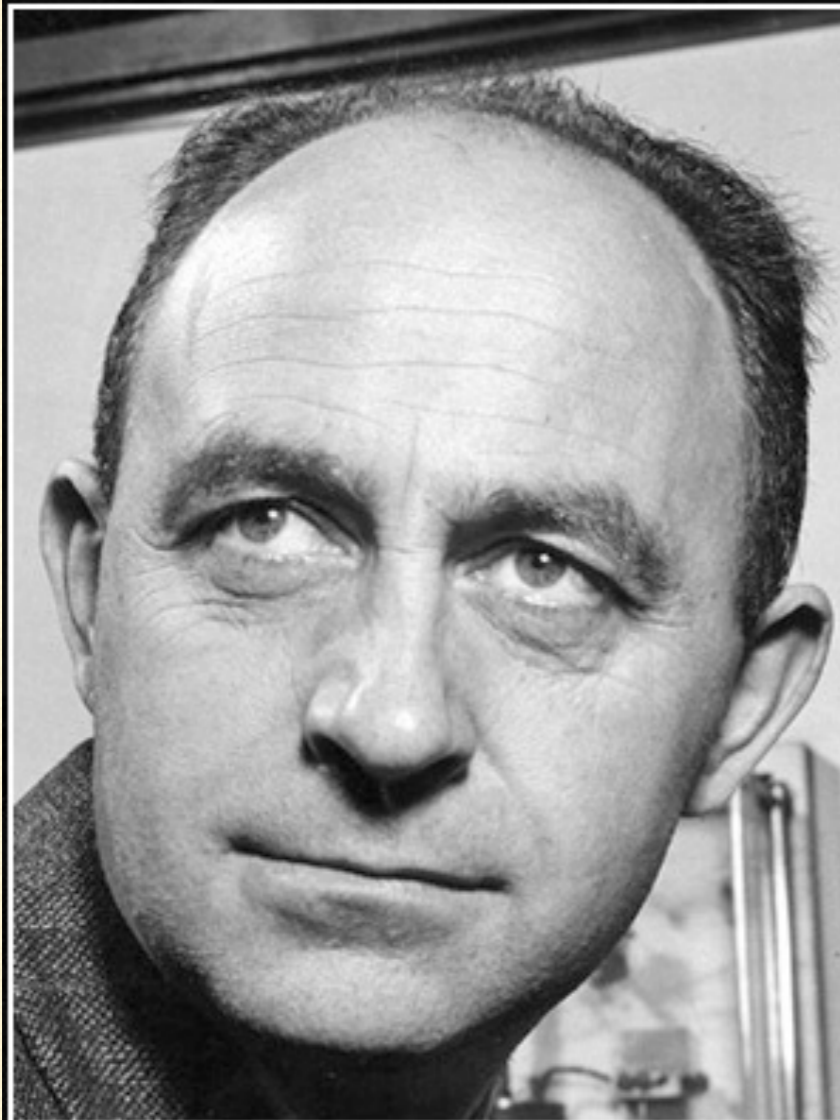

NUCLEAR EFFECTS IN NEUTRINO STUDIES

Joanna Sobczyk

June 28, 2017, Trento



Uniwersytet
Wrocławski



Never underestimate the joy people
derive from hearing something they
already know.

— *Enrico Fermi* —

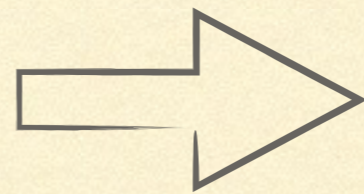
AZ QUOTES



**REPETITIO
EST
MATER
STUDIORUM**

OUTLINE

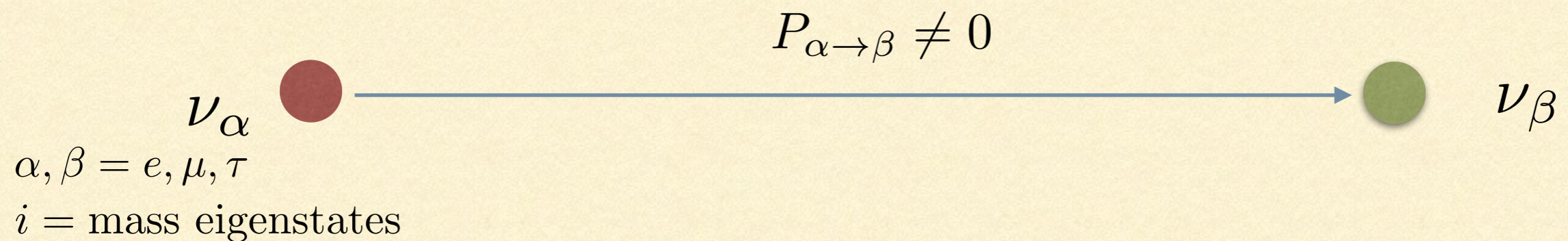
- Motivation: neutrino physics
- Neutrino oscillation experiments: why nuclear physics is important
- Lepton-nucleus scattering: quasielastic mechanism
 - Fermi Gas model
 - Additional nuclear effects
- Conclusions



Comparison

NEUTRINO OSCILLATIONS

- Neutrinos change their “identity” because mass eigenstates are not flavour eigenstates



$$|\nu_i\rangle = \sum_{\alpha} U_{i,\alpha} |\nu_\alpha\rangle$$

different basis

$$|\nu_i(t)\rangle = e^{-i(Et - \vec{p}\vec{x})} |\nu_i(0)\rangle$$

mass eigenstates propagate

NEUTRINO OSCILLATIONS

$$P_{\alpha \rightarrow \beta} = |\langle \nu_{\alpha}(t) | \nu_{\beta} \rangle|^2 = \left| \sum U_{\alpha i}^* U_{\beta i} e^{-im_i^2 L/2E} \right|^2$$

■ PMNS matrix:

$$\begin{pmatrix} \nu_e \\ \nu_{\mu} \\ \nu_{\tau} \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

- There are 6 parameters in the SM which influence oscillations.
- Various oscillation experiments are sensitive to different parameters (we can play with L and E)

EXPERIMENTS

$$P_{\alpha \rightarrow \beta} = \sin^2(2\theta) \sin^2 \left(1.27 \frac{\Delta m^2 L [eV^2][km]}{E [GeV]} \right)$$

given by the experimental setup

At the experiment one has to:

- distinguish events that are triggered by different neutrino types
- be able to make energy reconstruction to get E (neutrino beams are not monoenergetic!)

NEUTRINO PHYSICS - OPEN QUESTIONS

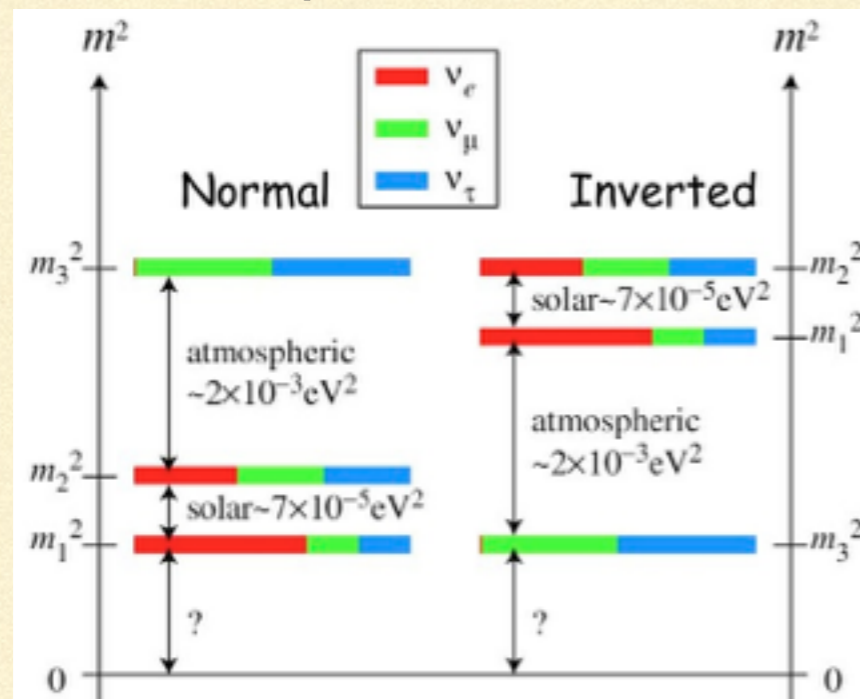
■ STANDARD MODEL

$$\sin^2(2\theta_{13}) = 0.093 \pm 0.008$$

$$\sin^2(2\theta_{12}) = 0.846 \pm 0.021$$

$$\sin^2(2\theta_{23}) > 0.92$$

- CP violation phase - still big uncertainty



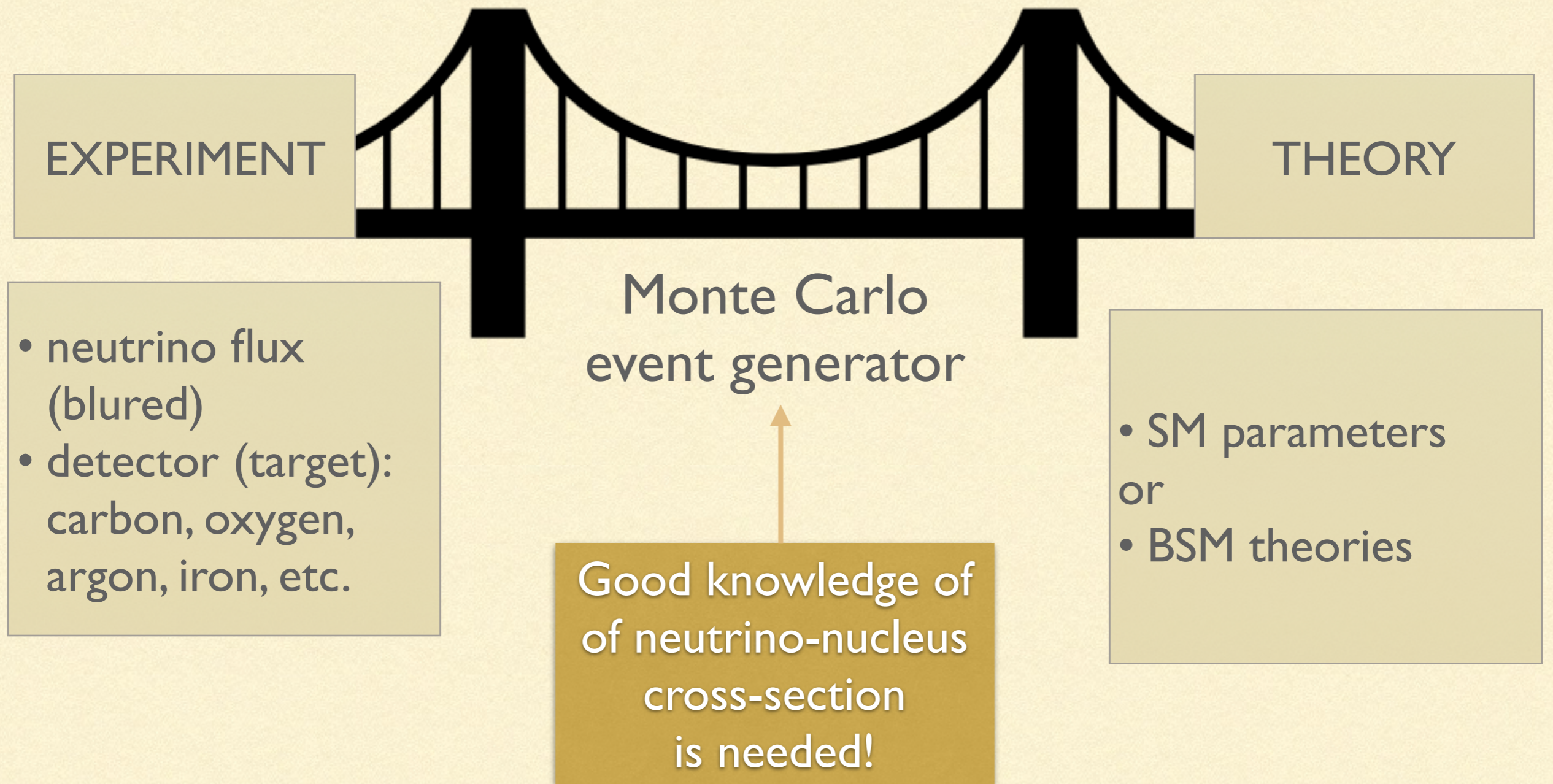
■ BEYOND STANDARD MODEL

- sterile neutrinos?
- more flavours?

Which model is correct?

*Further question: are neutrino Majorana particles?
But this cannot be answered by neutrino oscillation experiments.*

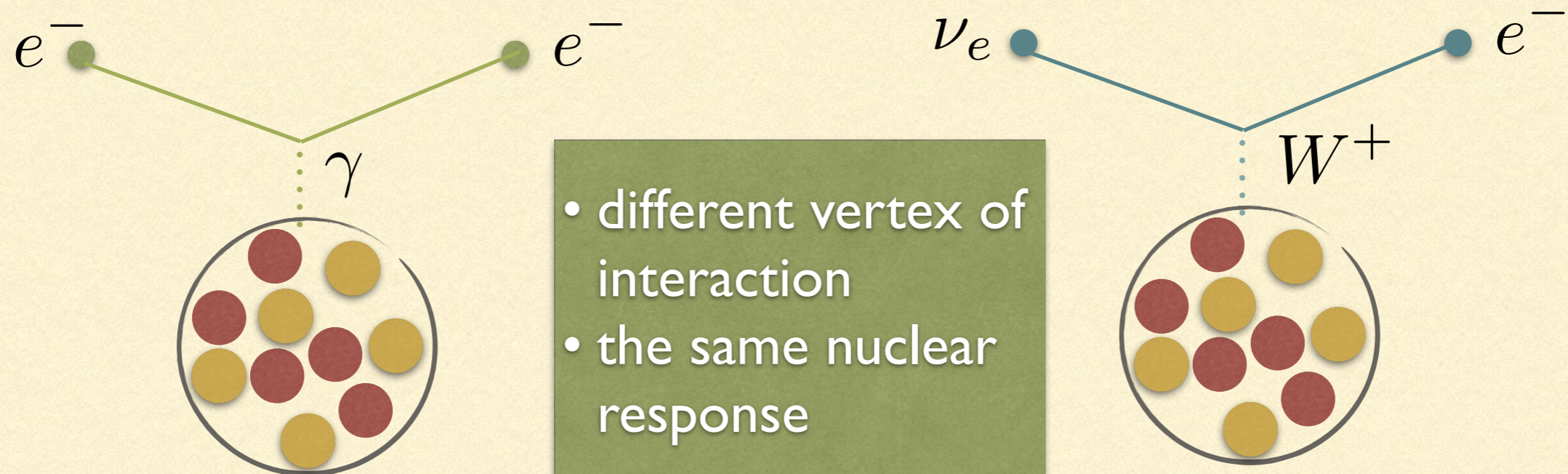
EXPERIMENT - THEORY



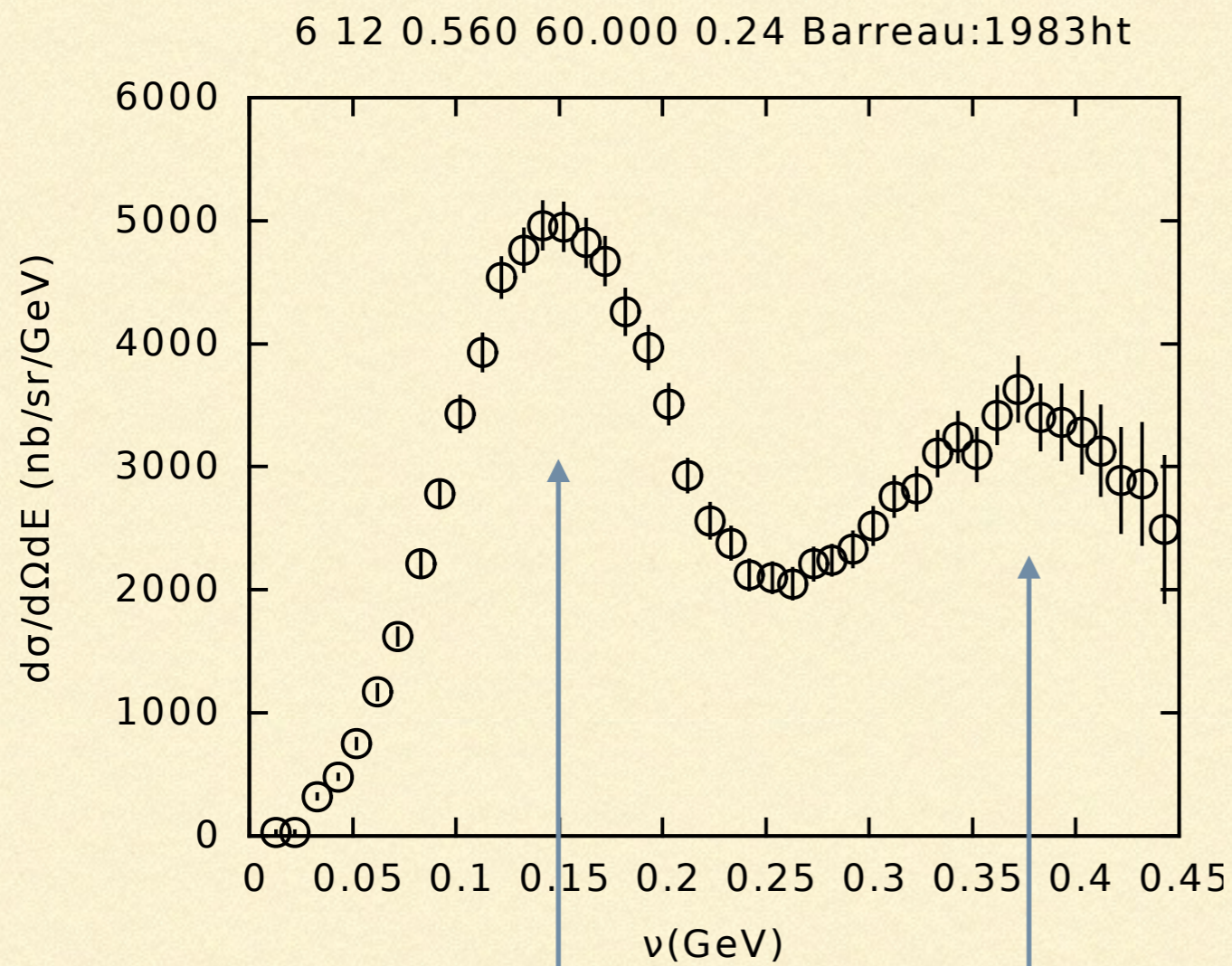
NEUTRINO-NUCLEUS CROSS SECTION

We need a precise model to calculate cross-section for neutrino scattering of various nuclei (carbon, oxygen, argon...)

We can check the models for electron scattering instead of neutrino scattering (much more data!)

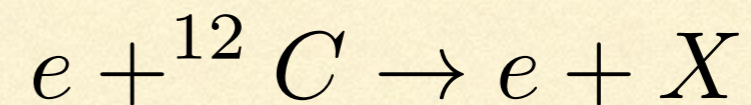


INCLUSIVE CROSS SECTION



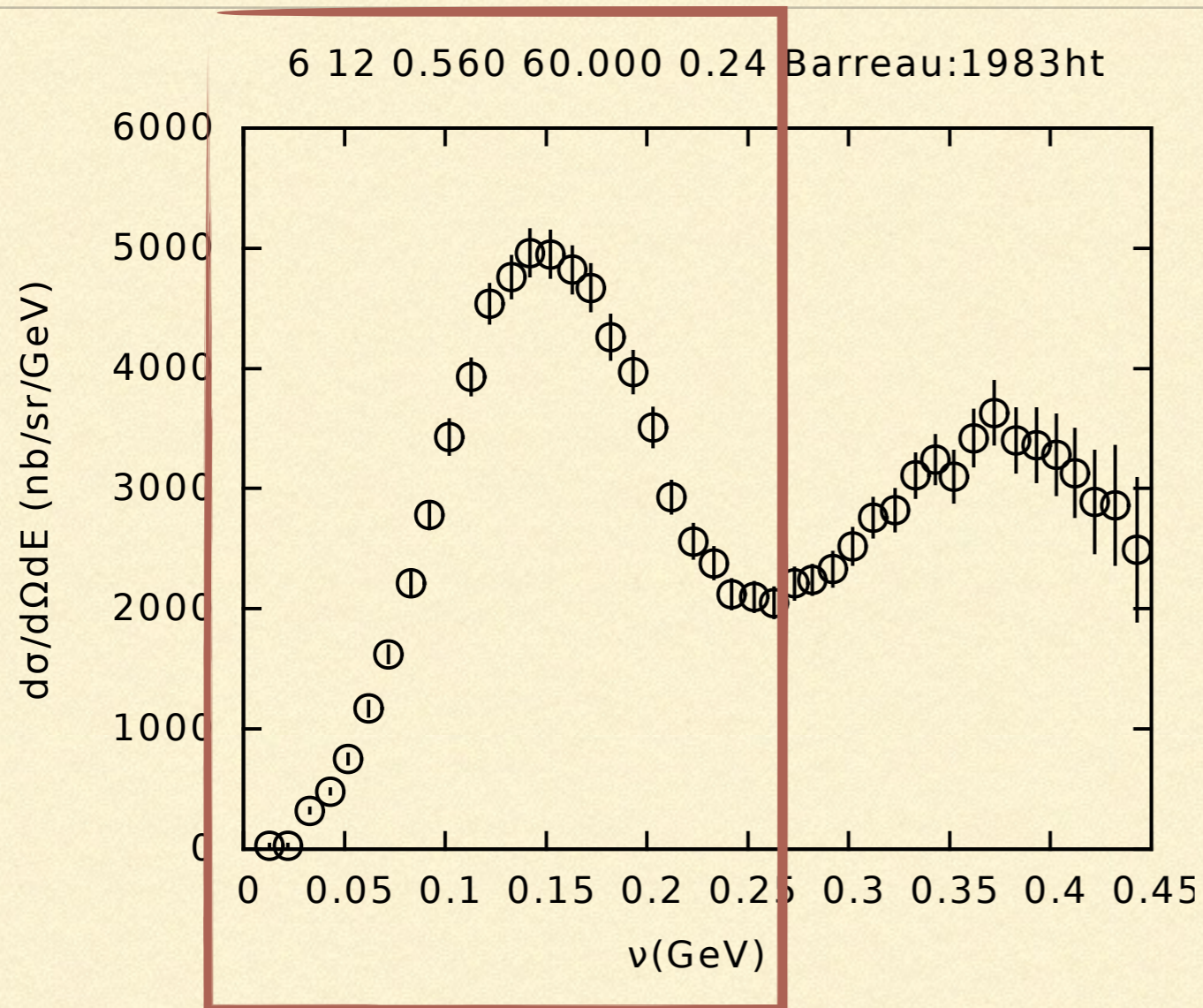
Different dynamic mechanisms

We have precise data for
the electron scattering



$E=560$ MeV, $\theta=60^\circ$

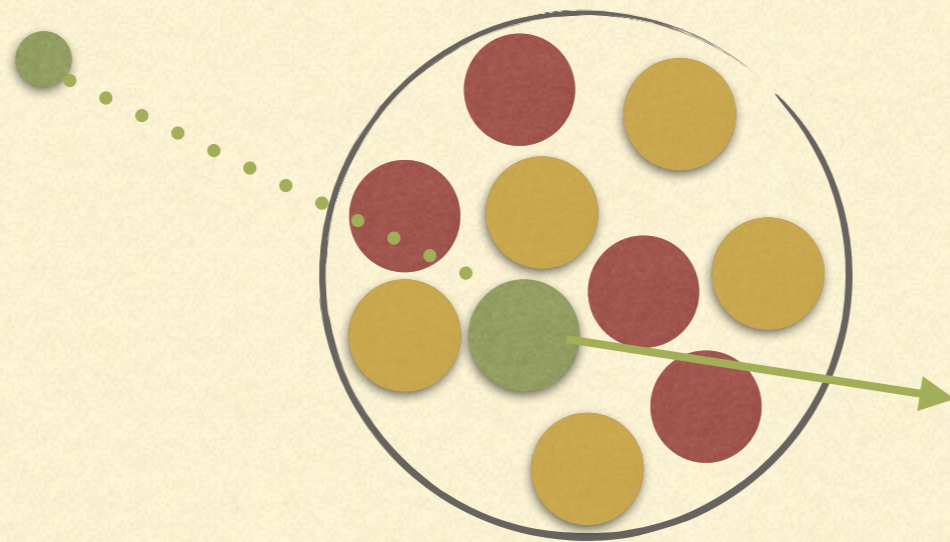
CROSS SECTION



QUASIELASTIC MECHANISM

QUASIELASTIC MECHANISM

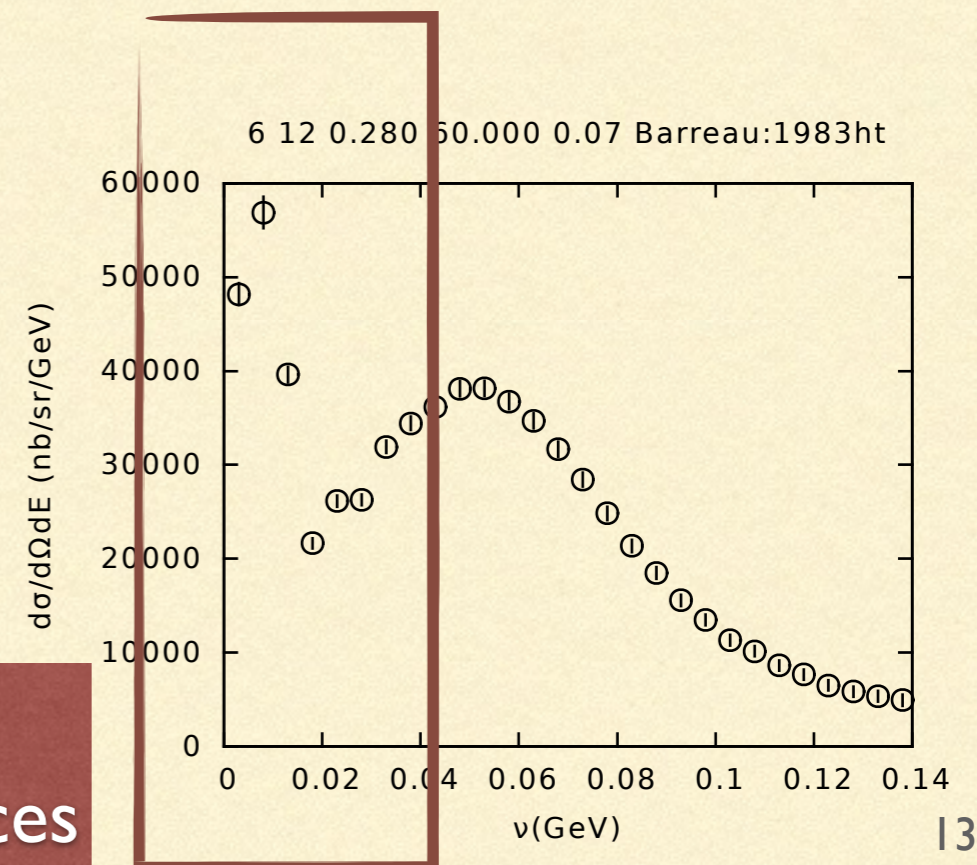
lepton



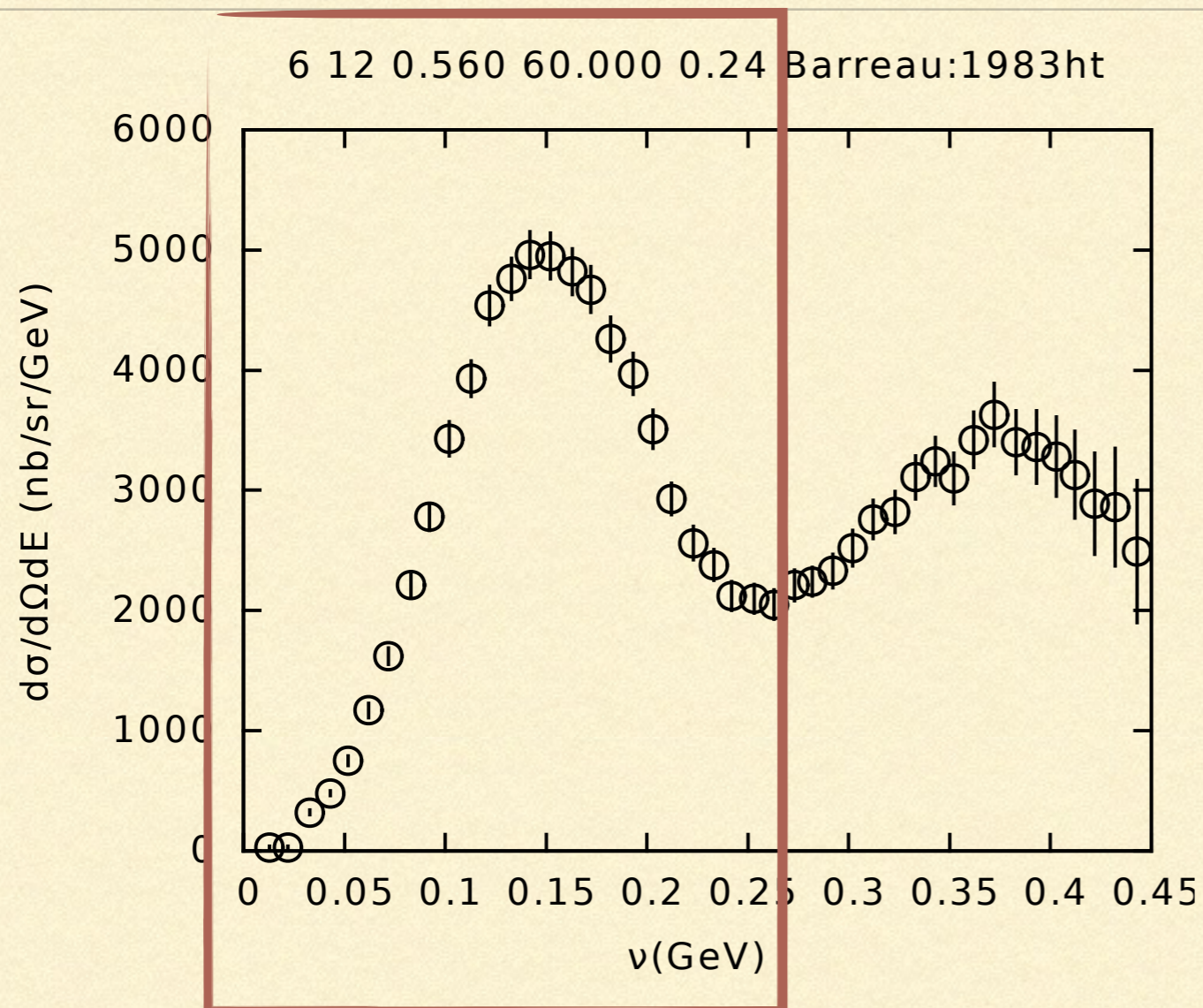
Impulse Approximation:
only one interacting
nucleon

It is correct
if momentum transfer
~ inter-nucleons distance
in nuclei
 $1 \text{ fm} = 200 \text{ MeV}/c$

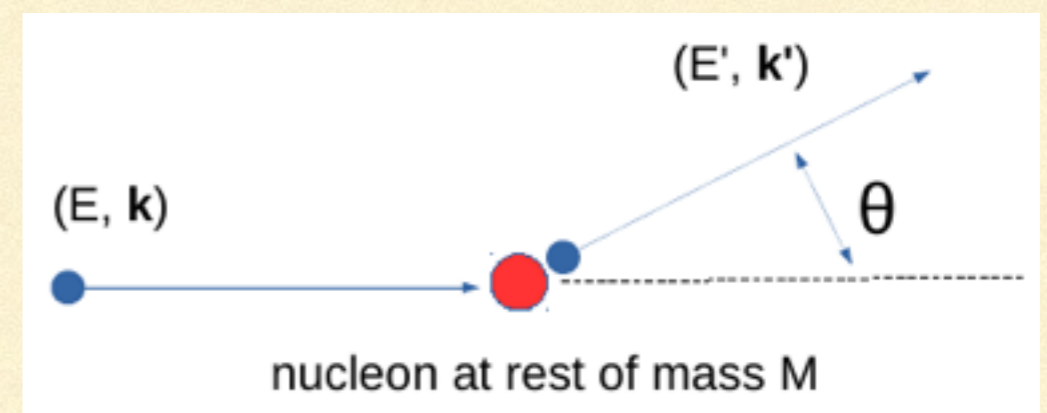
giant
resonances



QE PEAK'S POSITION



Suppose the elementary process is $eN \rightarrow eN$.

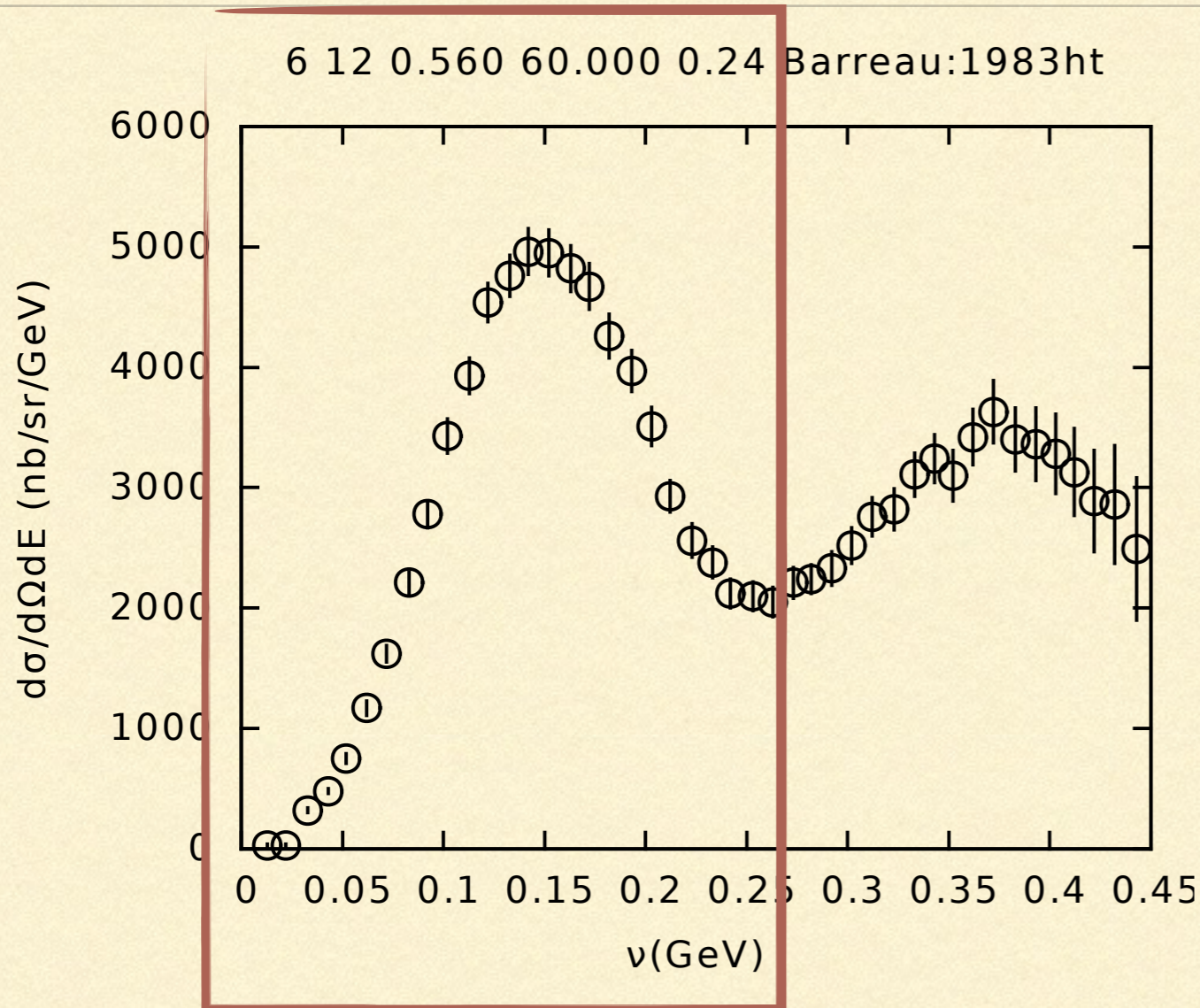


Energy-momentum conservation

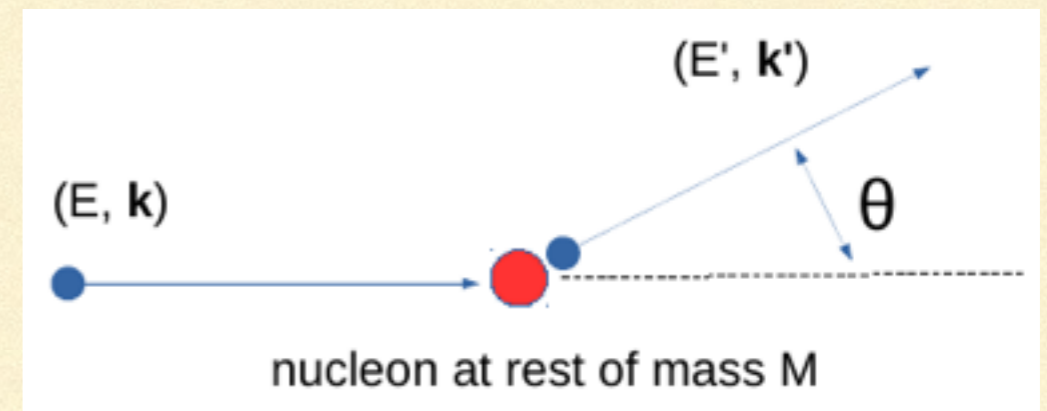
$$\nu = \frac{4E^2 \sin^2 \frac{\theta}{2}}{2M + 4E \sin^2 \frac{\theta}{2}} \Rightarrow \nu = 129 \text{ MeV}$$

QUASIELASTIC MECHANISM

QE PEAK'S POSITION



Suppose the elementary process is $eN \rightarrow eN$.

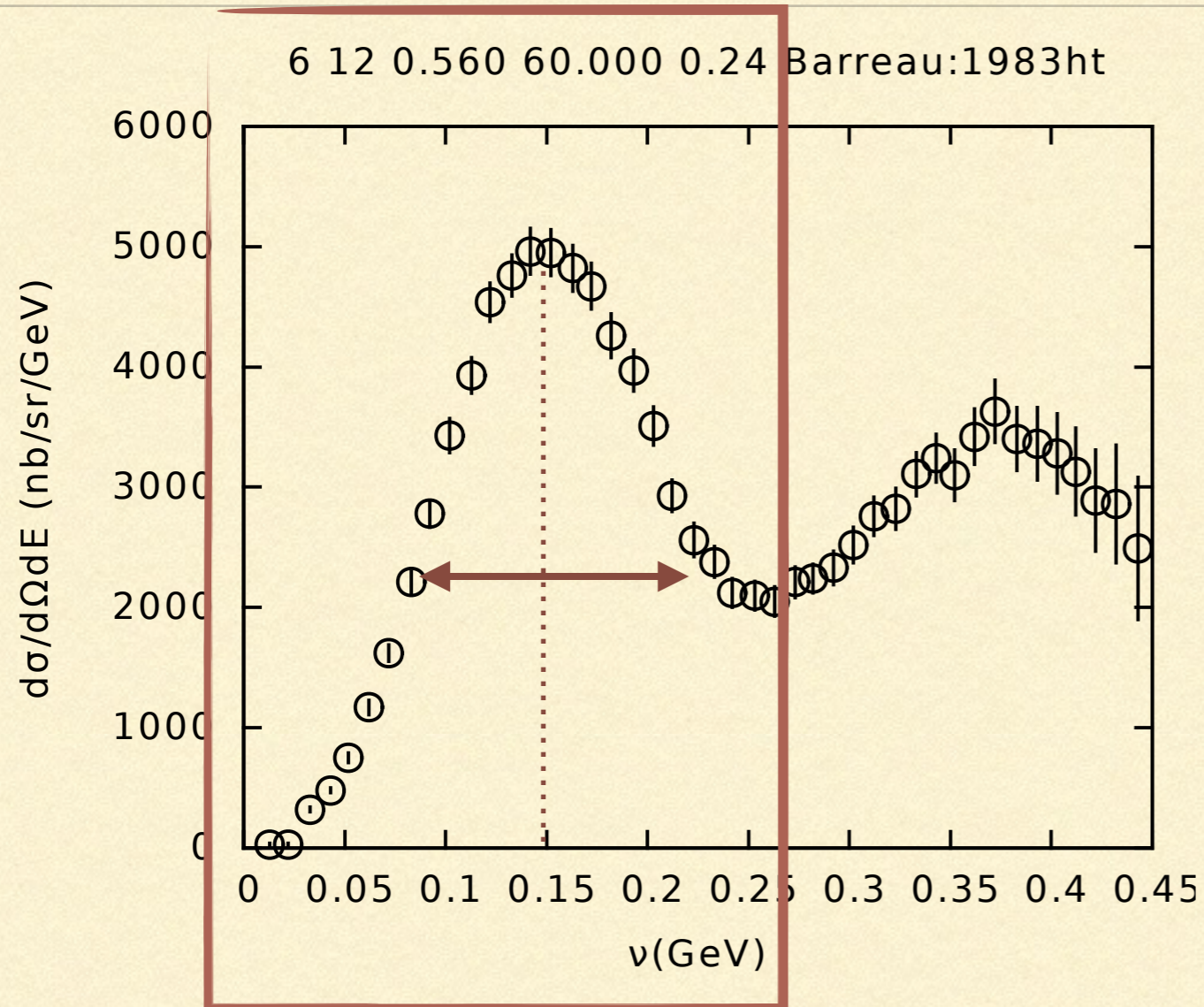


Energy-momentum conservation

$$\nu = \frac{4E^2 \sin^2 \frac{\theta}{2} + 2MB - B^2}{2M - 2B + 4E \sin^2 \frac{\theta}{2}}, \quad B = 25\text{MeV} \rightarrow \nu = 150\text{MeV}$$

binding energy

QE PEAK'S WIDTH



- Peak's width arises due to Fermi motion
- Peak's width tells us about the Fermi momentum

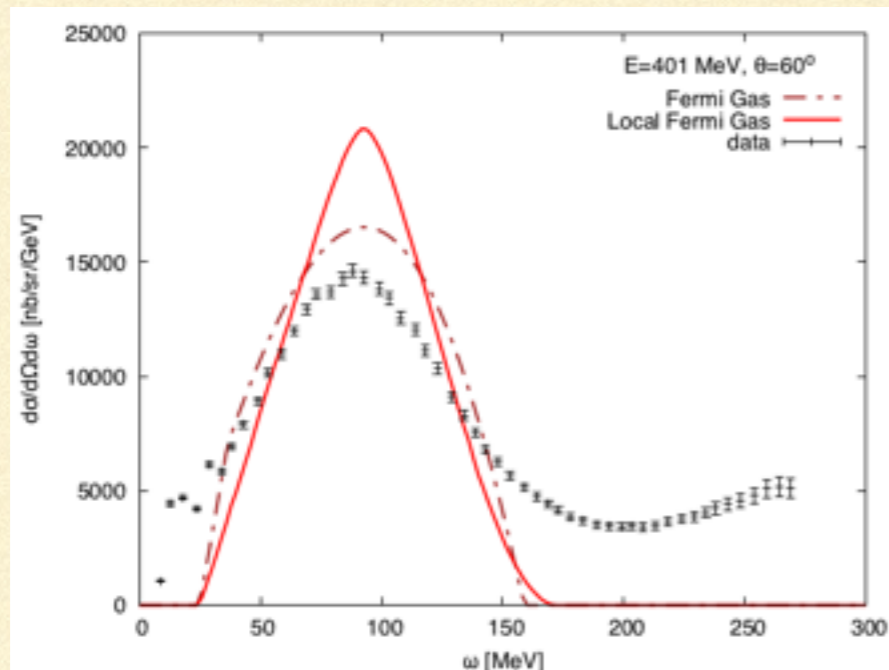
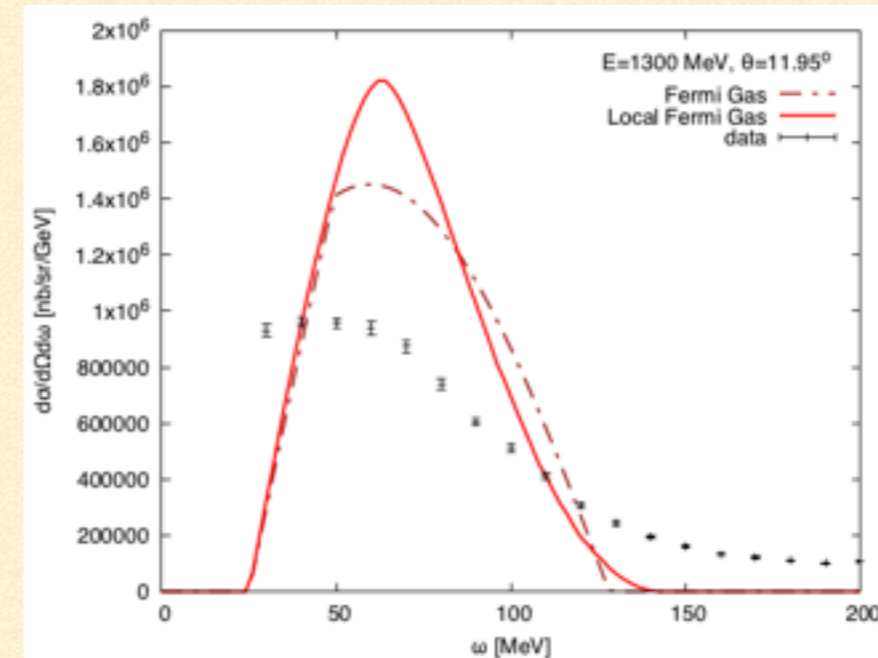
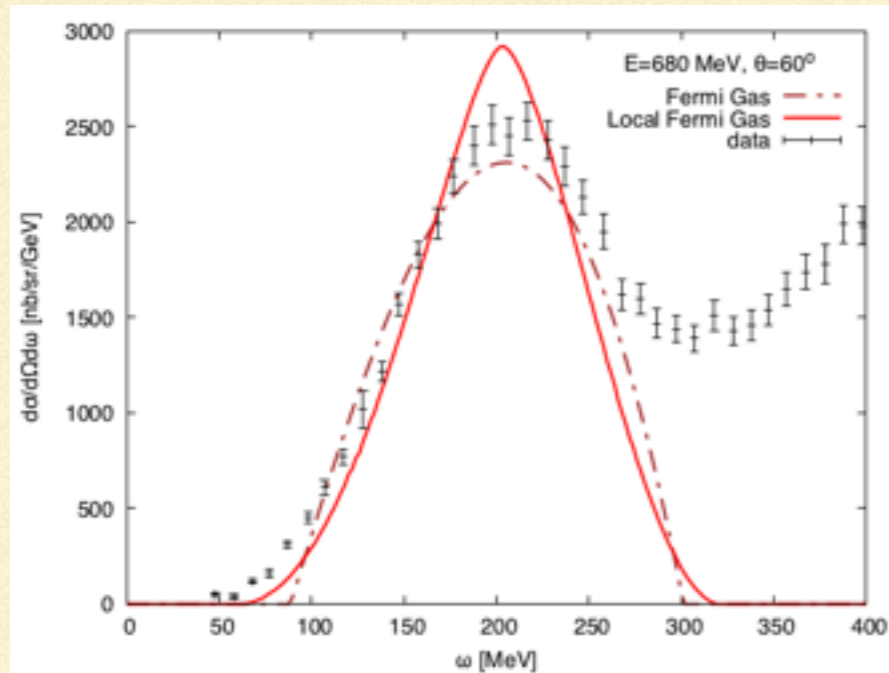
FERMI GAS

- The most basic approach:
statistical correlations + constant binding energy

$$\mathcal{H} = \sum_{i \in \text{nucleons}} \frac{p_i^2}{2M}$$

- We know with a very good precision how describe the interaction $e^- + N \rightarrow e^- + N$
- For neutrinos there is a room for improvement (axial form-factor)

FERMI GAS



Clearly, it is not possible to find a good parametrisation (binding energy and Fermi momentum) in terms of (L)FG

TURN-ON INTERACTION

- We need to employ a more sophisticated model for nucleons in the nuclei.

non-relativistic
propagator:

$$\mathcal{G}(E, p, \rho) = \frac{1}{E - \frac{p^2}{2M} - \Sigma(E, p, \rho)}$$

we include
the SELF-ENERGY
which is complex

$\text{Im}\Sigma(E, p)$ - particle
width

SPECTRAL FUNCTION

This is described by means of a spectral function:

$$E < \mu \quad S_h(E, p) = \frac{1}{\pi} \text{Im}G(E, p)$$

$$E > \mu \quad S_p(E, p) = -\frac{1}{\pi} \text{Im}G(E, p)$$

$$S_{h/p}(E, p) = \pm \frac{1}{\pi} \frac{\text{Im}\Sigma(E, p)}{[E - p^2/2M - \text{Re}\Sigma(E, p)]^2 + [\text{Im}\Sigma(E, p)]^2}$$

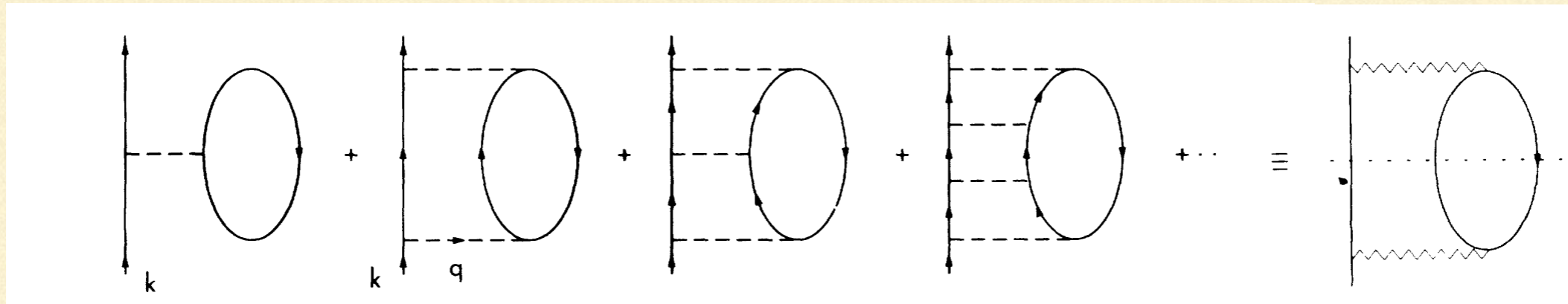
It can be shown that hole spectral function is the probability density for removing a particle with momentum k , with the removal energy E from the ground state.

E. OSET AND F. DE CORDOBA

SEMIPHENOMENOLOGICAL MODEL

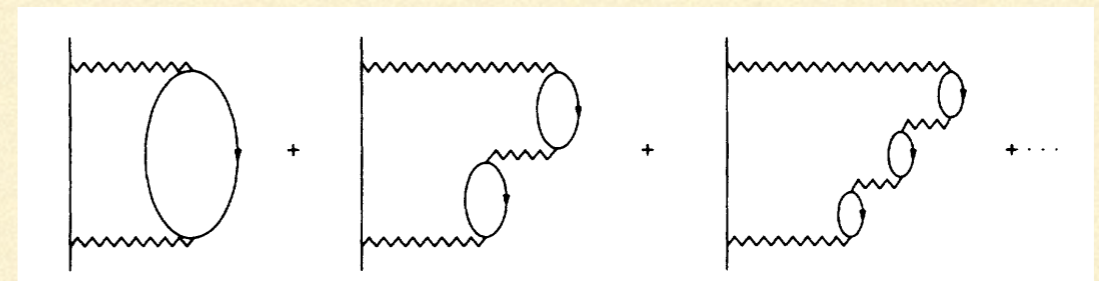
- A simple, semi-phenomenological approach to calculate nucleon self-energy in nuclear matter
 - We calculate the SF for the infinite nuclear matter at constant density. Then we use LDA (local density approximation), meaning we integrate SF with a density profile function to model the nucleus.
 - The calculation is non-relativistic which is OK for the hole SF but might be poor for the particle SF.
-

E. OSET AND F. DE CORDOBA SEMIPHENOMENOLOGICAL MODEL

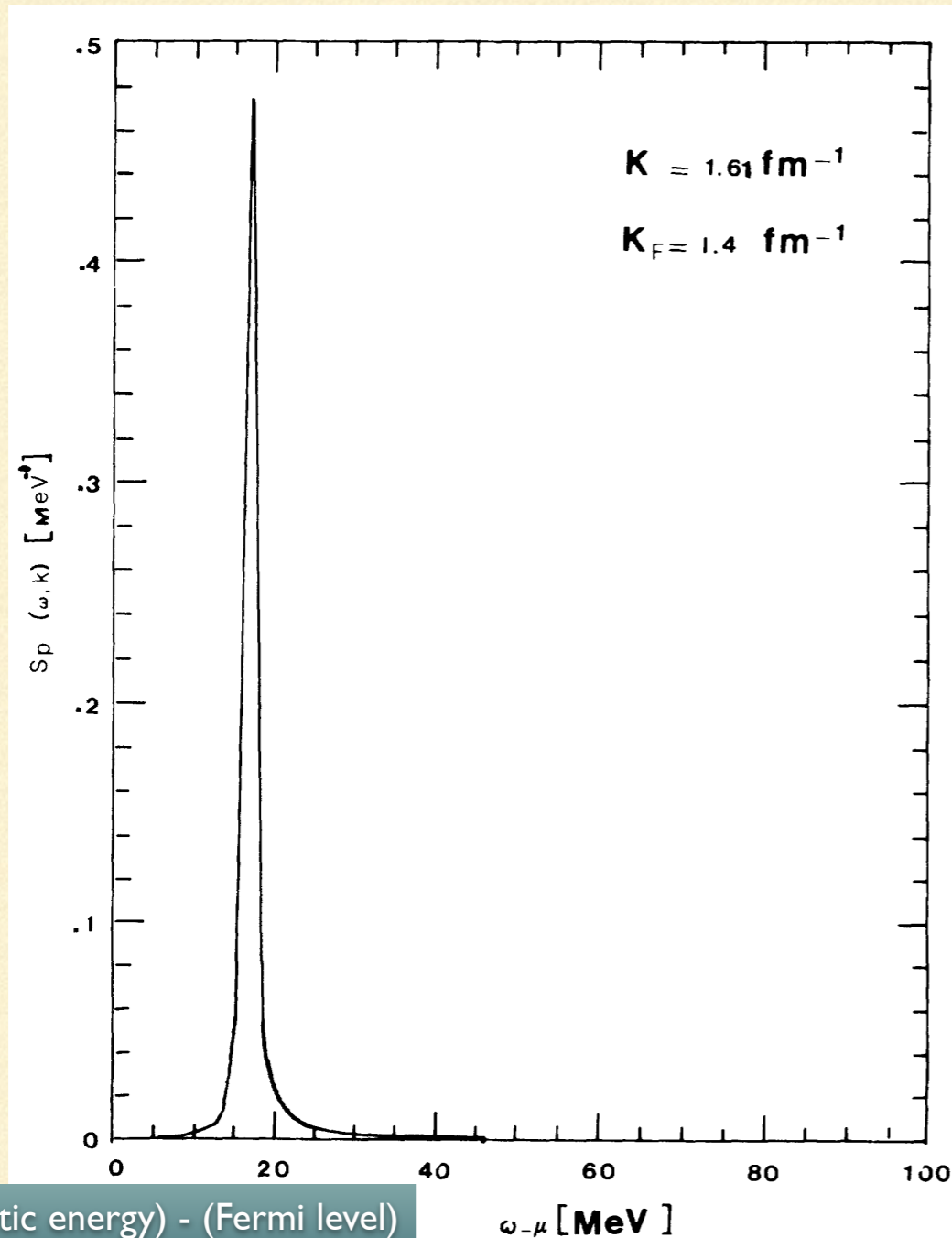


(F. de Cordoba, E. Oset, PRC 46, 5)

- calculate the nucleon self-energy by summing Lippmann-Schwinger series
- approximate t matrix with the free NN scattering matrix (average over angles \rightarrow use NN cross section)
- the density modifications will come from medium polarization



SPECTRAL FUNCTION



(kinetic energy) - (Fermi level)

$\omega - \mu$ [MeV]

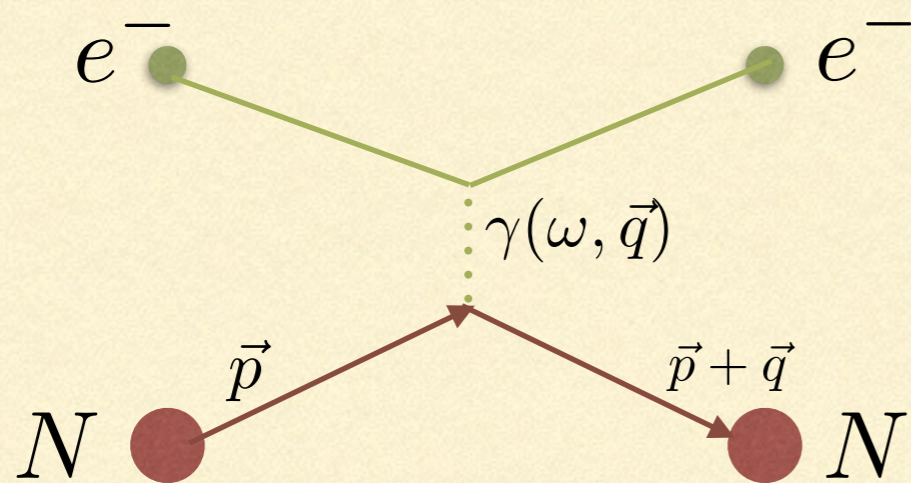
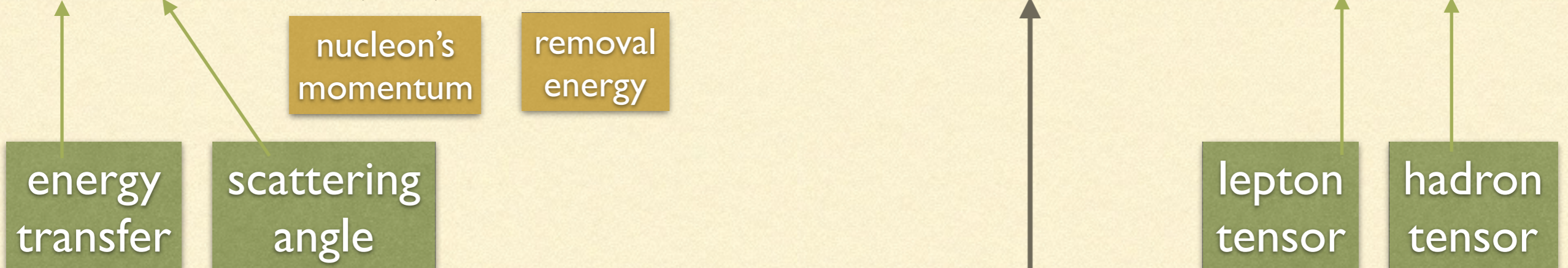
Particle spectral function at a density such that Fermi momentum $k_F = 1.4 \text{ fm}^{-1} = 280 \text{ MeV}$

For a particle of momentum $k = 1.61 \text{ fm}^{-1} = 320 \text{ MeV}$ the largest probability is for kinetic energy $\sim 17 \text{ MeV}$ higher than the Fermi level

(F. de Cordoba, E. Oset, PRC 46, 5)

SPECTRAL FUNCTIONS IN THE CROSS-SECTION

$$\frac{d\sigma}{d\omega d\Omega} = \int \frac{d^3p}{(2\pi)^3} \int dE S_h(E, \vec{p}) S_p(\omega - E, \vec{p} + \vec{q}) L_{\mu\nu} W^{\mu\nu}$$



For large energy-momentum transfer this nucleon becomes relativistic...

SPECTRAL FUNCTIONS IN THE CROSS-SECTION

$$\frac{d\sigma}{d\omega d\Omega} = \int \frac{d^3p}{(2\pi)^3} \int dE S_h(E, \vec{p}) S_p(\omega - E, \vec{p} + \vec{q}) L_{\mu\nu} W^{\mu\nu}$$

This is difficult to calculate numerically so some approximations can be done, e.g.

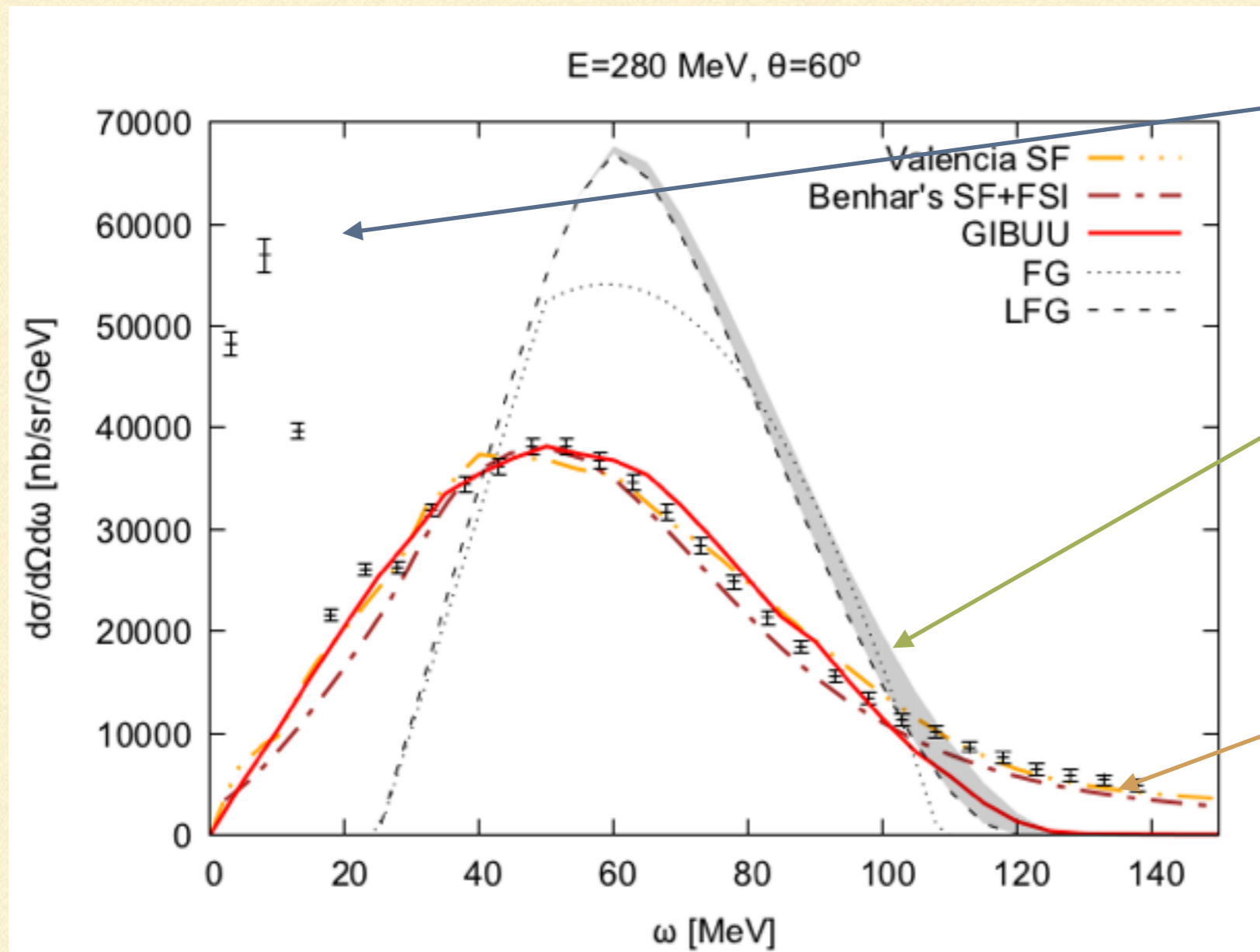
$$S_{h/p}(E, p) = \pm \frac{1}{\pi} \frac{\text{Im}\Sigma(E, p)}{[E - p^2/2M - \text{Re}\Sigma(E, p)]^2 + [\text{Im}\Sigma(E, p)]^2}$$

neglect the width: $\text{Im}\Sigma(E, p) \rightarrow 0$

$$S_h \propto \delta(E - \bar{E}(p)) \theta(\mu - E)$$

$$\bar{E}(p) = \frac{p^2}{2M} - \text{Re}\Sigma(\bar{E}(p), p)$$

RESULTS

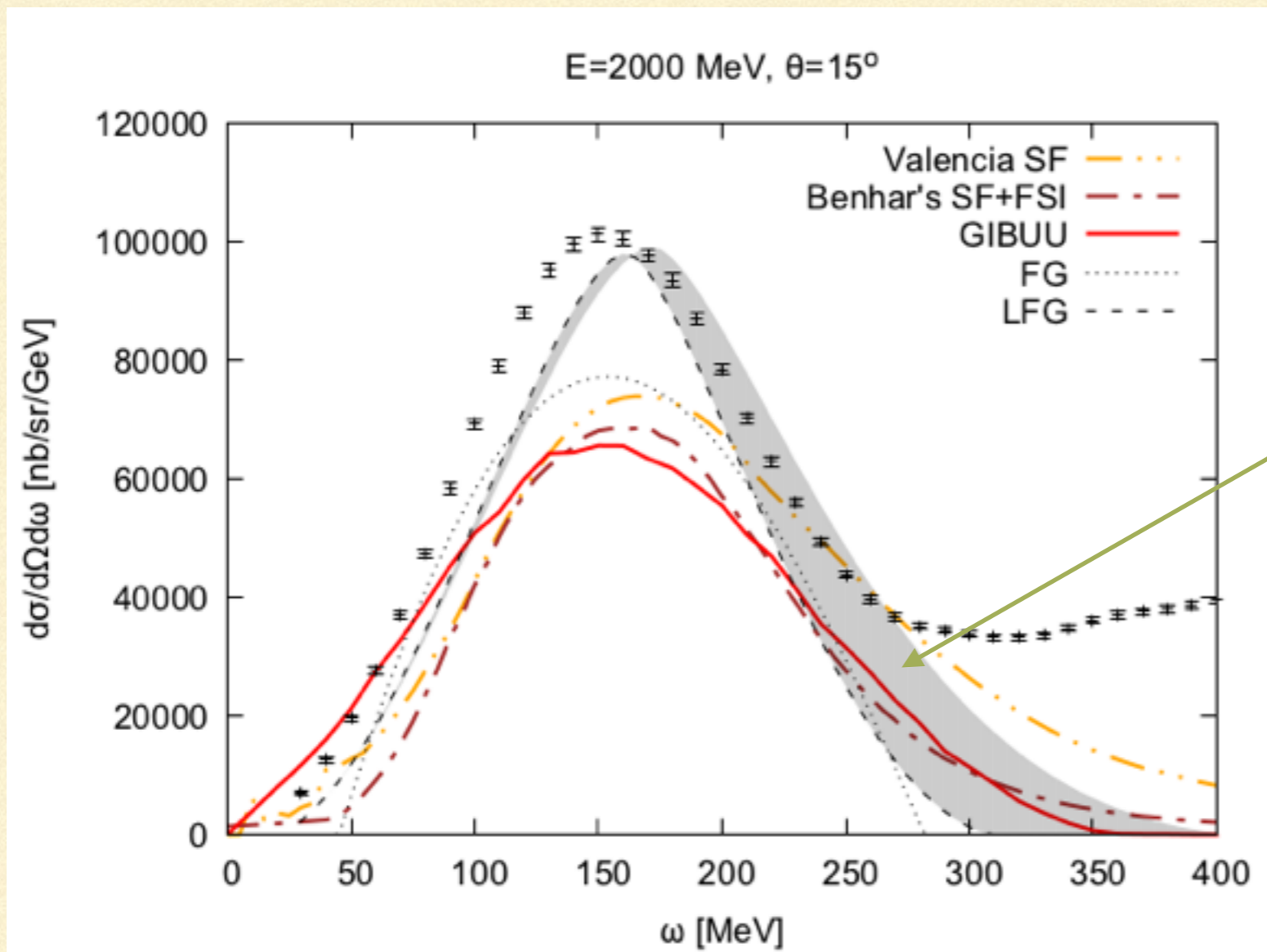


giant resonances
not reproduced

relativistic effects
are small

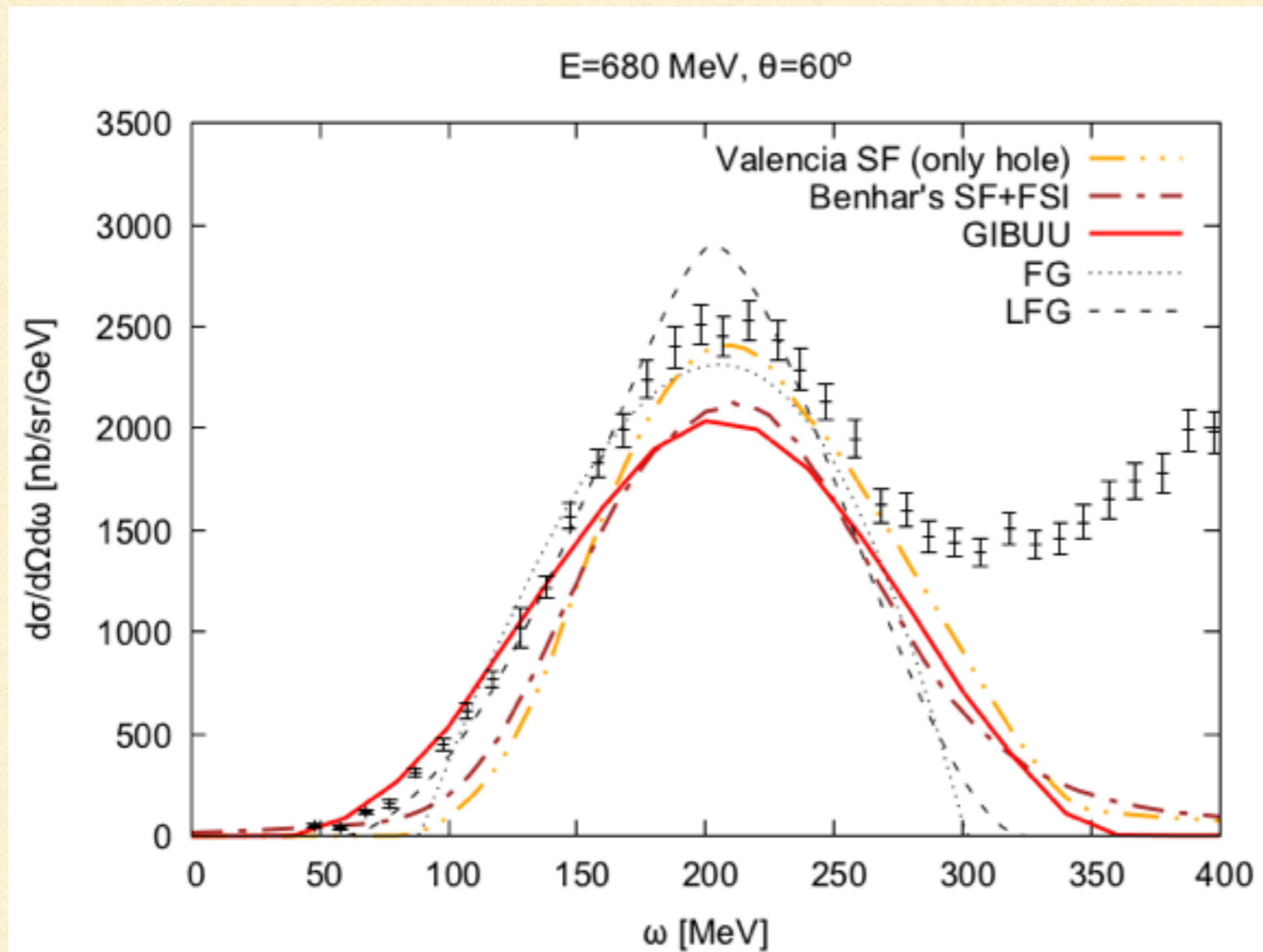
the long tail
comes from
imaginary part
of spectral functions

RESULTS



relativistic effects
are huge

RESULTS



(J.E.S. arXiv: 1706.06739)

giant resonances
not visible (large
momentum transfer)

relativistic effects
are huge

other mechanism
overlap with the
QE peak:
2p2h + delta prod.

IDEAS TO TAKE HOME

- We need a precise knowledge of neutrino-nucleus interaction. Nuclear effects are crucial for the analysis of neutrino experimental data
- First we should see how the models work for electron scattering.
- One has to account for different mechanisms: quasielastic, 2p2h, delta excitation...
- The fact that we are dealing with high energy transfer is a challenge

THANK YOU!
